

B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

February 2025 Semester End Main Examinations

Programme: B.E.

Branch: Computer Science and Engineering

Course Code: 22CS4PCTFC

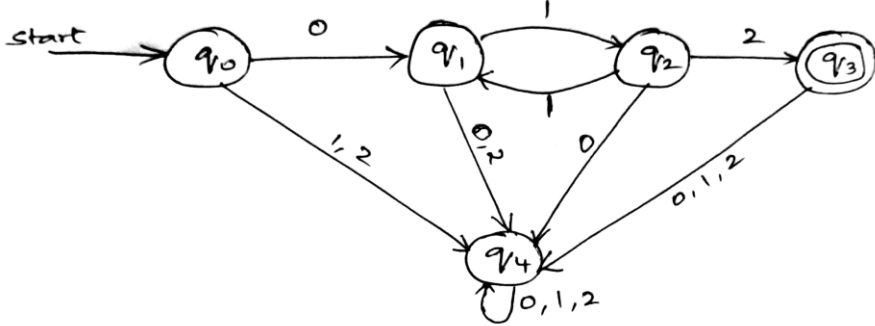
Course: Theoretical Foundations of Computations

Semester: IV

Duration: 3 hrs.

Max Marks: 100

Instructions: 1. Answer any FIVE full questions, choosing one full question from each unit.
2. Missing data, if any, may be suitably assumed.

Important Note: Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.			UNIT - I	CO	PO	Marks
	1	a)	Define Finite Automata. Demonstrate the same using an ON/OFF Switch.	1	1	5
		b)	Analyze the given DFA. Draw the transition table and write the language equivalent. Explain.	1	2	7
						
		c)	Obtain an ϵ -NFA which accepts strings consisting of zero or more a 's followed by zero or more b 's followed by zero or more c 's.	1	3	8
			OR			
	2	a)	Design DFA for accepting binary strings that i) start with 00 ii) having 001 iii) ending with 01 iv) not having 111 v) whose value is multiple of 2	3	3	10
		b)	Design NFA for accepting strings that have 1 in second last position. Convert the same to DFA.	1, 3	1, 3	10
			UNIT - II			
	3	a)	List the notations used to represent regular expressions. Demonstrate the same with an example.	1	1	6

	b)	Analyze the given Finite Automata (FA) and obtain the corresponding regular expression.	1	2	6																											
		<div><p>i.</p><pre>graph LR start((start)) --> q0((q0)) q0 -- 0 --> q1((q1)) q1 -- 1 --> q0 q0 -- 0 --> q2((q2)) q2 -- 1 --> q0 q2 -- 1 --> q3((q3)) q3 -- 0 --> q1 q3 -- "0,1" --> q3 style start fill:none,stroke:none style q0 stroke-width:4px</pre></div> <div><p>ii.</p><pre>graph LR start((start)) --> q0((q0)) q0 -- 0 --> q0 q0 -- 1 --> q1((q1)) q1 -- 1 --> q1 q1 -- 0 --> q2((q2)) q2 -- "0,1" --> q2 style start fill:none,stroke:none style q0 stroke-width:4px</pre></div>																														
	c)	Obtain an Non- Deterministic Finite Automata (NFA) for the regular expression $(a+b)^*aa(a+b)^*$. Show the step by step procedure involved in constructing the NFA.	1	3	8																											
		OR																														
4	a)	Explain closure property – complementation with an example.	1	1	6																											
	b)	Write the regular expressions for the following. i. $L=\{ w : n_a(w) \bmod 3 =0 \text{ where } w=(a,b)^* \}$ ii. $L=\{ a^n b^m \mid m \geq 1, n \geq 1, nm \geq 3 \}$	1	1	6																											
	c)	Obtain the distinguishable table for the automaton and then minimize the states of the following DFA.	1	3	8																											
		<table><tr><th>δ</th><th>a</th><th>b</th></tr><tr><td>A →</td><td>B</td><td>F</td></tr><tr><td>B</td><td>G</td><td>C</td></tr><tr><td>*C</td><td>A</td><td>C</td></tr><tr><td>D</td><td>C</td><td>G</td></tr><tr><td>E</td><td>H</td><td>F</td></tr><tr><td>F</td><td>C</td><td>G</td></tr><tr><td>G</td><td>G</td><td>E</td></tr><tr><td>H</td><td>G</td><td>C</td></tr></table>	δ	a	b	A →	B	F	B	G	C	*C	A	C	D	C	G	E	H	F	F	C	G	G	G	E	H	G	C			
δ	a	b																														
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D	C	G																														
E	H	F																														
F	C	G																														
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H	G	C																														
		UNIT - III																														
5	a)	Show that the below grammar is ambiguous. $S \rightarrow iCtS \mid iCtSeS \mid a$, $C \rightarrow b$	1	1	4																											
	b)	Consider the following context-free grammars. $G1: S \rightarrow aS \mid B, B \rightarrow b \mid bB$	1	2	8																											

		G2: $S \rightarrow aA \mid bB$, $A \rightarrow aA \mid B \mid \epsilon$, $B \rightarrow bB \mid \epsilon$			
		Write the Context free language generated by G1 and G2			
	c)	Analyze the given language and obtain a grammar to generate the following languages: i. $L = \{a^{n+2}b^m \mid n \geq 0 \text{ and } m > n\}$ ii. $L = \{a^n b^m c^k \mid n \geq 0 \text{ and } m > n\}$	2	2	8
		OR			
6	a)	Eliminate useless symbols in the grammar given below: $\{S \rightarrow aA \mid bB, A \rightarrow aA \mid a, B \rightarrow bB, D \rightarrow ab \mid Ea, E \rightarrow aC \mid d\}$	3	1	10
	c)	Consider the grammar. $S \rightarrow 0A \mid 1B$ $A \rightarrow 0AA \mid 1S \mid 1$ $B \rightarrow 1BB \mid 0S \mid 0$ Obtain the grammar in Chomsky Normal Form (CNF).	1	3	10
		UNIT - IV			
7	a)	State the pumping lemma for Context Free languages. Explain with an example.	2	2	5
	b)	Check if the Push Down Automata (PDA) to accept the language $L(M) = \{w \mid w (a+b)^* \text{ and } n_a(w) = n_b(w) \text{ is deterministic or non-deterministic?}$	3	3	5
	c)	For the given grammar, obtain the corresponding PDA. $S \rightarrow aABB \mid aAA$ $A \rightarrow aBB \mid a$ $B \rightarrow bBB \mid A$ $C \rightarrow a$	1	1	10
		OR			
8	a)	Design PDA for accepting $a^n b^{2n}$ such that $n \geq 1$.	3	3	10
	b)	Design PDA to accept $a^n b^n$. Also check whether the PDA is DPDA or NPDA.	3	3	10
		UNIT - V			
9	a)	Discuss about the various components of Turing machine model.	3	3	5
	b)	Find whether the lists given here have a Post Correspondence Solution. $M = (abb, aa, aaa)$ and $N = (bba, aaa, aa)$	3	3	5
	c)	Design a Turing machine to accept the language $L(M) = \{0^n 1^n 2^n \mid n \geq 1\}$	3	3	10
		OR			

	10	a)	Design TM that adds two numbers. Assume numbers are stored on tape as sequence of 1's and separated by a 0.	3	3	10
		b)	Design TM that accepts palindrome strings of a and b.	3	3	10

B.M.S.C.E. - ODD SEM 2024-25