

B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

September / October 2023 Supplementary Examinations**Programme: B.E****Branch: Computer Science and Engineering****Course Code: 19CS4PCTFC****Course: Theoretical Foundations of Computations****Semester: IV****Duration: 3 hrs.****Max Marks: 100****Date: 21.09.2023**

Instructions: 1. Answer any FIVE full questions, choosing one full question from each unit.
2. Missing data, if any, may be suitably assumed.

UNIT - I

- 1 a) Design DFA for accepting strings ($\Sigma = \{0,1\}$) 10
- i. Whose Length is divisible by 3
 - ii. Which have the pattern 001
 - iii. Which ends with the pattern 011
 - iv. Whose value is divisible by 2
 - v. Which have minimum three 1's in it.
- b) Design NFA for accepting strings over $\Sigma = \{0,1\}$ which has a 1 in the second last position. Convert the resulting NFA to DFA by subset construction method. 7
- c) Design epsilon NFA for accepting signed integer. 3

UNIT - II

- 2 a) Design regular expressions for accepting the below languages over $\Sigma = \{a,b\}$. 12
- i. Strings start with ab or ba
 - ii. Strings having even number of a's
 - iii. Strings having alternate a's and b's
 - iv. Strings of odd length
 - v. Strings end with abb
 - vi. Strings having baa
- b) Show that regular languages are closed under 8
- i. Union
 - ii. Complementation
 - iii. Intersection.

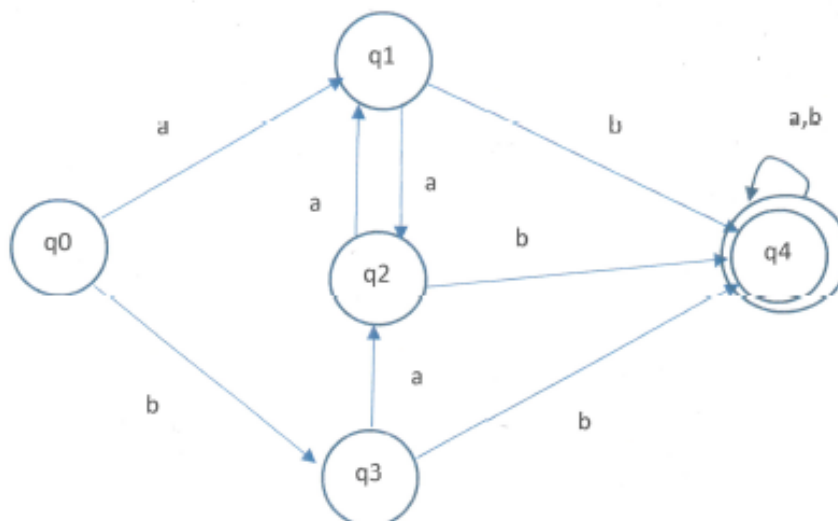
Important Note: Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.

OR

- 3 a) Convert the below DFA to regular expression using Kleene's theorem: 10

	0	1
$\rightarrow q0$	q1	q0
$*q1$	q1	q1

- b) Minimize the below DFA. Here, $\Sigma = \{a, b\}$ 10



UNIT - III

- 4 a) Design Context Free Grammar (CFG) for below languages. 10

- i. $L = \{a^n b^n c^m \mid n, m \geq 0\}$
- ii. $L = \{w \mid w \text{ is string of } a\text{'s and } b\text{'s and } w \text{ is palindrome}\}$
- iii. $L = \{a^n b^m \mid n < m, m, n \geq 0\}$
- iv. $L = \{a^n b^m c^m d^n \mid m, n \geq 1\}$
- v. $L = \{w \mid w \text{ is string of } a\text{'s and } b\text{'s and } |w| \bmod 3 = 0\}$

- b) Derive the string **00011** using below grammar with Leftmost and Rightmost derivation. 5

$S \rightarrow A1B$
 $A \rightarrow 0A \mid \epsilon$
 $B \rightarrow 0B \mid 1B \mid \epsilon$

- c) Eliminate epsilon productions in the grammar. Given below 5

$S \rightarrow ABCa \mid bD$
 $A \rightarrow BC \mid b$
 $B \rightarrow b \mid \epsilon$
 $C \rightarrow c \mid \epsilon$
 $D \rightarrow d$

OR

- 5 a) Eliminate the useless symbols and productions in the below grammar. 10

$S \rightarrow aA|bB$
 $A \rightarrow aA|a$
 $B \rightarrow bB$
 $D \rightarrow ab|Ea$
 $E \rightarrow aC|d$

- b) Convert the below grammar to CNF. 5

$S \rightarrow 0A|1B$
 $A \rightarrow 0AA|1S|1$
 $B \rightarrow 1A|0$

- c) Show that the below grammar is ambiguous. 5

$S \rightarrow aB|bA$
 $A \rightarrow aS|bAA|a$
 $B \rightarrow bS|aBB|b$

UNIT - IV

- 6 a) Design a Push Down Automata (PDA) for accepting the language $L = \{WCW^R | W \text{ is string of } a's \text{ and } b's\}$ 6

- b) Convert the below grammar to PDA. 6

$S \rightarrow aABC$
 $A \rightarrow aB|a$
 $B \rightarrow bA|b$
 $C \rightarrow a$

- c) Design PDA for accepting $L = \{a^n b^{2n} | n \geq 1\}$. Also check whether the string "aabbabb" is accepted or not using ID. 8

UNIT - V

- 7 a) Design Turing machine for accepting $L = \{0^n 1^n | n \geq 1\}$. Also show whether the string "00111" is accepted or not. 9

- b) Design Turing machine to accept the strings that end with 011 ($\Sigma = \{0,1\}$). 6

- c) Describe the Multi tape Turing machine with a neat diagram. 5
