

U.S.N.

B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

June 2025 Semester End Main Examinations

Programme: B.E.

Semester: IV

Branch: Computer Science and Engineering

Duration: 3 hrs.

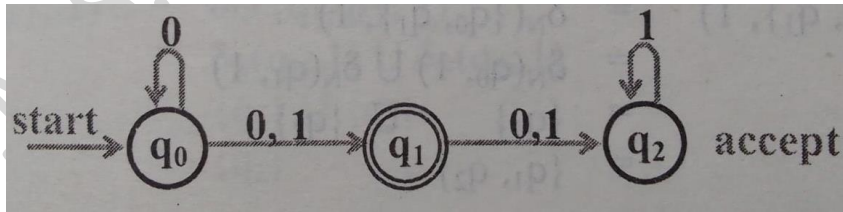
Course Code: 19CS4PCTFC

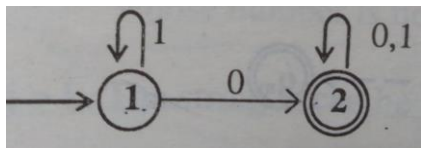
Max Marks: 100

Course: Theoretical Foundations of Computations

- Instructions:** 1. Answer any FIVE full questions, choosing one full question from each unit.
2. Missing data, if any, may be suitably assumed.

Important Note: Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.

		UNIT - I	CO	PO	Marks																		
1	a)	Construct a DFA to accept strings of a's and b's having even number of a's and even number of b's.	CO1	PO1	8																		
	b)	Construct DFA's accepting the following strings over the alphabet set $\Sigma = \{a,b\}$ i. Not more than three a's in the strings ii. The set of all strings except those which ends with 'abb' iii. Set of all strings containing the substring 'abb'	CO3	PO3	8																		
	c)	Write the formal definition of DFA.	CO1	PO1	4																		
		OR																					
2	a)	i. Design a deterministic finite automaton which accepts a string containing "the" anywhere in a string of {a-z} ii. Design a deterministic finite automaton which accepts a string containing "ing" at the end of a string in a string of {a-z}	CO1	PO1	8																		
	b)	Convert the below NFA to its equivalent DFA. 	CO3	PO3	8																		
	c)	Write the formal definition of ϵ - NFA.	CO1	PO1	4																		
		UNIT - II																					
3	a)	Minimize the following DFA using table filling algorithm. <table border="1" data-bbox="331 1870 641 2094"><tr><td>δ</td><td>a</td><td>b</td></tr><tr><td>$\rightarrow A$</td><td>B</td><td>E</td></tr><tr><td>B</td><td>C</td><td>F</td></tr><tr><td>*C</td><td>D</td><td>H</td></tr><tr><td>D</td><td>E</td><td>H</td></tr><tr><td>E</td><td>F</td><td>I</td></tr></table>	δ	a	b	$\rightarrow A$	B	E	B	C	F	*C	D	H	D	E	H	E	F	I	CO2	PO2	8
δ	a	b																					
$\rightarrow A$	B	E																					
B	C	F																					
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D	E	H																					
E	F	I																					

		<table><tr><td>*F</td><td>G</td><td>B</td></tr><tr><td>G</td><td>H</td><td>B</td></tr><tr><td>H</td><td>I</td><td>C</td></tr><tr><td>*I</td><td>A</td><td>E</td></tr></table>	*F	G	B	G	H	B	H	I	C	*I	A	E			
*F	G	B															
G	H	B															
H	I	C															
*I	A	E															
	b)	Obtain Regular Expressions (RE) for the following languages i. All strings containing at least one a and at least one b where $\Sigma = \{a,b,c\}$ ii. All strings that do not end with 01 where $\Sigma = \{0,1\}$ iii. All strings whose length is a multiple of 3 given $\Sigma = \{a,b\}$.	CO3	PO3	8												
	c)	Elaborate on homomorphism and inverse homomorphism properties of a regular expression.	CO1	PO1	4												
		OR															
4	a)	Obtain a regular expression for the FA shown below using Kleen's theorem. 	CO2	PO2	8												
	b)	i. Obtain a Regular Expression for Language $L = \{w: \text{string ends with ab or ba where } w \in \{a,b\}^*\}$ ii. Obtain an NFA for the regular expression $a^* + b^* + c^*$	CO3	PO3	8												
	c)	Show that $L = \{a^n \mid n \geq 0\}$ is not regular.	CO1	PO1	4												
		UNIT - III															
5	a)	Obtain a grammar to generate the language $L = \{a^n b^m \mid n \geq 0, m > n\}$	CO2	PO2	7												
	b)	Consider the grammar $E \rightarrow E + E \mid E * E \mid (E) \mid I$ $I \rightarrow a \mid b \mid c$ Obtain the leftmost and right most derivation for $a + b * c$.	CO2	PO2	5												
	c)	Convert the following grammar to CNF. $S \rightarrow aXbX, X \rightarrow aY \mid bY \mid \epsilon, Y \rightarrow X \mid c$	CO1	PO1	8												
		OR															
6	a)	Obtain CFG for $L = \{w \mid n_a(w) > n_b(w), \Sigma = \{a,b\}\}$	CO2	PO2	8												
	b)	Given the grammar $S \rightarrow aS \mid aSbS \mid \epsilon$, check whether it is ambiguous or not.	CO2	PO2	5												
	c)	Eliminate Useless symbols in the grammar $G = (V, T, P, S)$ $V = \{S, A, B, C, D, E\}$, $T = \{a, b, d\}$, $S = S$ $P = \{S \rightarrow aA \mid bB, A \rightarrow aA \mid a, B \rightarrow bB, D \rightarrow ab \mid Ea, E \rightarrow aC \mid d\}$	CO1	PO1	7												

		UNIT - IV			
7	a)	Obtain a PDA to accept the language $L=\{w w \in (a,b)^* \text{ and } n_a(w)>n_b(w)\}$	CO3	PO3	10
	b)	Obtain the corresponding PDA for the grammar given below. $S \rightarrow aABC$ $A \rightarrow aB a$ $B \rightarrow bA b$ $C \rightarrow a$ Give the instantaneous description of aabba.	CO2	PO2	10
		OR			
8	a)	Obtain a PDA to accept a string of balanced parenthesis. The parentheses to be considered are (,), [,].	CO3	PO3	10
	b)	Obtain a CFG for the given PDA. $\delta(q_0, a, Z) = (q_0, AZ)$ $\delta(q_0, a, A) = (q_0, A)$ $\delta(q_0, b, A) = (q_1, \epsilon)$ $\delta(q_1, \epsilon, Z) = (q_2, \epsilon)$	CO2	PO2	10
		UNIT - V			
9	a)	Design a Turing Machine for $L=\{ww^R\}$. Trace and show the traversal for the string abbaabba.	CO2	PO2	10
	b)	Design a Turing Machine for $L=\{a^n b^n\}$. Show the tracing for string aaabbb.	CO2	PO2	10
		OR			
10	a)	Design a Turing Machine for $L= \{0^n 1^n 2^n, n \geq 1\}$. Demonstrate its correctness by tracing it for the string 001122.	CO2	PO2	10
	b)	Find whether the below lists have a post correspondence solution or not. i. $M = (abb, aa, aaa)$ and $N = (bba, aaa, aa)$ ii. $A = (1, 10111, 10)$ and $B = (111, 10, 0)$	CO2	PO2	10
