

# B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

## August 2024 Supplementary Examinations

Programme: B.E.

Branch: Institutional Elective

Course Code: 21CV7OEFEA

Course: Finite Element Analysis

Semester: VII

Duration: 3 hrs.

Max Marks: 100

**Instructions:** 1. Answer any FIVE full questions, choosing one full question from each unit.  
2. Missing data, if any, may be suitably assumed.

### UNIT - I

- 1 a) Derive equation of equilibrium for three dimensional stress state. **10**  
b) Discuss with example plane stress and plane strain conditions. Derive stress strain relation for plane-stress condition. **10**

OR

- 2 a) A simply supported beam is subjected to a uniformly distributed load. Determine maximum deflection using Rayleigh Ritz method. **10**  
b) Explain in detail the steps involved in the finite element analysis for solving a problem. **10**

### UNIT - II

- 3 a) List the properties of stiffness matrix. **05**  
b) With a neat sketch, derive stiffness matrix for a 1-D bar element. **10**  
c) Define shape function. List the properties of shape functions. **05**

### UNIT - III

- 4 Analyze the beam for member end forces as shown in Fig.1, by using FE technique. **20**

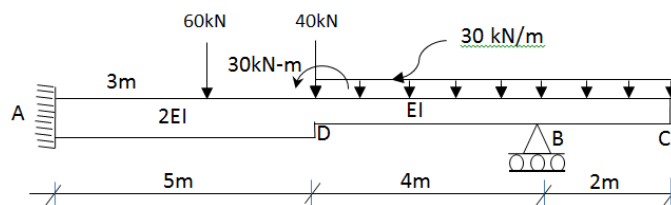


Fig. 1

### UNIT - IV

- 5 a) Obtain expression for shape functions of CST element. Sketch their variations. **10**  
b) Derive shape functions of a 9-noded 2D quadrilateral element using Lagrange polynomials. **10**

**Important Note:** Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.

## UNIT - V

- 6 a) Derive stiffness matrix for a 4-noded quadrilateral isoparametric element. **16**  
b) Write the characteristics of a Jacobian matrix. **04**

OR

- 7 a) For the quadrilateral element shown in figure 2, find the Jacobian matrix at  $\xi = \frac{1}{4}$  and  $\eta = \frac{1}{4}$ . **10**

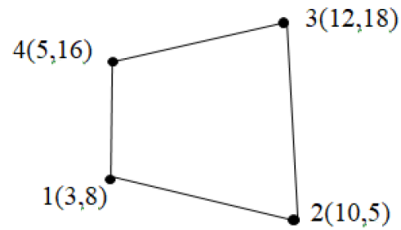


Fig. 2

- b) A four-noded quadrilateral element has coordinates 1(10, 10), 2(50, 10), 3(60, 60) and 4(10, 40). If the element nodal displacement vector is given by  $\{q\} = \{0, 0, 1, 2, 0, 1.5, 1, 0\}$  mm, determine (i) the  $x$  &  $y$  coordinates of point P which has  $\xi = 0.5$  and  $\eta = 0.5$  and (ii) displacements  $u$  &  $v$  of the point P. **10**

\*\*\*\*\*