

# B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

## October 2024 Supplementary Examinations

Programme: B.E.

Branch: CSE (ICB), AI&DS, CSE (DS)

Course Code: 23DC4PCDAA

Course: Design and Analysis of Algorithms

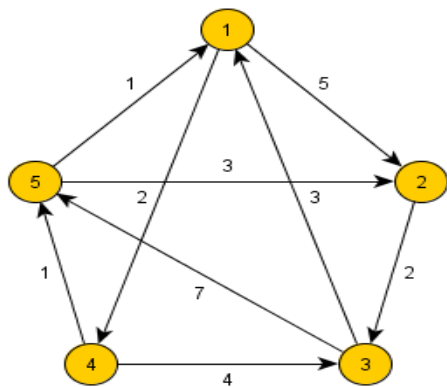
Semester: IV

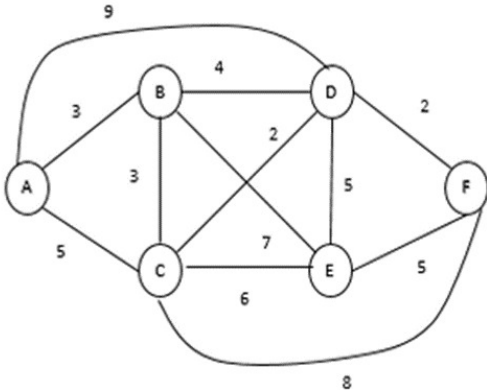
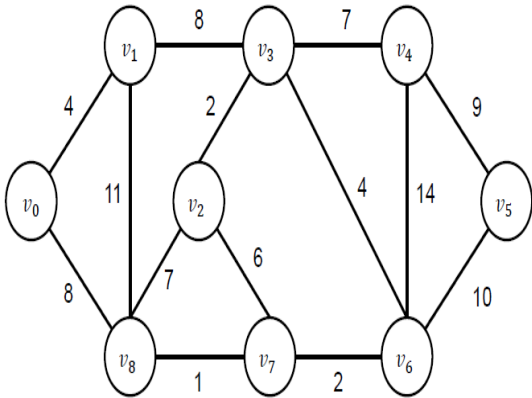
Duration: 3 hrs.

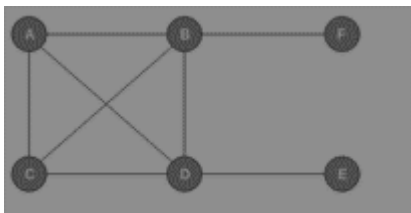
Max Marks: 100

**Instructions:** 1. Answer any FIVE full questions, choosing one full question from each unit.  
2. Missing data, if any, may be suitably assumed.

Important Note: Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.			UNIT - I	CO	PO	Marks
	1	a)	Demonstrate with an example Worst case, Best case time complexity of an algorithm.	CO1	PO1	06
		b)	Discuss the general plan to find the efficiency of recursive algorithms. Apply the same to find the efficiency of solving Tower of Hanoi problem.	CO1	PO1	08
		c)	Analyze the time complexity for the following codes. Show the steps clearly.	CO2	PO2	06
			<pre> int a = 0, i = N; while (i &gt; 0) {     a += i;     i /= 2; } </pre>			
			<pre> int recursivefun (int n) {     if(n&lt;=0)         return 1;     else         return 1+ recursivefun (n/5) } </pre>			
			UNIT - II			
	2	a)	Differentiate between different variations of Decrease and Conquer technique with an example.	CO2	PO2	06
		b)	Apply Johnson Trotter method to generate permutations for the set {4,5,6}. Write the algorithm for the same.	CO2	PO2	06
		c)	Apply the DFS-based algorithm and source removal method to solve the topological sorting problem for the following digraph. Also prove that the topological sorting problem has a solution if and only if it is a DAG.	CO3	PO3	08
			<pre> graph TD     a((a)) --&gt; b((b))     b((b)) --&gt; e((e))     e((e)) --&gt; g((g))     g((g)) --&gt; f((f))     f((f)) --&gt; c((c))     c((c)) --&gt; a((a))     d((d)) --&gt; a((a))     d((d)) --&gt; b((b))     d((d)) --&gt; e((e))     d((d)) --&gt; f((f))     d((d)) --&gt; g((g)) </pre>			

		<b>UNIT - III</b>			
3	a)	Apply Strassen's matrix multiplication to multiply following matrices. Discuss how this method is better than the direct matrix multiplication. $\begin{bmatrix} 3 & 1 \\ 4 & 2 \end{bmatrix} * \begin{bmatrix} 2 & 3 \\ 5 & 6 \end{bmatrix}$	CO2	PO2	07
	b)	Write the bottom up algorithm for Heap construction. Construct a heap for the list 1, 8, 6, 5, 3, 7, 4 by using bottom-up algorithm.	CO1	PO1	07
	c)	Illustrate the tracing of Quicksort algorithm for the following set of numbers. 54, 26, 93, 17, 77, 31, 44, 55, 20	CO2	PO2	06
		<b>OR</b>			
4	a)	Consider the problem of searching for genes in DNA sequences using Horspool's algorithm. A DNA sequence is represented by a text on the alphabet {A, C, G, T}, and the gene or gene segment is the pattern. a. Construct the shift table for the following gene segment. TCCTATTCTT  b. Apply Horspool's algorithm to locate the above pattern in the following DNA sequence:  CGTATTCTTTTATAGATCTCCTATTCTT	CO3	PO3	08
	b)	Apply Horner's rule to evaluate the polynomial $p(x) = 3x^4 - x^3 + 2x + 5$ at $x = -2$ .	CO2	PO2	06
	c)	Is Merge sort better than Quick sort, in the worst case. Justify your answer by deriving the time complexities for both in worst case.	CO1	PO1	06
		<b>UNIT - IV</b>			
5	a)	Apply Floyd's algorithm to find all pair shortest path for the given graph below. 	CO1	PO1	06

	b)	<p>In a telephone network, each line has a bandwidth, <math>bw</math>. The bandwidth of transmission line is the highest frequency that that line can support. Imagine a city to be a graph, the vertices represent the switching stations, and the edges represent the transmission lines and the weight of the edges represent <math>bw</math>. Use appropriate algorithm to establish the call through lowest Bandwidth. Assume the connection has to be established from A.</p> 	CO2	PO1	08							
	c)	<p>The characters a to h have the set of frequencies based on the first 8 Fibonacci numbers as follows: a : 1, b : 1, c : 2, d : 3, e : 5, f : 8, g : 13, h : 21 A Huffman code is used to represent the characters. What is the sequence of characters corresponding to the following code? 1101111001110101</p>	CO3	PO3	06							
		OR										
6	a)	<p>Obtain the solution for a knapsack problem using dynamic method with knapsack capacity <math>M=6</math>, <math>n=3</math>, <math>(w_1, w_2, w_3) = (1, 2, 3)</math> and <math>(p_1, p_2, p_3) = (10, 15, 40)</math>. Analyze its efficiency</p>	CO2	PO2	08							
	b)	<p>Using the modified prim's algorithm to find the maximum spanning tree for the following graph.</p> 	CO3	PO3	08							
	c)	<p>For the following instance of coin row problem, apply dynamic programming approach.</p> <table border="1" data-bbox="347 1953 1171 2040"><tr><td>Coin Denominations</td><td>6</td><td>2</td><td>9</td><td>11</td><td>7</td><td>4</td></tr></table>	Coin Denominations	6	2	9	11	7	4	CO1	PO1	04
Coin Denominations	6	2	9	11	7	4						

			<b>UNIT - V</b>																							
7	a)	Solve the following instance of the knapsack problem by the branch and bound algorithm. Assume knapsack weight is W=15. <table><tr><th>Item</th><th>Weight</th><th>Profit</th></tr><tr><td>1</td><td>5</td><td>40</td></tr><tr><td>2</td><td>7</td><td>35</td></tr><tr><td>3</td><td>2</td><td>18</td></tr><tr><td>4</td><td>4</td><td>4</td></tr><tr><td>5</td><td>5</td><td>10</td></tr><tr><td>6</td><td>1</td><td>2</td></tr></table>	Item	Weight	Profit	1	5	40	2	7	35	3	2	18	4	4	4	5	5	10	6	1	2	CO 2	PO2	<b>08</b>
Item	Weight	Profit																								
1	5	40																								
2	7	35																								
3	2	18																								
4	4	4																								
5	5	10																								
6	1	2																								
	b)	Show the state space tree for finding sum of subset for the set X={5,8,13} with d=13 using Backtracking technique. Show all the solutions.	CO2	PO2	<b>06</b>																					
	c)	Write Approximation Vertex Cover Algorithm. Apply the Approximation Vertex Cover Algorithm for the following graph and find the vertex cover for the same. 	CO2	PO2	<b>06</b>																					

\*\*\*\*\*