

U.S.N.

B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

October 2024 Supplementary Examinations

Programme: B.E.

Branch: Computer Science and Engineering

Course Code: 23CS4PCTFC

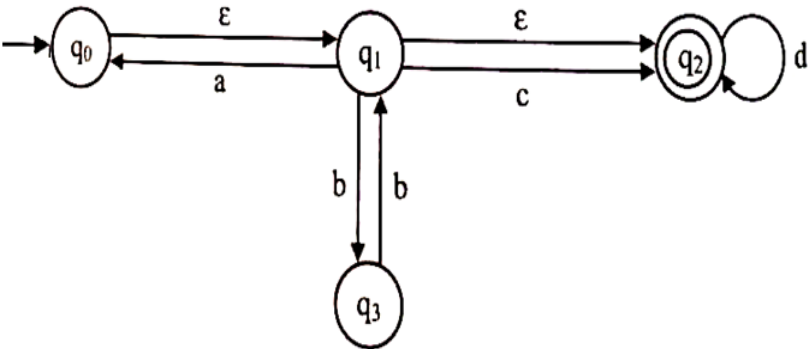
Course: Theoretical Foundations of Computations

Semester: IV

Duration: 3 hrs.

Max Marks: 100

Instructions: 1. Answer any FIVE full questions, choosing one full question from each unit.
2. Missing data, if any, may be suitably assumed.

Important Note: Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.			UNIT - I	CO	PO	Marks
	1	a)	(i) Design Deterministic Finite Automata (DFA) which accepts set of strings such that every string containing 00 as a substring but not 000 as substring. Consider alphabet set as $\Sigma = \{0, 1\}$. (ii) Design NFA for the language $L = \{ \text{all strings over } (0,1)^* \text{ that have at least two consecutive 0's or two consecutive 1's} \}$	CO1	PO1	5
		b)	Convert the following Non-Deterministic Finite Automata (NFA) with Epsilon (ϵ)-transitions to equivalent NFA without Epsilon - transitions by giving the epsilon closure of all the states. 	CO1	PO1	8
		c)	Construct NFA which accepts set of all strings whose second last symbol is 1. Convert this NFA to DFA using Subset Construction Method. Consider alphabet set as $\Sigma = \{0, 1\}$.	CO1	PO1	7
			OR			
	2	a)	(i) Design DFA to accept strings of a's and b's ending with ab or ba (ii) Design a DFA to accept the language $L = \{ w \mid \text{number of a's in } (w) \geq 1, \text{ number of b's in } (w) \geq 2 \}$	CO1	PO1	5

	b)	Convert the following NFA to DFA using Subset Construction Method.	CO 1	PO 1	8																				
		<table><tr><td>δ</td><td>0</td><td>1</td></tr><tr><td>$\rightarrow Q0$</td><td>Q0, Q1</td><td>Q1</td></tr><tr><td>* Q1</td><td>Q2</td><td>Q2</td></tr><tr><td>Q2</td><td>\emptyset</td><td>Q2</td></tr></table>	δ	0	1	$\rightarrow Q0$	Q0, Q1	Q1	* Q1	Q2	Q2	Q2	\emptyset	Q2											
δ	0	1																							
$\rightarrow Q0$	Q0, Q1	Q1																							
* Q1	Q2	Q2																							
Q2	\emptyset	Q2																							
	c)	Convert the following ε -NFA to DFA.	CO 1	PO 1	7																				
		<table><tr><td>δ</td><td>ε</td><td>a</td><td>b</td><td>c</td></tr><tr><td>$\rightarrow P$</td><td>\emptyset</td><td>P</td><td>Q</td><td>R</td></tr><tr><td>Q</td><td>P</td><td>Q</td><td>R</td><td>\emptyset</td></tr><tr><td>* R</td><td>Q</td><td>R</td><td>\emptyset</td><td>P</td></tr></table>	δ	ε	a	b	c	$\rightarrow P$	\emptyset	P	Q	R	Q	P	Q	R	\emptyset	* R	Q	R	\emptyset	P			
δ	ε	a	b	c																					
$\rightarrow P$	\emptyset	P	Q	R																					
Q	P	Q	R	\emptyset																					
* R	Q	R	\emptyset	P																					
		UNIT-II																							
3	a)	Construct the minimum state automata for the finite automata given below. Consider alphabet set as $\Sigma = \{0, 1\}$.	CO 2	PO 2	10																				
	b)	Convert the DFA which accepts Even number of 1's to Regular Expression (RE) by eliminating intermediate states method. Consider alphabet set as $\Sigma = \{0, 1\}$.	CO 2	PO 2	10																				
		UNIT - III																							
4	a)	Convert the following Grammar to Chomsky Normal Form (CNF) $S \rightarrow abAB$, $A \rightarrow Bab \mid \varepsilon$, $B \rightarrow Baa \mid A \mid \varepsilon$	CO 2	PO 2	10																				
	b)	Design a Context Free Grammar (CFG) for $L = \{ a^n c^m b^k \mid n=m \text{ or } m \leq k, \text{ for } n, m, k \geq 0 \}$. Write formal definition of the obtained CFG.	CO 2	PO 2	10																				

		OR			
5	a)	Convert the following Grammar to Chomsky Normal Form (CNF) $S \rightarrow AB \mid aB$, $A \rightarrow aab \mid \varepsilon$, $B \rightarrow bbA$	CO 2	PO 2	10
	b)	Design a CFG for the language that generates the set of (i) All strings with exactly one a (ii) All strings with at least one a (iii) All strings with at least three a's Consider alphabet set as $\Sigma = \{a, b\}$.	CO 2	PO 2	10
		UNIT - IV			
6	a)	i. Construct a Non-Deterministic Push Down Automata (NPDA) for accepting all palindromes over the alphabet set $\Sigma = \{a, b\}$ ii. Design Deterministic Push Down Automata (DPDA) for the language $L = \{a^n b^{2n} \mid n \geq 1\}$	CO 3	PO 3	8
	b)	Construct PDA that accepts the language generated by the grammar $S \rightarrow aSbb \mid abb$	CO 3	PO 3	6
	c)	Prove that the language $L = \{a^n b^n c^n, n \geq 1\}$ is not Context Free Language (CFL)	CO 3	PO 3	6
		UNIT - V			
7	a)	Design a Turing Machine (TM) for set of string with equal number of 0's and 1's over $\{0, 1\}^*$	CO 3	PO 3	10
	b)	Determine whether the following (A, B) pairs have a Post Correspondence solution or not, if Yes give solution, if No why, Justify. (i) $A = \{b, babb, ba\}$ $B = \{bb, ba, ba\}$ (ii) $A = \{1^2, 10^2, 1^3\}$ $B = \{1^3, 0^2 1, 1^2\}$	CO 3	PO 3	10
