

U.S.N.

**B.M.S. College of Engineering, Bengaluru-560019**

Autonomous Institute Affiliated to VTU

**June 2025 Semester End Main Examinations****Programme: B.E.****Semester: IV****Branch: Electronics and Communication Engineering****Duration: 3 hrs.****Course Code: 23EC4PCFAW / 22EC4PCFAW****Max Marks: 100****Course: Fields and Waves**

- Instructions:** 1. Answer any FIVE full questions, choosing one full question from each unit.  
 2. Missing data, if any, may be suitably assumed.  
 3. Quantities indicated in bold represent vectors.

Important Note: Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.			<b>UNIT - I</b>	<b>CO</b>	<b>PO</b>	<b>Marks</b>
	1	a)	Obtain the relationship between electric flux density and electric field intensity.	1	1	<b>05</b>
		b)	State and illustrate Gauss' law.	-	-	<b>05</b>
		c)	Given the field $\mathbf{D} = 6\rho \sin(\phi/2) \mathbf{a}_\rho + 1.5\rho \cos(\phi/2) \mathbf{a}_\phi \text{ C/m}^2$ , evaluate both sides of divergence theorem for the region bounded by $\rho=2$ , $0 \leq \phi \leq \pi$ , $0 \leq z \leq 5$ .	1	1	<b>10</b>
			<b>OR</b>			
	2	a)	Derive an expression for electric field intensity at any point due to an infinite sheet of charge.	1	1	<b>06</b>
		b)	Two uniform line charges of density $4\text{nC/m}$ and $6\text{nC/m}$ lie in $x=0$ plane at $y = 5$ and $-6$ respectively, in free space. Find $\mathbf{E}$ at $(4,0, 3)$ .	1	1	<b>07</b>
		c)	An electric field is expressed as $\mathbf{E} = 6x^2 \mathbf{a}_x + 6y \mathbf{a}_y + 4 \mathbf{a}_z \text{ V/m}$ . Find: (i) $V_{MN}$ , if points M and N are specified by M $(2, 6, -1)$ and N $(-3, -3, 2)$ . (ii) $V_M$ , if Q $(4, -2, -35)$ is the zero-potential point.	1	1	<b>07</b>
			<b>UNIT - II</b>			
	3	a)	From the law of conservation of charge, it can be said that current is continuous from one side of a reference surface to the other. Considering a suitable reference surface, obtain the current continuity equation.	1	1	<b>07</b>
		b)	Evaluate the boundary conditions related to electric field at the interface of a conductor and free-space.	2	2	<b>07</b>
		c)	Derive the expression of capacitance of a coaxial capacitor having inner radius $a$ , outer radius $b$ and the length $L$ .	1	1	<b>06</b>

		<b>OR</b>			
4	a)	Given $\mathbf{J} = 10 \rho^2 z \mathbf{a}_\rho - 4\rho \cos^2\phi \mathbf{a}_\phi$ mA/m <sup>2</sup> , find current density at P (3, 30°, 2) and also determine current flowing outward through $\rho=3, 0 < \phi < 2\pi, 2 < z < 2.8$ .	1	1	<b>07</b>
	b)	Derive Poisson's equation from point form of Gauss law.	1	1	<b>05</b>
	c)	Given the potential field $V = [A \rho^4 + B \rho^{-4}] \sin(4\phi)$ volts, show that $\nabla^2 V = 0$ . Also, determine the values of A and B, so that $V = 100$ volts and $ \mathbf{E}  = 500$ V/m at P ( $\rho=1, \phi = 22.5^\circ, z=2$ ).	1	1	<b>08</b>
		<b>UNIT - III</b>			
5	a)	State and explain Ampere's circuital law. Using the same, derive the expression for magnetic field intensity at any point due to an infinite length filamentary current carrying conductor present on z-axis.	1	1	<b>07</b>
	b)	Given the following values for $P_1, P_2$ and $I_1 \Delta \mathbf{L}_1$ , calculate $\Delta \mathbf{H}_2$ , $P_1(1, 2, 3), P_2(-3, -1, 2), 2\pi(-\mathbf{a}_x + \mathbf{a}_y + 2\mathbf{a}_z)$ $\mu\text{Am}$ .	1	1	<b>05</b>
	c)	Evaluate the boundary conditions at the interface of two magnetic media.	1	1	<b>08</b>
		<b>OR</b>			
6	a)	State and explain Biot-Savart's law.	1	1	<b>04</b>
	b)	A rectangular path is formed by $P_1(2, 3, 4)$ to $P_2(4, 3, 4)$ to $P_3(4, 3, 1)$ to $P_4(2, 3, 1)$ to $P_1$ . (i). Evaluate the closed line integral of $\mathbf{H}$ about the path, given that $\mathbf{H} = 3z \mathbf{a}_x - 2x^3 \mathbf{a}_z$ A/m (ii). Analyze the quotient enclosed by the path as an approximation to $(\nabla \times \mathbf{H})_y$ (iii). Evaluate $(\nabla \times \mathbf{H})_y$ at the center of the area.	2	2	<b>10</b>
	c)	Two differential current elements, $I_1 \Delta \mathbf{L}_1 = 3 \times 10^{-6} \mathbf{a}_y$ Am at $P_1(1, 0, 0)$ and $I_2 \Delta \mathbf{L}_2 = 3 \times 10^{-6}(-0.5 \mathbf{a}_x + 0.4 \mathbf{a}_y + 0.3 \mathbf{a}_z)$ Am at $P_2(2, 2, 2)$ are located in free-space. Find the vector force exerted on $I_1 \Delta \mathbf{L}_1$ by $I_2 \Delta \mathbf{L}_2$ .	1	1	<b>06</b>
		<b>UNIT - IV</b>			
7	a)	Starting from the equation of Faraday's law, obtain the point form of Maxwell's equation concerning spatial derivative of $\mathbf{E}$ and time derivative of $\mathbf{H}$ .	1	1	<b>05</b>
	b)	Within certain region, $\epsilon = 10^{-11}$ F/m and $\mu = 10^{-5}$ H/m, if $B_x = 2 \times 10^{-4} \cos(10^5 t) \sin(10^{-3} y)$ T, find $\mathbf{E}$ and analyse the total magnetic flux passing through the surface $x=0, 0 < y < 40\text{m}, 0 < z < 2\text{m}$ at $t = 1 \mu\text{s}$ .	2	2	<b>07</b>
	c)	Consider the case of wave propagation in free-space in which, $\mathbf{E}$ -field is x-direction. Using the Maxwell's equation in phasor form, obtain Helmholtz wave equation and comment the solution for $\mathbf{E}$ -field.	2	2	<b>08</b>

			<b>OR</b>			
	8	a)	Evaluate the amplitude of displacement current density  i. In the air space at point within a large power distribution transformer where $\vec{B} = 0.8 \cos[1.257 \times 10^{-6}(3 \times 10^8 t - x)] \hat{a}_y \text{ T}$ ii. In a metallic conductor at 60Hz, if $\epsilon = \epsilon_0$ , $\mu = \mu_0$ , $\sigma = 5.8 \times 10^7 \text{ S/m}$ and $\vec{J} = \sin(377t - 117.1z) \hat{a}_x \text{ MA/m}^2$ .	2	2	<b>08</b>
		b)	Starting from Maxwell's curl equation, obtain the equation of Poynting's theorem and analyze the same.	2	2	<b>12</b>
			<b>UNIT - V</b>			
	9	a)	Explain the reflection of uniform plane wave when it is incident normally on the boundary between two regions of different dielectric and hence obtain the expression of reflection coefficient.	1	1	<b>10</b>
		b)	Given $\eta_1 = 100 \Omega$ and $\eta_2 = 300 \Omega$ and $E_{x10}^+ = 100 \text{ V/m}$ : (i). Evaluate the field values for incident, reflected and transmitted wave. (ii). Analyze average power density of incident, reflected and transmitted wave.	2	2	<b>10</b>
			<b>OR</b>			
	10	a)	Starting from the total instantaneous field derive an expression for Standing Wave Ratio (SWR), which has both travelling wave and standing wave terms.	1	1	<b>08</b>
		b)	Consider a 50 MHz uniform plane wave having electric field amplitude of 10 V/m. The medium is lossless, having $\epsilon_r = \epsilon'_r = 9$ and $\mu_r = 1$ . The wave propagates in x, y plane at a $30^\circ$ angle to the x- axis and is linearly polarized along z. Obtain the phasor expression for the electric field.	1	1	<b>06</b>
		c)	Determine the reflection and transmission coefficients of an electric field wave travelling in air and is incident normally on a boundary between air and dielectric having permittivity $\epsilon_r = 4$ and permeability, $\mu_r = 1$ .	2	2	<b>06</b>

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