

# B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

## February 2025 Semester End Main Examinations

**Programme: B.E.**

**Branch: Computer Science and Engineering**

**Course Code: 22CS4PCADA**

**Course: Analysis and Design of Algorithms**

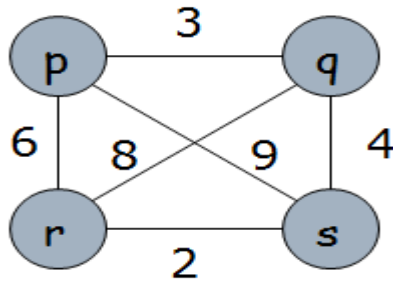
**Semester: IV**

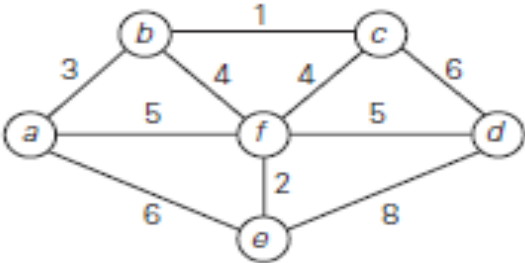
**Duration: 3 hrs.**

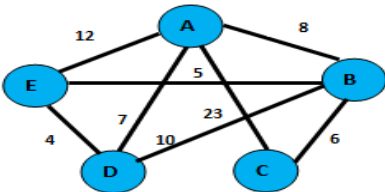
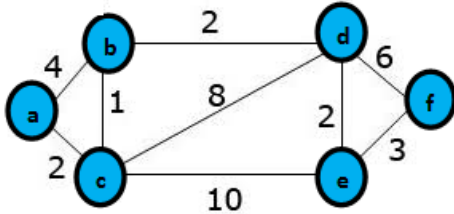
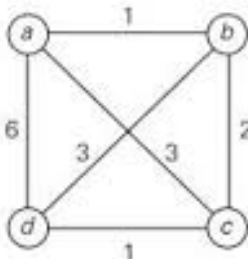
**Max Marks: 100**

**Instructions:** 1. Answer any FIVE full questions, choosing one full question from each unit.  
2. Missing data, if any, may be suitably assumed.

Important Note: Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.			UNIT - I	CO	PO	Marks
	1	a)	Demonstrate worst case best case and average case scenario complexity of an algorithm with an example.	CO1	PO1	8
		b)	With the help of a flowchart, explain the various stages of algorithm design process.	CO1	PO1	8
		c)	Solve the following recurrence relation using backward substitution method. i. $x(n) = x(n/2) + n$ for $n > 1$ , $x(1) = 1$ ii. $x(n) = x(n-1) + 5$ for $n > 1$ and $x(0) = 0$	CO1	PO1	4
			OR			
	2	a)	By applying the steps in finding out the time complexity of non-recursive algorithm shown below. Find the time complexity for the following code.  i. <pre>void main() {   int i, j, k = 0;   for (i = n/2; i &lt;= n; i++)   {     for (j = 2; j &lt;= n; j = j * 2)     {       k = k + n / 2;     }   } }</pre>	CO2	PO1	4
		b)	Write recursive algorithm for Towers of Hanoi problem for “n” disks. Draw the recursion tree for $n=3$ and showing the order of moves	CO2	PO1	6
		c)	Apply selection sort technique to sort the list {O, N, L, I, N, E, T, E, S, T} in alphabetical order showing the output of each pass during the sorting process. Write an algorithm for the same and find its time complexity	CO2	PO1	10

		<b>UNIT - II</b>			
3	a)	Apply exhaustive search technique to list all tours starting from city 'p' and find the minimum cost route among them. 	CO2	PO1	<b>4</b>
	b)	Differentiate between different variations of Decrease and Conquer technique with an example	CO2	PO2	<b>6</b>
	c)	Determine the number of character comparisons made by the Brute-Force pattern matching algorithm in searching for the pattern "WOOD" in the text "TWO_ROADS_DIVERGED_IN_A_YELLOW_WOOD". Also write an algorithm for the same and derive the best-case and worst-case time complexities.	CO1	PO2	<b>10</b>
		<b>OR</b>			
4	a)	Apply Decrease and Conquer technique to find Topological order for the following graph using DFS method and Source Removal method with the source vertex '1'.	CO2	PO1	<b>10</b>
	b)	Apply Johnson Trotter method to generate permutations for the following set. 1,2,3,4	CO2	PO1	<b>6</b>
	c)	Apply Exhaustive Search technique to solve the following instance of Knapsack problem: Number of objects N=4, weights of four objects= {7, 3, 4, 5} and profits= {42, 12, 40, 25} with the capacity of Knapsack W=10	CO2	PO1	<b>4</b>
		<b>UNIT - III</b>			
5	a)	Given the numbers {10,34,22,11,54,66,33,24,25,56,77,21}. Construct MergeSort tree to sort these numbers in the ascending order. Also write an algorithm for Merge sort.	CO2	PO2	<b>8</b>
	b)	For the given array, write an algorithm to determine mode using the concept of presorting and analyze its time complexity	CO1	PO1	<b>6</b>
	c)	Briefly explain different variations of Transform and Conquer technique, explain each with an example.	CO2	PO1	<b>6</b>
		<b>OR</b>			
6	a)	Is merge sort is better than quick sort in the worst case, justify your answer by deriving the time complexities for both in worst case.	CO1	PO2	<b>8</b>

	b)	Create a min heap tree for the following list of elements and sort an array. Also, write the algorithm for the same. <div>{58, 25, 35, 38, 110, 48, 18}</div>	CO2	PO1	8																																																												
	c)	Apply divide and conquer technique to multiply the following two long integers: <div>2547 and 1605</div>	CO2	PO1	4																																																												
		UNIT - IV																																																															
7	a)	Suppose the knapsack problem is solved by Dynamic programming technique and the solution table is given below. Explain step by step process of selecting objects to get optimal solution. Consider number of objects=4, Weight={1,5,3,4} for the items with the number (1,2,3,4), Capacity of Knapsack=8 <table><tr><td></td><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td></tr><tr><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td></tr><tr><td>1</td><td>0</td><td>15</td><td>15</td><td>15</td><td>15</td><td>15</td><td>15</td><td>15</td><td>15</td></tr><tr><td>2</td><td>0</td><td>15</td><td>15</td><td>15</td><td>15</td><td>15</td><td>25</td><td>25</td><td>25</td></tr><tr><td>3</td><td>0</td><td>15</td><td>15</td><td>15</td><td>24</td><td>24</td><td>25</td><td>25</td><td>25</td></tr><tr><td>4</td><td>0</td><td>15</td><td>15</td><td>15</td><td>24</td><td>24</td><td>25</td><td>25</td><td>29</td></tr></table>		0	1	2	3	4	5	6	7	8	0	0	0	0	0	0	0	0	0	0	1	0	15	15	15	15	15	15	15	15	2	0	15	15	15	15	15	25	25	25	3	0	15	15	15	24	24	25	25	25	4	0	15	15	15	24	24	25	25	29	CO2	PO1	6
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	b)	Apply Krushkals's algorithm to find minimum spanning tree for the following graph. Also write an algorithm for the same 	CO2	PO1	8																																																												
	c)	Suppose the string below is to be sent over a network. Construct a Huffman tree and find the code word for each character. Justify how Huffman tree reduces the string size through encoding compare to sending original string. <div>BCAADDCCACACAC</div>	CO2	PO1	6																																																												
		OR																																																															
8	a)	Design Dynamic programming based algorithm to find all pair shortest paths. Apply the same to the below graph	CO2	PO1	10																																																												

																				
	b)	<p>Design a Greedy algorithm for finding single source shortest paths. Apply the same on the below graph to find shortest paths from vertex 'A' to all other nodes.</p> 	CO2	PO1	10															
		UNIT - V																		
9	a)	Write the state space tree for finding sum of subset for the set $X=\{5,8,13\}$ with $d=13$ using Backtracking technique.	CO2	PO1	6															
	b)	Distinguish between P, NP and NP completeness problem	CO3	PO2	6															
	c)	<p>Apply Branch and Bound approach to solve the Knapsack problem for the following data.</p> <p>Number objects <math>n=4</math>, Knapsack Capacity <math>M=10</math></p> <table border="1" data-bbox="561 1113 952 1408"> <thead> <tr> <th>Item No.</th> <th>Profit</th> <th>Weight</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>40</td> <td>4</td> </tr> <tr> <td>2</td> <td>42</td> <td>7</td> </tr> <tr> <td>3</td> <td>25</td> <td>5</td> </tr> <tr> <td>4</td> <td>12</td> <td>3</td> </tr> </tbody> </table>	Item No.	Profit	Weight	1	40	4	2	42	7	3	25	5	4	12	3	CO2	PO1	8
Item No.	Profit	Weight																		
1	40	4																		
2	42	7																		
3	25	5																		
4	12	3																		
		OR																		
10	a)	Apply backtracking approach to write state space tree to find sum of subsets for set $S=\{5, 5, 10\}$ and $d=10$ .	CO2	PO1	10															
	b)	<p>Apply branch and bound technique for the travelling salesman problem to the below graph.</p> 	CO2	PO1	10															

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