

U.S.N.

B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

August 2024 Semester End Main Examinations

Programme: B.E.

Branch: Computer Science and Engineering

Course Code: 23CS4PCTFC

Course: Theoretical Foundations of Computations

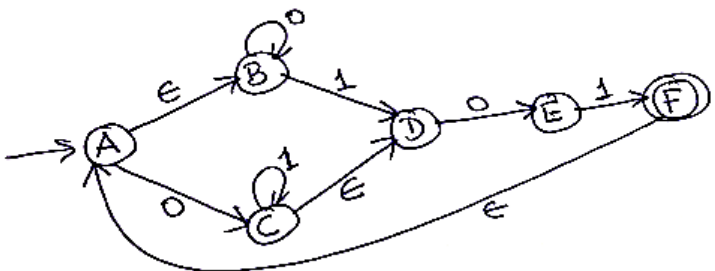
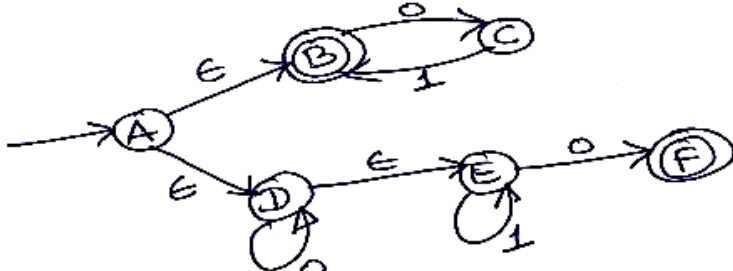
Semester: IV

Duration: 3 hrs.

Max Marks: 100

Instructions: 1. Answer any FIVE full questions, choosing one full question from each unit.
2. Missing data, if any, may be suitably assumed.

| Important Note: Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice. | | | UNIT - I | CO | PO | Marks |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---|----|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----|-----|-------|
| | 1 | a) | Define Deterministic Finite Automata (DFA). Construct the DFA to accept the language $L = \{w \mid w \in \{a, b\}^* \text{ and } w \text{ ends with } abb\}$. Show the DFA transition function movements for the string abaabb | CO3 | PO3 | 10 |
| | | b) | For the Non-deterministic Finite Automata (NFA) shown below, using the subset construction method to find the equivalent DFA. | CO3 | PO3 | 10 |
| | | | | | | |
| | | | OR | | | |
| | 2 | a) | Define NFA. Construct the NFA to accept the language $L = \{w \mid w \in \{a, b\}^* \text{ and } w \text{ has exactly two } a\text{'s}\}$. Show the NFA transition function movements for the string babbab | CO3 | PO3 | 6 |
| | | b) | Define ϵ -closure (A), where A is any state of the given ϵ -NFA (Epsilon NFA). Compute the ϵ -closure of the states $\{A, B, C, F\}$ from the following ϵ -NFA. | CO1 | PO1 | 4 |

| | | | | | |
|---|----|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----|-----|----|
| | |  | | | |
| | c) | Convert following ϵ -NFA (Epsilon NFA) to DFA using Epsilon (ϵ) closure. | CO3 | PO3 | 10 |
| | |  | | | |
| | | UNIT - II | | | |
| 3 | a) | Design Regular Expressions (RE) which generates the following languages over the alphabet set $\Sigma = \{0, 1\}$. i. Set of all strings ending with 1 and not containing 00. ii. Set of all strings that do not contain the substring 01. | CO3 | PO3 | 6 |
| | b) | Show that the regular languages are closed under Difference and Intersection operation. | CO2 | PO2 | 6 |
| | c) | State pumping lemma for regular languages. Use pumping lemma to show that the following language is not regular. $L = \{xx^R \mid x \in (0, 1)^*\}$. | CO2 | PO2 | 8 |
| | | UNIT - III | | | |
| 4 | a) | Design Context Free Grammar (CFG) to generate each of the following languages. i. $L = \{a^i b^j c^k \mid j = i + k\}$ ii. $L = \{a^i b^j c^k \mid j = i \text{ or } j = k\}$ | CO2 | PO2 | 6 |
| | b) | Let G be the CFG with productions set as $\{S \rightarrow S+S \mid S-S \mid S^*S \mid S/S \mid (S) \mid a\}$. Answer the following w.r.t $a+(a^*a)/a-a$. i. Give two left most derivations. ii. Draw the derivation tree corresponds to each of the derivations in (i). iii. How many distinct leftmost derivations are there? | CO3 | PO3 | 6 |

| | | | | | |
|---|----|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----|-----|----|
| | c) | Convert following CFG to Greibach Normal Form (GNF). $S \rightarrow AaA \mid CA \mid BaB$ $A \rightarrow aaBa \mid CDA \mid aa \mid DC$ $B \rightarrow bB \mid bAB \mid bb \mid aS$ $C \rightarrow Ca \mid bC \mid D$ $D \rightarrow bD \mid \epsilon$ | C02 | P02 | 8 |
| | | OR | | | |
| 5 | a) | Write CFG to generate each of the following languages. i. $L = \{a^i b^j c^k \mid i < j\}$ ii. $L = \{a^i b^j c^k \mid j < k\}$ | C02 | P02 | 6 |
| | b) | Answer the following i. Identify the language generated by the CFG with productions $S \rightarrow aSaSbS \mid aSbSaS \mid bSaSaS \mid \epsilon$ ii. Show that the CFG with productions $S \rightarrow aSb \mid aaSb \mid \epsilon$ is ambiguous. | C02 | P02 | 6 |
| | c) | Define Chomsky Normal Form (CNF). Convert following Grammar to CNF. $S \rightarrow ABA$, $A \rightarrow aA \mid \epsilon$, $B \rightarrow bB \mid \epsilon$ | C03 | P03 | 8 |
| | | UNIT – IV | | | |
| 6 | a) | Define Push Down Automata (PDA). Construct Nondeterministic Push Down Automata (NPDA) for the language $L = \{w \mid w \in (a,b)^* \text{ and } w \text{ is palindrome of even length}\}$ by final state method. Show the Instantaneous Description (ID) for the string abaaba is accepted by the NPDA constructed. | C03 | P03 | 8 |
| | b) | Convert following Grammar to PDA. Show the instantaneous description for the string "aabba" $S \rightarrow aABC$ $A \rightarrow aB \mid a$ $B \rightarrow bA \mid b$ $C \rightarrow a$ | C02 | P02 | 6 |
| | c) | State pumping lemma for Context Free Languages (CFL). Apply pumping lemma to show the language $L = \{a^i b^j c^k \mid i < j < k\}$ is not a context free language. | C02 | P02 | 6 |
| | | UNIT - V | | | |
| 7 | a) | Design the Turing Machine (TM) which accepts the set of all palindromes over the alphabet set $\Sigma = \{0, 1\}$. Trace the operation of the constructed TM on the string 100001 | C03 | P03 | 10 |
| | b) | Define Post Correspondence Problem (PCP). Find a Post Correspondence Solution for following two lists given. | C03 | P03 | 6 |

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|--|--|----|------------------------------------|---|----------------|----------------|--|------------|------------|----------|
| | | | | | List X | List Y | | | | |
| | | | | i | X _i | Y _i | | | | |
| | | | | 1 | 10 | 101 | | | | |
| | | | | 2 | 01 | 100 | | | | |
| | | | | 3 | 0 | 10 | | | | |
| | | | | 4 | 100 | 0 | | | | |
| | | | | 5 | 1 | 010 | | | | |
| | | c) | Describe Multitape Turing Machine. | | | | | <i>COI</i> | <i>POI</i> | 4 |

B.M.S.C.E. - EVEN SEM 2023-24