

B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

February / March 2023 Semester End Main Examinations

Programme: B.E.

Branch: ES Cluster (EI/MD/EC/EE/ET)

Course Code: 19ES5CCDSP

Course: Digital Signal Processing

Semester: V

Duration: 3 hrs.

Max Marks: 100

Date: 27.02.2023

Instructions: 1. Answer any FIVE full questions, choosing one full question from each unit.
2. Missing data, if any, may be suitably assumed.

UNIT - I

- 1 a) Consider the analog signal, $x_a(t) = 3 \cos(2000\pi t) + 5 \sin(6000\pi t) + 10 \cos(12000\pi t)$. **06**
- What is the Nyquist rate?
 - If $F_s = 5000$ samples/sec, Write the discrete time signal
 - What is the analog signal $y_a(t)$ that can be reconstructed from the samples if ideal interpolation is used?
- b) Compute the energy in frequency domain using Parseval's theorem for the 6-point sequence $x[n] = \{1, 3, -2, 1, -3, 4\}$. **06**
- c) Apply DFT-IDFT method to compute the circular convolution of two given sequences $x[n] = \{2, 1, 2, 1\}$, $h[n] = \{1, 2, 3, 4\}$. **08**

OR

- 2 a) Compute 4-point DFT of $x(n) = \{1, -2, 2, -1\}$. Write 4-point DFT of $y(n) = \{-2, 2, -1, 1\}$ using properties of DFT. **06**
- b) Compute the circular correlation of the sequence $x(n) = \{1, 1, 2, 1\}$. **06**
- c) Given 10-point sequence $x(n) = \{1, 2, 4, 6, -1, 2, 4, 1, 3, 7\}$ Compute i) $X(0)$ ii) $X(5)$ **08**
- iii) $\sum_{k=0}^9 X(k)$ iv) $\sum_{k=0}^9 |X(k)|^2$ without computing DFT

UNIT - II

- 3 a) Compute 8-point DFT of $h(n) = [1, 1, -1, -1]$ using DIF-FFT radix-2 algorithm. Identify what type of filter is this: LPF|HPF|BPF|BSF? **10**
- b) Compute the output $y(n)$ of a filter whose impulse response is $h(n) = \{1, 2\}$ and input signal $x(n) = \{1, 4, 3, 0, 7, 4, -7, -7, -1, 3, 4, 3\}$ using overlap and save method **10**

Important Note: Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.

UNIT - III

- 4 a) Design a digital IIR low pass filter using Butterworth approximation for the following analog specifications: **12**
Pass band edge : 500 Hz, Stop band edge : 750 Hz, Pass band gain : -3 dB, Stop band attenuation : -15dB, Sampling Frequency : 2000 Hz. Use Bilinear transformation.
- b) Obtain cascade structure for the given system **08**
$$y(n) = \frac{5}{8} y(n-1) - \frac{1}{16} y(n-2) + x(n) + \frac{3}{4} x(n-1) + \frac{1}{8} x(n-2)$$

OR

- 5 a) Given $H(s) = \frac{s+1}{s^2+5s+6}$, use impulse invariant transformation to convert this to $H(z)$. Assume $F_s = 1 \text{ Hz}$ **06**
- b) Obtain parallel structure for the given IIR system transfer function **08**
$$H(z) = \frac{z(3z+1)}{3(z-\frac{1}{2})(z-\frac{1}{4})}$$
- c) What are the limitations of impulse invariance method? Compare FIR and IIR filters **06**

UNIT - IV

- 6 a) Design a FIR digital filter using a Hamming window with $N=7$ **08**
$$H_d(e^{j\omega}) = \begin{cases} e^{-j3\omega} & |\omega| \leq \frac{3\pi}{4} \\ 0 & \frac{3\pi}{4} < |\omega| < \pi \end{cases}$$
- b) Determine the direct form realization and linear phase realization of digital filter with impulse response **06**
$$h(n) = \delta(n) - 0.5 \delta(n-1) + \frac{1}{4} \delta(n-2) + 0.25 \delta(n-3) - 0.5 \delta(n-4) + \delta(n-5)$$
- c) Mention the different types of window functions used in FIR filter design and also write their mathematical expressions. **06**

UNIT - V

- 7 a) Given a quadratic MSE function for the Wiener filter: $J = 40 - 20w + 10w^2$. Find the optimal solution for w^* to achieve the minimum MSE J_{\min} and determine J_{\min} . **04**
- b) Apply the LMS algorithm to adaptive filter for the noise cancellation with relevant block diagram. **08**
- c) With a neat block diagram explain two stage interpolator and decimator, representing multistage implementation of sampling rate conversion **08**
