

B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

February 2025 Semester End Main Examinations

Programme: B.E.

Branch: Computer Science and Engineering

Course Code: 22CS4PCTFC

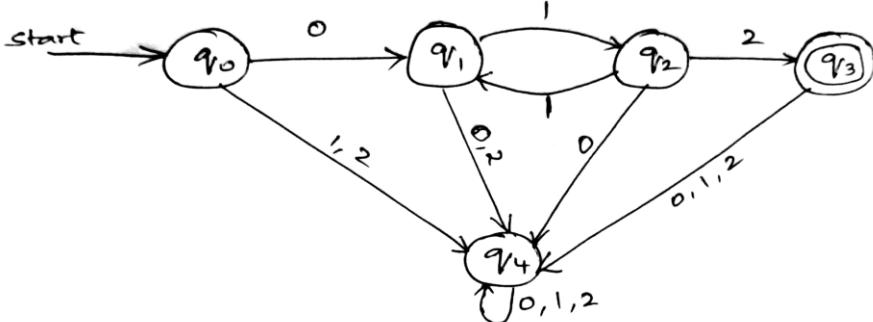
Course: Theoretical Foundations of Computations

Semester: IV

Duration: 3 hrs.

Max Marks: 100

Instructions: 1. Answer any FIVE full questions, choosing one full question from each unit.
2. Missing data, if any, may be suitably assumed.

| | | | UNIT - I | | |
|---|----|--|-----------|-----|-----------|
| | | | CO | PO | Marks |
| 1 | a) | Define Finite Automata. Demonstrate the same using an ON/OFF Switch. | 1 | 1 | 5 |
| | b) | Analyze the given DFA. Draw the transition table and write the language equivalent. Explain. | 1 | 2 | 7 |
| | c) |  <p>Obtain an ϵ-NFA which accepts strings consisting of zero or more a's followed by zero or more b's followed by zero or more c's.</p> | 1 | 3 | 8 |
| | | OR | | | |
| 2 | a) | Design DFA for accepting binary strings that i) start with 00 ii) having 001 iii) ending with 01 iv) not having 111 v) whose value is multiple of 2 | 3 | 3 | 10 |
| | b) | Design NFA for accepting strings that have 1 in second last position. Convert the same to DFA. | 1, 3 | 1,3 | 10 |
| | | | UNIT - II | | |
| | | | 1 | 1 | 6 |
| 3 | a) | List the notations used to represent regular expressions. Demonstrate the same with an example. | | | |

Important Note: Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.

| | b) | Analyze the given Finite Automata (FA) and obtain the corresponding regular expression. | 1 | 2 | 6 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|-------------------|-----|---|----------|---|---|-------------------|---|---|----------|---|---|-----------|---|---|----------|---|---|----------|---|---|----------|---|---|----------|---|---|----------|---|---|--|--|--|
| | i. | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | ii. | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | c) | Obtain an Non- Deterministic Finite Automata (NFA) for the regular expression $(a+b)^*aa(a+b)^*$. Show the step by step procedure involved in constructing the NFA. | 1 | 3 | 8 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | OR | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 4 | a) | Explain closure property – complementation with an example. | 1 | 1 | 6 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | b) | Write the regular expressions for the following. <ol style="list-style-type: none"> $L = \{w : n_a(w) \bmod 3 = 0 \text{ where } w = (a, b)^*\}$ $L = \{a^n b^m \mid m \geq 1, n \geq 1, nm \geq 3\}$ | 1 | 1 | 6 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | c) | Obtain the distinguishable table for the automaton and then minimize the states of the following DFA. | 1 | 3 | 8 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | <table border="1"> <thead> <tr> <th>δ</th><th>a</th><th>b</th></tr> </thead> <tbody> <tr> <td>\xrightarrow{A}</td><td>B</td><td>F</td></tr> <tr> <td>B</td><td>G</td><td>C</td></tr> <tr> <td>*C</td><td>A</td><td>C</td></tr> <tr> <td>D</td><td>C</td><td>G</td></tr> <tr> <td>E</td><td>H</td><td>F</td></tr> <tr> <td>F</td><td>C</td><td>G</td></tr> <tr> <td>G</td><td>G</td><td>E</td></tr> <tr> <td>H</td><td>G</td><td>C</td></tr> </tbody> </table> | δ | a | b | \xrightarrow{A} | B | F | B | G | C | *C | A | C | D | C | G | E | H | F | F | C | G | G | G | E | H | G | C | | | |
| δ | a | b | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| \xrightarrow{A} | B | F | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| B | G | C | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| *C | A | C | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| D | C | G | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| E | H | F | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| F | C | G | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| G | G | E | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| H | G | C | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | UNIT - III | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 5 | a) | Show that the below grammar is ambiguous. $S \rightarrow iCtS \mid iCtSeS \mid a, \quad C \rightarrow b$ | 1 | 1 | 4 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | b) | Consider the following context-free grammars. $G1: S \rightarrow aS \mid B, \quad B \rightarrow b \mid bB$ | 1 | 2 | 8 | | | | | | | | | | | | | | | | | | | | | | | | | | | |

| | | | | | |
|---|----|--|---|---|----|
| | | G2: $S \rightarrow aA \mid bB$, $A \rightarrow aA \mid B \mid \epsilon$, $B \rightarrow bB \mid \epsilon$ Write the Context free language generated by G1 and G2 | | | |
| | c) | Analyze the given language and obtain a grammar to generate the following languages: i. $L = \{a^{n+2}b^m \mid n \geq 0 \text{ and } m > n\}$ ii. $L = \{a^n b^m c^k \mid n \geq 0 \text{ and } m > n\}$ | 2 | 2 | 8 |
| | | OR | | | |
| 6 | a) | Eliminate useless symbols in the grammar given below: $\{S \rightarrow aA \mid bB, A \rightarrow aA \mid a, B \rightarrow bB, D \rightarrow ab \mid Ea, E \rightarrow aC \mid d\}$ | 3 | 1 | 10 |
| | c) | Consider the grammar. $S \rightarrow 0A \mid 1B$ $A \rightarrow 0AA \mid 1S \mid 1$ $B \rightarrow 1BB \mid 0S \mid 0$ Obtain the grammar in Chomsky Normal Form (CNF). | 1 | 3 | 10 |
| | | UNIT - IV | | | |
| 7 | a) | State the pumping lemma for Context Free languages. Explain with an example. | 2 | 2 | 5 |
| | b) | Check if the Push Down Automata (PDA) to accept the language $L(M) = \{w \mid w (a+b)^*\}$ and $n_a(w) = n_b(w)$ is deterministic or non-deterministic? | 3 | 3 | 5 |
| | c) | For the given grammar, obtain the corresponding PDA. $S \rightarrow aABB \mid aAA$ $A \rightarrow aBB \mid a$ $B \rightarrow bBB \mid A$ $C \rightarrow a$ | 1 | 1 | 10 |
| | | OR | | | |
| 8 | a) | Design PDA for accepting $a^n b^{2n}$ such that $n \geq 1$. | 3 | 3 | 10 |
| | b) | Design PDA to accept $a^n b^n$. Also check whether the PDA is DPDA or NPDA. | 3 | 3 | 10 |
| | | UNIT - V | | | |
| 9 | a) | Discuss about the various components of Turing machine model. | 3 | 3 | 5 |
| | b) | Find whether the lists given here have a Post Correspondence Solution. $M = (abb, aa, aaa)$ and $N = (bba, aaa, aa)$ | 3 | 3 | 5 |
| | c) | Design a Turing machine to accept the language $L(M) = \{0^n 1^n 2^n \mid n \geq 1\}$ | 3 | 3 | 10 |
| | | OR | | | |

| | | | | | | |
|--|----|----|---|---|---|-----------|
| | 10 | a) | Design TM that adds two numbers. Assume numbers are stored on tape as sequence of 1's and separated by a 0. | 3 | 3 | 10 |
| | | b) | Design TM that accepts palindrome strings of a and b. | 3 | 3 | 10 |

B.M.S.C.E. - ODD SEM 2024-25