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# B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

## May 2023 Semester End Main Examinations

**Programme: B.E.**

**Branch: Electronics and Communication Engineering**

**Course Code: 22EC3PCSAS**

**Course: Signals and Systems**

**Semester: III**

**Duration: 3 hrs.**

**Max Marks: 100**

**Date: 12.05.2023**

**Instructions:** 1. Answer any FIVE full questions, choosing one full question from each unit.  
2. Missing data, if any, may be suitably assumed.

### UNIT - I

1 a) Determine whether the following signal are periodic or not. If periodic find the period. **05**

(i)  $x(t) = 3\cos(250\pi t) + 5\sin(200\pi t)$       (ii)  $x[n] = e^{j(\frac{\pi}{4})n}$

b) Evaluate the following expressions **05**

(i)  $\sum_{n=-\infty}^{\infty} e^{2n} \delta(n-2)$       (ii)  $\sum_{n=-5}^{5} (\sin 2n) \delta(n+7)$

c) A signal  $y(t)$  is defined below. Sketch the signal and Perform the following operations  
(i)  $x(2t)$  (ii)  $x(2t+3)$  (iii)  $x(1-2t)$  (iv)  $x(-t-1)$   
if  $x(t) = \begin{cases} (t+1); & -1 \leq t \leq 0 \\ (-t+1); & 0 \leq t \leq 1 \end{cases}$  **10**

### UNIT - II

2 a) A system is defined as below **10**  
 $y(t) = x^2(-t)$   
 Check the system for following properties. Also show the mathematics behind all the properties.  
 (i) linearity (ii) memory (iii) causality (iv) time invariance (v) stability

b) A system is defined as below **10**  
 $y[n] = \sum_{k=n_0}^n x[k]$   
 Check the system for following properties. Also show the mathematics behind all the properties.  
 (i) linearity (ii) memory (iii) causality (iv) time invariance (v) stability

**Important Note:** Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.

### UNIT - III

3 a) The input  $x(t)$  and impulse response  $h(t)$  of a LTI system are given below. 10  
 $x(t) = 2u(t-1) - 2u(t-3)$  And  $h(t) = u(t+1) - 2u(t-1) + u(t+3)$

Sketch  $x(t)$  and  $h(t)$ . Find the output of the system and sketch the output.

b) An impulse response is given by 06

$$h[n] = \left(\frac{1}{2}\right)^n u(n+3). \text{ Test the following properties}$$

(i) Memory (ii) causality (iii) stability

c) Draw the direct form 2 structure for the following system 04

$$y(t) = x(t) + 2\frac{d}{dt}x(t) + 3\frac{d^2}{dt^2}x(t) - 4\frac{d}{dt}y(t) + 5\frac{d^2}{dt^2}y(t)$$

### OR

4 a) The input  $x(t)$  and impulse response  $h(t)$  of a LTI system are given below. 10  
 $x(t) = u(t+1) - u(t-1)$  And  $h(t) = 2x(t)$

Sketch  $x(t)$  and  $h(t)$ . Find the output of the system and sketch the output.

b) Let  $h_1(t), h_2(t), h_3(t), h_4(t)$  be impulse response of LTI systems. Construct a system with impulse response  $h(t)$  using  $h_1(t), h_2(t), h_3(t), h_4(t)$  as subsystems. Draw the interconnection of the systems to obtain

$$(i) h(t) = h_1(t) + \{h_2(t) * h_3(t)\} + h_4(t)$$

$$(ii) h(t) = h_1(t) * \{h_2(t) + h_3(t)\} * h_4(t)$$

c) Draw the direct form 2 structure for the following system. 04

$$\frac{d^2}{dt^2}y(t) + 3\frac{d}{dt}y(t) + 5y(t) = \frac{d}{dt}x(t) + 4x(t)$$

### UNIT - IV

5 a) Find the DTFT of following signals 08

$$(i) x[n] = (0.5)^{n+2}u[n]$$

$$(ii) x[n] = n(0.5)^{2n}u[n]$$

b) State and prove frequency shift property of DTFT. 06

c) Find the frequency response of  $h[n] = \left(\frac{1}{2}\right)^n u(n)$  06

### OR

6 a) State and prove time shift property of DTFS. 06

b) Determine the Fourier series coefficients for the signal below. 08

$$x[n] = 1 + \sin \Omega_0 n + 3 \cos \Omega_0 n + \cos(2\Omega_0 n + \frac{\pi}{2})$$

c) Find the system transfer function for the following difference equation using DTFT 06

$$y[n] - \frac{1}{2}y[n-1] = x[n]$$

Hence find the impulse response of the system.

**UNIT - V**

7 a) Find the Z transform of the signal and plot the ROC. 07

$$x[n] = \left(\frac{1}{4}\right)^n u(n) + \left(\frac{1}{2}\right)^n u(n)$$

b) Solve the following difference equation using Z transform 07

$$y[n] - 0.8y[n-1] = x[n]$$

where, input,  $x[n] = (0.5)^n u[n]$ , and,  $y[-1] = 2$

c) Discuss the properties of ROC with an example each. 06

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