

U.S.N.

B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

June 2025 Semester End Main Examinations**Programme: B.E.****Semester: III****Branch: Artificial Intelligence and Machine Learning****Duration: 3 hrs.****Course Code: 23AM3PCPSM****Max Marks: 100****Course: Probability and Statistics for Machine Learning**

- Instructions:** 1. Answer any FIVE full questions, choosing one full question from each unit.
2. Missing data, if any, may be suitably assumed.

Important Note: Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.

		UNIT - I	CO	PO	Marks																									
1	a)	What are some real-world applications of probability in machine learning?	CO2	PO1	05																									
	b)	Let A_1, A_2, A_3 and A_4 be mutually independent events such that $P(A_1) = 1/2$, $P(A_2) = 1/4$, $P(A_3) = 1/8$ and $P(A_4) = 1/16$. What is the value of $P(A_1 \cup A_2) + P(A_3 \cup A_4) - P(A_1 \cap A_2 \cap A_3 \cap A_4)$	CO1	PO2	08																									
	c)	The joint probability distribution of X and Y is given below: <table><tr><td></td><td>Y</td><td>1</td><td>3</td><td>9</td></tr><tr><td>X</td><td></td><td></td><td></td><td></td></tr><tr><td>2</td><td></td><td>1/8</td><td>1/24</td><td>1/12</td></tr><tr><td>4</td><td></td><td>1/4</td><td>1/4</td><td>0</td></tr><tr><td>6</td><td></td><td>1/8</td><td>1/24</td><td>1/12</td></tr></table> i. Find the marginal probability distribution of Y. ii. Find the conditional distribution of Y given that $X = 2$ iii. Are X and Y independent?		Y	1	3	9	X					2		1/8	1/24	1/12	4		1/4	1/4	0	6		1/8	1/24	1/12	CO1	PO2	07
	Y	1	3	9																										
X																														
2		1/8	1/24	1/12																										
4		1/4	1/4	0																										
6		1/8	1/24	1/12																										
		OR																												
2	a)	Explain the intuition behind joint, marginal, and conditional probability.	CO2	PO1	06																									
	b)	The odds against Algorithm A successfully classifying data are 8:6, and the odds in favor of Algorithm B successfully classifying the same data are 14:16. i. What is the chance that neither algorithm successfully classifies the data, if they both try, independently of each other? ii. What is the probability that the data will be successfully classified by either algorithm?	CO3	PO1	08																									

	c)	Explain the following with an example: i. Random experiment ii. Event iii. Trials	CO2	PO1	06																																																							
		UNIT - II																																																										
3	a)	How do Maximum A Posteriori (MAP) and Maximum Likelihood Estimation (MLE) techniques differ?	CO2	PO1	06																																																							
	b)	Given three urns, where the first urn contains 7 white and 10 black balls, the second urn contains only black balls, and the third urn contains 17 white balls, a person randomly selects an urn and draws a ball, which turns out to be white. What is the total probability that the white ball drawn came from the first urn and the third urn, respectively?	CO2	PO2	08																																																							
	c)	How does the Gaussian Naive Bayes Classifier work, and what assumptions does it make about the features? What are its advantages and limitations?	CO1	PO2	06																																																							
		OR																																																										
4	a)	Use the naive Bayes method to determine if a loan with attributes $X = (\text{Home Owner} = \text{No}, \text{Marital Status} = \text{Married}, \text{Income} = \text{High})$ should be classified as a Defaulted Borrower or not. Determine which is larger, $P(\text{Yes} X)$ or $P(\text{No} X)$. <table><tr><th>Tid</th><th>Home Owner</th><th>Marital Status</th><th>Annual Income</th><th>Defaulted Borrower</th></tr><tr><td>1</td><td>Yes</td><td>Single</td><td>High</td><td>No</td></tr><tr><td>2</td><td>No</td><td>Married</td><td>High</td><td>No</td></tr><tr><td>3</td><td>No</td><td>Single</td><td>Low</td><td>No</td></tr><tr><td>4</td><td>Yes</td><td>Married</td><td>High</td><td>No</td></tr><tr><td>5</td><td>No</td><td>Divorced</td><td>Low</td><td>Yes</td></tr><tr><td>6</td><td>No</td><td>Married</td><td>Low</td><td>No</td></tr><tr><td>7</td><td>Yes</td><td>Divorced</td><td>High</td><td>No</td></tr><tr><td>8</td><td>No</td><td>Single</td><td>Low</td><td>Yes</td></tr><tr><td>9</td><td>No</td><td>Married</td><td>Low</td><td>No</td></tr><tr><td>10</td><td>No</td><td>Single</td><td>Low</td><td>Yes</td></tr></table>	Tid	Home Owner	Marital Status	Annual Income	Defaulted Borrower	1	Yes	Single	High	No	2	No	Married	High	No	3	No	Single	Low	No	4	Yes	Married	High	No	5	No	Divorced	Low	Yes	6	No	Married	Low	No	7	Yes	Divorced	High	No	8	No	Single	Low	Yes	9	No	Married	Low	No	10	No	Single	Low	Yes	CO3	PO3	10
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	b)	A medical test detects a rare disease affecting 1 in 1000 people. The test has a 99% accuracy rate. Using Bayes' theorem, explain prior, posterior, and likelihood probabilities. Calculate the probability that a person who tests positive actually has the disease.	CO3	PO2	10																																																							
		UNIT - III																																																										
5	a)	Define a random variable and explain its types with appropriate examples.	CO1	PO1	06																																																							
	b)	Calculate the expectation of the number of failures preceding the first success in an infinite series of independent trials, each with constant probability 'p' of success.	CO1	PO2	08																																																							

	c)	A player tosses two fair coins. He wins Rs.5 if two head occur, Rs. 2 if one head occurs and Re. 1 if no head occurs. Calculate the variance of the player's gain.	CO1	PO3	06
		OR			
6	a)	Consider a survey where X represents customer satisfaction (1 for satisfied, 0 for not satisfied) and Y represents customer recommendation (1 for yes, 0 for no). The joint probability distribution is: $P(0,0) = 0.5, P(0,1) = 0.2, P(1,0) = 0.2, P(1,1) = 0.1$. i. Are X and Y independent? Explain. ii. Are (X+Y) and (X-Y) independent? Explain.	CO2	PO2	10
	b)	If X is a Poisson variable such that $P(X = 2) = 9P(X = 4)$ i. Compute the parameter λ . ii. Compute the mean and variance of X. iii. Calculate $P(X = 0)$.	CO1	PO2	10
		UNIT - IV			
7	a)	The Life times of a certain kind of electronic devices have a mean of 300 hours and a S.D of 25 hours. Assuming that the distribution of these life times to be approximated closely to normal curve. i. Find the probability that any one of these electronic devices will have a life time of more than 350 hours ii. What percentage will have lifetimes of 300 hours or less? iii. What percentage will have lifetimes from 220 to 260 hours?	CO3	PO2	10
	b)	The waiting time (in minutes) for the next train follows a uniform distribution over the interval (a, b) with the probability density function $f(x) = \frac{1}{b-a} \quad a < x < b$ i. Determine the mean and variance of the waiting time. ii. For a specific case where a = 0 and b = 30 minutes, calculate the probability that a person will wait at least 20 minutes.	CO2	PO2	10
		OR			
8	a)	A machine in a factory process orders sequentially, one after another. The time (in minutes) required to complete an order follows a continuous distribution with the probability density function: $f(x) = Kx^2, 0 < x < 5$. i. Determine the value of K. ii. Compute the expectation (mean) processing time. iii. Find the probability that processing takes more than 4 minutes given that it has already exceeded 3 minutes.	CO1	PO2	10
	b)	In a credit card fraud detection system, 5% of transactions are classified as fraudulent. A sample of 3000 transactions is selected for analysis. i. State the Central Limit Theorem (CLT) and explain how it can be applied in this scenario. ii. Explain the concept of the continuity correction factor and why it is necessary when applying CLT to approximate probabilities from a discrete distribution.	CO3	PO2	10

			iii. Using CLT and the continuity correction factor, calculate the probability that the sample contains between 140 and 150 fraudulent transactions (inclusive of both limits).																			
			UNIT - V																			
	9	a)	Why do researchers often prefer sampling over studying the entire population?	CO2	PO1	06																
		b)	Calculate the standard deviation from the following data: <table><tr><td>Marks</td><td>0-10</td><td>10-20</td><td>20-30</td><td>30-40</td><td>40-50</td><td>50-60</td><td>60-70</td></tr><tr><td>No. of Students</td><td>5</td><td>7</td><td>14</td><td>12</td><td>9</td><td>6</td><td>2</td></tr></table>	Marks	0-10	10-20	20-30	30-40	40-50	50-60	60-70	No. of Students	5	7	14	12	9	6	2	CO3	PO2	10
Marks	0-10	10-20	20-30	30-40	40-50	50-60	60-70															
No. of Students	5	7	14	12	9	6	2															
		c)	The weekly salaries (in ₹) of five employees are: 12,000, 15,000, 18,000, 22,000, 25,000. Compute the first quartile (Q_1) and the third quartile (Q_3).	CO3	PO3	04																
			OR																			
	10	a)	An economic analyst is studying the income distribution of a small town. After collecting income data from various households, the analyst needs to summarize this data using a measure of central tendency. Describe the characteristics of a good measure of central tendency, and identify which measure (mean, median, or mode) would be most appropriate for this data and why.	CO1	PO1	06																
		b)	The heights (in cm) of five students are given as: 150, 155, 160, 165, 170. i. Compute the mean of the given data. ii. If each student's height is measured relative to 150 cm (i.e., subtract 150 from each value), find the mean of the transformed data. iii. Verify whether the mean remains unchanged due to this shift in origin.	CO3	PO2	08																
		c)	A researcher analyses test scores of 200 students. She calculates the mean, median, and standard deviation and creates histograms. She then uses the data to predict overall student performance and tests score differences between two departments. 1. Identify the descriptive statistics used. 2. Identify the inferential statistics used. 3. Explain the difference between descriptive and inferential statistics using this example.	CO3	PO2	06																
