

# B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

## December 2023 Supplementary Examinations

Programme: B.E.

Branch: Electronics and Communication Engineering

Course Code: 22EC3PCSAS

Course: Signals and Systems

Semester: III

Duration: 3 hrs.

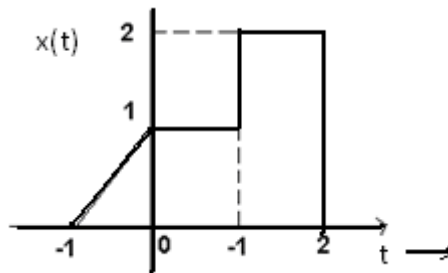
Max Marks: 100

**Instructions:** 1. Answer any FIVE full questions, choosing one full question from each unit.  
2. Missing data, if any, may be suitably assumed.

### UNIT - I

- 1 a) Given  $x(t)$  as shown in figure 1(b), Sketch the following 10

- i)  $x(2t-1)$
- ii)  $x(4-t)$
- iii)  $x(t)u(t)$
- iv)  $x(-t/2)$
- v)  $x(t)+x(-t)$



- b) Identify whether the signal is periodic or non-periodic, if periodic find the fundamental period 06

- i)  $x(n) = \cos\left(\frac{n\pi}{12}\right) + \sin\left(\frac{n\pi}{18}\right)$
- ii)  $x(n) = \cos\left(\frac{4n\pi}{13} + \pi\right)$

- c) Plot the signal 04

$$x(t) = u(t+2) + r(t+1) - r(t) - u(t-2) - u(t-4)$$

### UNIT - II

- 2 a) For the following systems determine whether the system is Linear, Causal, Stable, Time-invariant and Memory less 10

i)  $y(n) = ax[n] + b$

ii)  $y(t) = e^{x(t)}$

- b) A system consists of several subsystems connected as shown in figure 2(b). Find the operator  $H$  relating  $x(t)$  to  $y(t)$  for the subsystem operators given by; 06

$$H_1: y_1(t) = x_1(t)x_1(t-1)$$

$$H_2: y_2(t) = |x_2(t)|$$

$$H_3: y_3(t) = 1 + 2x_3(t)$$

$$H_4: y_4(t) = \cos(x_4(t))$$

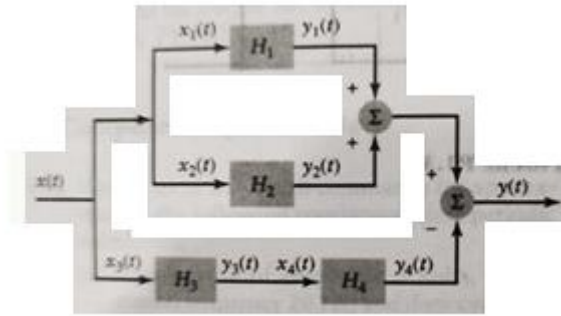


Figure 2(b)

- c) Derive the condition for stability of an LTI discrete system. **04**

### UNIT - III

- 3 a) Determine output  $y(t)$  for an input  $x(t) = e^{-3t} u(t)$  and unit impulse response  $h(t) = u(t-2)$  using convolution integral. **06**
- b) An LTI system is characterized by  $h[n] = (1/4)^n u[n]$ . compute the output of the system at time  $n=0, 5 \& 10$ , when input is  $x[n] = u[n]$  **08**
- c) Consider two systems having impulse responses  $h_1(t) = e^{-3t} u(t)$  and  $h_2(t) = 2e^{-t} u(t)$  find the overall impulse responses when the systems are connected in i) Parallel and ii) series **06**

OR

- 4 a) For each impulse responses listed below. Determine whether the systems are memoryless, Causal and stable. **08**
- (i)  $h(t) = e^{-2|t|}$
- (ii)  $h(n) = \left(\frac{1}{3}\right)^n u(n+1)$
- b) Find the natural response of the system described by  $y(n) + 3y(n-1) + 2y(n-2) = 2x(n) + 3x(n-1)$  with initial conditions  $y(-1) = 7$  and  $y(-2) = -3$  **08**
- c) Represent following difference equation in Direct form-I and Direct form-II block diagram representation. **04**

$$\frac{d^2 y(t)}{dt^2} + 2 \frac{dy(t)}{dt} - \frac{dx(t)}{dt} = y(t)$$

### UNIT - IV

- 5 a) The unit impulse response of an LTI system is  $h[n] = \alpha^n u[n]$ . Find the response of the system using DTFT to an input defined by  $x[n] = \beta^n u[n]$ , where  $\alpha, \beta < 1$  and  $\alpha \neq \beta$  **10**
- b) Find the DTFS representation of the given waveform shown in fig 5(b). **10**

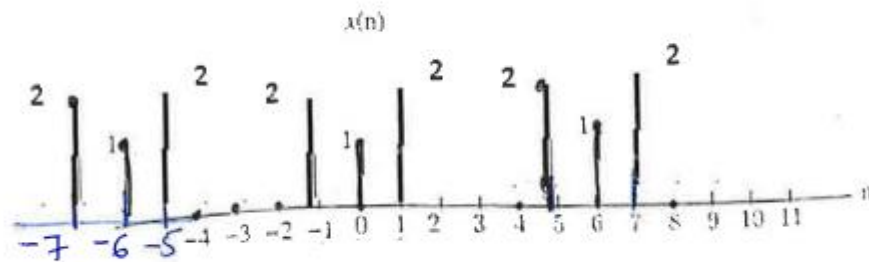


Figure 5(b)

**OR**

- 6 a) Find the DTFT for the following signal  $x(n)$  and draw its spectrum  $X(n)=a^n u(n)$  ; magnitude of  $a < 1$ . **08**
- b) Evaluate the DTFS representation for the signals **08**
- i)  $x(n) = \cos[(\pi/8)n]$
- ii)  $x(n) = \cos[(\pi/3)n] + \cos[(\pi/4)n]$
- c) State and describe sampling theorem. **04**

#### UNIT - V

- 7 a) Solve the given difference equation using Unilateral Z transform for the given initial conditions  $y[-1] = 2$  and input  $x[n] = u[n]$ . **06**  
 $y(n) - 0.1 y(n-1) = x(n)$
- b) Find the Z-transform of the following sequences and find the ROC **08**

i)  $x[n] = \left[ \frac{1}{2} \right]^n \sin \Omega_0 n u[n]$

ii)  $x[n] = \left( \frac{1}{2} \right)^n \{u[n] - u[n-10]\}$

- c) A causal system is represented by the following difference equation **06**  
 $y[n] - 0.25y(n-2) = x(n) - 0.5x(n-1)$
- a. Determine the system function  $H(z)$  and the corresponding ROC
- b. Determine the impulse response of the system in analytical form

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