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# B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

## June / July 2025 Semester End Main Examinations

**Programme: B.E.**

**Semester: III**

**Branch: Electrical and Electronics Engineering**

**Duration: 3 hrs.**

**Course Code: 23EE3ESEFT/19ES3GCFTH/22EE3PCFTH**

**Max Marks: 100**

**Course: Electromagnetic Field Theory/ Field Theory**

**Instructions:** 1. Answer any FIVE full questions, choosing one full question from each unit.  
2. Missing data, if any, may be suitably assumed.

<b>UNIT - I</b>			<i>CO</i>	<i>PO</i>	<b>Marks</b>
1	a)	Derive an expression for electric field intensity at any point due to an infinite line charge.	<i>CO1</i>	<i>PO1</i>	<b>08</b>
	b)	For the point C (4.4, -115°, 2) in cylindrical coordinate system, find the rectangular and spherical coordinates.	<i>CO1</i>	<i>PO2</i>	<b>04</b>
	c)	Given $\mathbf{D} = 5 r \sin^2\theta \cos^2\phi \mathbf{a}_r$ C/m <sup>2</sup> . Evaluate both sides of Gauss Divergence theorem for the region, $r < 2$ .	<i>CO2</i>	<i>PO2</i>	<b>08</b>
<b>OR</b>					
2	a)	State and explain Coulomb's law of force between two-point charges. Also, determine the vector force exerted on charge $Q_A$ by $Q_B$ , if $Q_A = -20\mu\text{C}$ is located at A (-6, 4, 7) and $Q_B = 50\mu\text{C}$ is located at B (5, 8, -2).	<i>CO2</i>	<i>PO2</i>	<b>08</b>
	b)	Find the total charge contained in a 2 cm length of the electron beam for $2 \text{ cm} < z < 4 \text{ cm}$ , $\rho = 1 \text{ cm}$ and $\rho_v = -5e^{-10^5\rho z} \mu\text{C/m}^3$ .	<i>CO2</i>	<i>PO2</i>	<b>06</b>
	c)	In a certain region of space $\mathbf{D} = 8xyz^4 \mathbf{a}_x + 4x^2z^4 \mathbf{a}_y + 16x^2yz^3 \mathbf{a}_z$ . Find the total electric flux passing through the rectangular surface, $z=2$ , $0 < x < 2$ , $1 < y < 3$ in $\mathbf{a}_z$ direction.	<i>CO2</i>	<i>PO2</i>	<b>06</b>
<b>UNIT - II</b>					
3	a)	Derive the expression of convection current density by considering the movement of a charge element.	<i>CO2</i>	<i>PO2</i>	<b>05</b>
	b)	If we take the zero reference for potential at infinity, find the potential at (0, 0, 2) in free-space, caused by (i) 12 nC/m on the line $\rho = 2.5$ , $z = 0$ (ii) point charge of 18 nC at (1, 2, -1).	<i>CO2</i>	<i>PO2</i>	<b>08</b>
	c)	Evaluate the boundary conditions related to electric field at the interface of a conductor and free-space.	<i>CO3</i>	<i>PO3</i>	<b>07</b>
<b>OR</b>					

**Important Note:** Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.

	4	a)	Given $\mathbf{E} = y \mathbf{a}_x + x \mathbf{a}_y + 2 \mathbf{a}_z$ V/m, determine the work done in carrying a 2C of charge from B (1,0,1) to A (0.8, 0.6, 1) along the shorter arc of the circle, $x^2 + y^2 = 1$ , $z = 1$ .	CO2	PO3	<b>07</b>
		b)	Obtain the expression for potential energy in a system of 'N' charges.	CO1	PO2	<b>07</b>
		c)	The current density is given in cylindrical co-ordinates as; $\mathbf{J} = -10^6 z^{1.5} \mathbf{a}_z$ in the region $0 \leq \rho \leq 20 \mu\text{m}$ , and $\mathbf{J} = 0$ , elsewhere. (i) Find the total current crossing the surface $z = 0.1\text{m}$ in the $\mathbf{a}_z$ direction. (ii) If the velocity is $2 \times 10^6 \text{ m/s}$ at $z = 0.1 \text{ m}$ , find the $\rho_v$ there.	CO3	PO3	<b>06</b>
	<b>UNIT - III</b>					
5	a)	Derive the boundary conditions on $\mathbf{D}$ and $\mathbf{E}$ at the interface of the perfect dielectrics.	CO2	PO2	<b>07</b>	
	b)	Given the potential field $V = [A \rho^4 + B \rho^4] \sin 4\phi$ volts, show that $\nabla^2 V = 0$ . Also, determine the values of A and B, so that $V = 100$ volts and $ \mathbf{E}  = 500 \text{ V/m}$ at P ( $\rho = 1, \phi = 22.5^\circ, z = 2$ ).	CO2	PO2	<b>07</b>	
	c)	Derive the expression of capacitance of a coaxial capacitor having inner radius a, outer radius b and the length L.	CO3	PO3	<b>06</b>	
	<b>OR</b>					
6	a)	Calculate numerical values for V and $\rho_v$ at point P in free-space, if $V = 5\rho^2 \cos(2\phi)$ , at P ( $\rho = 3, \phi = \frac{\pi}{3}, z = 2$ ).	CO2	PO2	<b>06</b>	
	b)	Solve the Laplace's equation for the potential field in the homogeneous region between the two concentric conducting spheres with radii a and b ( $b > a$ ), if potential $V = 0$ at $r = b$ and $V = V_0$ at $r = a$ . And find the capacitance between the two concentric spheres.	CO3	PO2	<b>08</b>	
	c)	Let the region $z < 0$ be composed of a uniform dielectric material for which $\epsilon_r = 3.2$ , while the region $z > 0$ is characterized by $\epsilon_r = 2$ . Let $\mathbf{D}_1 = -30 \mathbf{a}_x + 50 \mathbf{a}_y + 70 \mathbf{a}_z \text{ nC/m}^2$ . Find (i) $\mathbf{D}_{N1}$ (ii) $\mathbf{D}_{t1}$ (iii) $\theta_1$ (iv) $\mathbf{D}_{N2}$ .	CO3	PO3	<b>06</b>	
	<b>UNIT - IV</b>					
7	a)	Given the points $P_1(1, 2, 3)$ and $P_2(-3, -1, 2)$ , calculate $\Delta \mathbf{H}_2$ , if incremental current element, $I_1 \Delta \mathbf{L}_1 = 2\pi(-\mathbf{a}_x + \mathbf{a}_y + 2\mathbf{a}_z) \mu\text{A}\cdot\text{m}$ .	CO2	PO2	<b>05</b>	
	b)	State and explain Ampere's circuital law. Using the same, derive the expression for magnetic field intensity at any point due to an infinite length filamentary current carrying conductor present on z-axis.	CO3	PO3	<b>07</b>	
	c)	Evaluate the boundary conditions at the interface of two magnetic media.	CO1	PO1	<b>08</b>	
	<b>OR</b>					

	8	a)	Consider a rectangular path $P_1(2, 3, 4)$ to $P_2(4, 3, 4)$ to $P_3(4, 3, 1)$ to $P_4(2, 3, 1)$ to $P_1$ . (i) Evaluate the closed line integral of $\mathbf{H}$ about this path, given that $\mathbf{H} = 3z \mathbf{a}_x - 2x^3 \mathbf{a}_z$ A/m. (ii) Determine the quotient of the closed line integral and the area enclosed by the path as an approximation to $(\nabla \times \mathbf{H})_y$ .	CO3	PO3	<b>06</b>
		b)	Two differential current elements, $I_1\Delta L_1 = 3 \times 10^{-6} \mathbf{a}_y$ A-m at $P_1(1, 0, 0)$ and $I_2\Delta L_2 = 3 \times 10^{-6}(-0.5\mathbf{a}_x + 0.4\mathbf{a}_y + 0.3\mathbf{a}_z)$ A-m at $P_2(2, 2, 2)$ are located in free-space. Find the vector force exerted on $I_1\Delta L_1$ by $I_2\Delta L_2$ .	CO3	PO3	<b>06</b>
		c)	Write an explanatory note on scalar and vector magnetic potentials.	CO2	PO2	<b>08</b>
<b>UNIT - V</b>						
	9	a)	Starting from the equation of Faraday's law, obtain the point form of Maxwell's equation concerning spatial derivative of $\mathbf{E}$ and time derivative of $\mathbf{H}$ .	CO3	PO3	<b>05</b>
		b)	Derive the wave equations that characterize the propagation of uniform plane wave in free-space.	CO2	PO2	<b>07</b>
		c)	Starting from Maxwell's equation involving curl on $\mathbf{H}$ , obtain the equation of Poynting's theorem and interpret the same.	CO2	PO2	<b>08</b>
<b>OR</b>						
	10	a)	Given $B_x = 2 \times 10^{-4} \cos(10^5 t) \sin(10^{-3} y)$ T, $\epsilon = 10^{-11}$ F/m and $\mu = 10^{-5}$ H/m within a certain region; (i) Find $\mathbf{E}$ (ii) Find the total magnetic flux passing through the surface $x=0, 0 < y < 40$ m, $0 < z < 2$ m at $t=1\mu$ s.	CO3	PO3	<b>07</b>
		b)	Explain the inadequacy of Ampere's circuital law for time-varying fields. Obtain a suitable correction for the same, which will remain consistent for both time and non-time-varying fields.	CO2	PO2	<b>06</b>
		c)	Given a non-magnetic material having $\epsilon_r' = 3.2$ and $\sigma = 1.5 \times 10^{-4}$ S/m, find the following in free-space, (i) Loss tangent (ii) Attenuation constant (iii) Phase constant (iv) Intrinsic impedance. Consider $f = 3$ MHz.	CO3	PO3	<b>07</b>

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