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# B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

## August 2024 Semester End Main Examinations

**Programme: B.E.**

**Branch: Computer Science & Engineering**

**Course Code: 22CS4PCTFC**

**Course: Theoretical Foundations of Computations**

**Semester: IV**

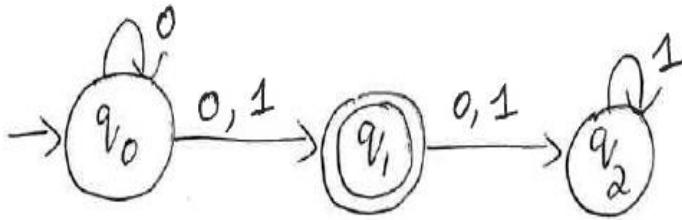
**Duration: 3 hrs.**

**Max Marks: 100**

**Instructions:** 1. Answer any FIVE full questions, choosing one full question from each unit.  
2. Missing data, if any, may be suitably assumed.

<b>UNIT - I</b>			<b>CO</b>	<b>PO</b>	<b>Marks</b>
1	a)	Construct a Deterministic Finite Automata (DFA) to accept a string of a's and b's having not more than three a's	CO3	PO3	<b>5</b>
	b)	List the applications of Automata and explain	CO1	PO2	<b>5</b>
	c)	Convert the given Non-Deterministic Finite Automata (NFA) to its equivalent DFA	CO2	PO2	<b>10</b>
<b>UNIT - II</b>					
2	a)	Obtain regular expression to accept the strings of a's and b's such that every block of four consecutive symbols containing at least two b's.	CO1	PO1	<b>5</b>
	b)	Using Pumping Lemma, show that the language $L = \{a^{n!} \mid n \geq 0\}$ is not regular. Note: $n!$ represents n factorial.	CO2	PO2	<b>6</b>

**Important Note:** Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.



	c)	<p>For the given transition table, obtain the minimized DFA for the following:</p> <table border="1"> <tr> <td><math>\delta</math></td><td>0</td><td>1</td></tr> <tr> <td><math>\rightarrow</math> A</td><td>B</td><td>A</td></tr> <tr> <td>B</td><td>A</td><td>C</td></tr> <tr> <td>C</td><td>D</td><td>B</td></tr> <tr> <td>*D</td><td>D</td><td>A</td></tr> <tr> <td>E</td><td>D</td><td>F</td></tr> <tr> <td>F</td><td>G</td><td>E</td></tr> <tr> <td>G</td><td>F</td><td>G</td></tr> <tr> <td>H</td><td>G</td><td>D</td></tr> </table>	$\delta$	0	1	$\rightarrow$ A	B	A	B	A	C	C	D	B	*D	D	A	E	D	F	F	G	E	G	F	G	H	G	D	CO1	PO1	9
$\delta$	0	1																														
$\rightarrow$ A	B	A																														
B	A	C																														
C	D	B																														
*D	D	A																														
E	D	F																														
F	G	E																														
G	F	G																														
H	G	D																														
		<b>OR</b>																														
3	a)	<p>Obtain Regular Expressions (RE) for the following languages over the alphabet set <math>\Sigma = \{a, b\}</math></p> <ol style="list-style-type: none"> <li>Set of string of a's and b's having substring "aa"</li> <li>Strings of a's and b's whose lengths are multiples of 3</li> <li>Strings that do not end with ab</li> </ol>	CO1	PO1	5																											
	b)	<p>Analyze the following NFA and obtain the regular expression using Kleene's technique for the following DFA.</p>	CO2	PO2	10																											
	c)	Show that $L = \{a^i b^j \mid i > j\}$ is NOT regular using pumping lemma	CO2	PO2	5																											
		<b>UNIT - III</b>																														
4	a)	<p>Obtain a grammar to generate a language consisting of all non-palindromes over <math>\{a, b\}</math>. Give the derivation for the string <b>ababba</b> which is not a palindrome.</p>	CO2	PO2	6																											
	b)	<p>Show that the following grammar is ambiguous.</p> $\begin{aligned} S &\rightarrow AB \mid aaB \\ A &\rightarrow a \mid Aa \\ B &\rightarrow b \end{aligned}$	CO2	PO2	4																											
	c)	<p>Convert the following grammar to its corresponding Chomsky Normal Form (CNF).</p> $\begin{aligned} S &\rightarrow 0A \mid 1B \\ A &\rightarrow 0AA \mid 1S \mid 1 \\ B &\rightarrow 1BB \mid 0S \mid 0 \end{aligned}$	CO2	PO2	10																											

		<b>OR</b>			
5	a)	Show that the following grammar is ambiguous over $w= ( ( ) ( ) )$ $S \rightarrow SS \mid (S) \mid \epsilon$	<i>CO2</i>	<i>PO2</i>	<b>5</b>
	b)	Eliminate useless symbols for the following grammar $S \rightarrow aA \mid a \mid Bb \mid cC$ $A \rightarrow aB$ $B \rightarrow a \mid Aa$ $C \rightarrow cCD$ $D \rightarrow ddd$	<i>CO2</i>	<i>PO2</i>	<b>8</b>
	c)	Analyze the following grammar and eliminate all unit productions from the grammar. $S \rightarrow Aa \mid B \mid Ca$ $B \rightarrow aB \mid b$ $C \rightarrow Db \mid D$ $D \rightarrow E \mid d$ $E \rightarrow ab$	<i>CO2</i>	<i>PO2</i>	<b>7</b>
<b>UNIT - IV</b>					
6	a)	Design Push Down Automata (PDA) for the language $L=\{a^n b^{2n} \mid n \geq 1\}$ . Write an Instantaneous Description for the string <b>aabb</b>	<i>CO3</i>	<i>PO3</i>	<b>5</b>
	b)	Convert the following grammar to PDA $S \rightarrow aABB \mid aAA$ $A \rightarrow aBB \mid a$ $B \rightarrow bBB \mid b$ $C \rightarrow a$	<i>CO2</i>	<i>PO2</i>	<b>10</b>
	c)	Show Context Free Languages (CFL) are not closed under Intersection	<i>CO2</i>	<i>PO2</i>	<b>5</b>
<b>UNIT - V</b>					
7	a)	Differentiate between Recursive Language and Recursively Enumerable Languages	<i>CO2</i>	<i>PO2</i>	<b>5</b>
	b)	Obtain a Turing Machine which accepts the language $L=\{0^n 1^n \mid n \geq 1\}$	<i>CO3</i>	<i>PO3</i>	<b>10</b>
	c)	Describe undecidable problems	<i>CO1</i>	<i>PO1</i>	<b>5</b>

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