

U.S.N.								
--------	--	--	--	--	--	--	--	--

B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

April 2025 Semester End Make-Up Examinations

Programme: B.E.

Semester: V

Branch: Industrial Engineering and Management

Duration: 3 hrs.

Course Code: 23IM5PCOPR

Max Marks: 100

Course: Operations Research

Instructions: 1. Answer any FIVE full questions, choosing one full question from each unit.
2. Missing data, if any, may be suitably assumed.

UNIT - I			CO	PO	Marks																
1	a)	Define OR. Give its origin and development of OR. Give its applications.	CO1	PO1	10																
	b)	A firm makes two types of pie of furniture, chairs and tables. The contribution for each product as calculated by the accounting department are Rs.200 per chair and Rs.300 per table. Both products are processed on three machines M1, M2 and M3. The time required to produce each product and the total time available per week on each machine are as follows i) Formulate this as LPP ii) How should the manufacturer schedule his production in order to maximize the contribution. <table border="1"> <tr> <th>Machine</th> <th>Chair</th> <th>Table</th> <th>Available hours</th> </tr> <tr> <td>M1</td> <td>3</td> <td>3</td> <td>36</td> </tr> <tr> <td>M2</td> <td>5</td> <td>2</td> <td>50</td> </tr> <tr> <td>M3</td> <td>2</td> <td>6</td> <td>60</td> </tr> </table>	Machine	Chair	Table	Available hours	M1	3	3	36	M2	5	2	50	M3	2	6	60	CO2	PO2	10
Machine	Chair	Table	Available hours																		
M1	3	3	36																		
M2	5	2	50																		
M3	2	6	60																		
OR																					
2	a)	Solve the problem LPP using Simplex method Maximize $Z = 2x_1 + 10x_2 + x_3$ Subjected to $5x_1 + 2x_2 + x_3 + s_1 \leq 15$ $2x_1 + x_2 + 7x_3 + s_2 \leq 20$ $x_1 + 3x_2 + 2x_3 + s_3 \leq 25$ $x_1, x_2, x_3 \geq 0$	CO2	PO2	10																
	b)	Solve the following by Big M method. Maximize $Z = 4x_1 + 5x_2 - 3x_3$ Subjected to $x_1 + x_2 + x_3 = 10$ $x_1 - x_2 \geq 1$ $2x_1 + 3x_2 + x_3 \leq 40$ $x_1, x_2, x_3 \geq 0$	CO2	PO2	10																

Important Note: Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.

UNIT - II																																			
3	a)	To solve the transportation problem what are the information must be known and what are the information mode and write the application of transportation model.	CO3	PO1	10																														
	b)	Three jobs are to be done by 4 machines each job can be assigned to one and only one machine. The cost of each job on each machine is given in the following	CO3	PO2	10																														
<table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th></th><th>M₁</th><th>M₂</th><th>M₃</th><th>M₄</th></tr> </thead> <tbody> <tr> <td>J₁</td><td>18</td><td>24</td><td>28</td><td>32</td></tr> <tr> <td>J₂</td><td>8</td><td>13</td><td>17</td><td>19</td></tr> <tr> <td>J₃</td><td>10</td><td>15</td><td>15</td><td>22</td></tr> </tbody> </table>							M ₁	M ₂	M ₃	M ₄	J ₁	18	24	28	32	J ₂	8	13	17	19	J ₃	10	15	15	22										
	M ₁	M ₂	M ₃	M ₄																															
J ₁	18	24	28	32																															
J ₂	8	13	17	19																															
J ₃	10	15	15	22																															
What are the job assignments which will minimize the total cost?																																			
OR																																			
4	a)	Maximize the following transportation matrix	CO3	PO2	10																														
		<table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th></th><th>M₁</th><th>M₂</th><th>M₃</th><th>M₄</th><th>Supply</th></tr> </thead> <tbody> <tr> <td>S₁</td><td>15</td><td>51</td><td>42</td><td>33</td><td>23</td></tr> <tr> <td>S₂</td><td>80</td><td>42</td><td>26</td><td>81</td><td>44</td></tr> <tr> <td>S₃</td><td>90</td><td>40</td><td>66</td><td>60</td><td>33</td></tr> <tr> <td>Demand</td><td>23</td><td>31</td><td>16</td><td>30</td><td></td></tr> </tbody> </table>		M ₁	M ₂	M ₃	M ₄	Supply	S ₁	15	51	42	33	23	S ₂	80	42	26	81	44	S ₃	90	40	66	60	33	Demand	23	31	16	30				
	M ₁	M ₂	M ₃	M ₄	Supply																														
S ₁	15	51	42	33	23																														
S ₂	80	42	26	81	44																														
S ₃	90	40	66	60	33																														
Demand	23	31	16	30																															
	b)	A company has 4 salesman A, B, C and D. These salesman are to be allotted 4 cities 1, 2, 3 and 4. The estimated profit per day for each salesman in each city is given in the following table	CO3	PO2	10																														
		<table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th></th><th>1</th><th>2</th><th>3</th><th>4</th></tr> </thead> <tbody> <tr> <td>A</td><td>16</td><td>10</td><td>14</td><td>11</td></tr> <tr> <td>B</td><td>14</td><td>11</td><td>15</td><td>15</td></tr> <tr> <td>C</td><td>15</td><td>15</td><td>13</td><td>12</td></tr> <tr> <td>D</td><td>13</td><td>12</td><td>14</td><td>15</td></tr> </tbody> </table>		1	2	3	4	A	16	10	14	11	B	14	11	15	15	C	15	15	13	12	D	13	12	14	15								
	1	2	3	4																															
A	16	10	14	11																															
B	14	11	15	15																															
C	15	15	13	12																															
D	13	12	14	15																															
	What is the optimum assignment which will yield maximum profit?																																		
UNIT - III																																			
5	a)	Explain the Queuing system, explain the characteristics of queuing system.	CO3	PO2	10																														
	b)	In a hair trimming salon with one barber, the customer arrival follows Poisson distribution at an average rate of 1 every 45 minutes. The service time is exponentially distributed with a mean of 30 minutes. Find <ol style="list-style-type: none"> Average number of customer in the salon Average waiting time of a customer before service Average idle time of the barber 	CO3	PO2	10																														
OR																																			
6	a)	At an emergency ward of a private hospital which can handle only one patient at a time, 96 patients arrive in a day on an average it takes on an average 10 minutes to treatment to a patient. The cost of treatment is Rs.200 per patient for 10 minutes. The cost creates at Rs.20 per minute of time reduced. How much minutes the cost increased at Rs.20 per minute of time. How much amount would be budgeted by the clinic to reduce the queue size to 1/2 ?	CO4	PO3	10																														

	b)	A supermarket has 2 salesgirls bringing into the sales at counter if the service time for each customer is exponentially distributed with a mean of 4 minutes and the people arrive in Poisson distribution at counters at the rate of 10 per hour , determine all the measures of multiple service model.	CO4	PO3	10																																								
		UNIT - IV																																											
7	a)	Explain the features of a game. Give the game theory terminology.	CO2	PO2	10																																								
	b)	Solve the following game. Determine the optimum strategies and the values of the game. $\begin{array}{cc} B_1 & B_2 \\ A_1 & \begin{bmatrix} 8 & -3 \\ -3 & 1 \end{bmatrix} \\ A_2 & \end{array}$	CO2	PO2	10																																								
		OR																																											
8	a)	Solve the game by graphical method. <table border="1" style="margin-left: auto; margin-right: auto; text-align: center;"><tr><td></td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td></tr><tr><td>1</td><td>3</td><td>0</td><td>6</td><td>-1</td><td>7</td></tr><tr><td>2</td><td>-1</td><td>5</td><td>-2</td><td>2</td><td>1</td></tr></table>		1	2	3	4	5	1	3	0	6	-1	7	2	-1	5	-2	2	1	CO2	PO2	10																						
	1	2	3	4	5																																								
1	3	0	6	-1	7																																								
2	-1	5	-2	2	1																																								
	b)	Write the general decision tree model and explain it.	CO1	PO1	10																																								
		UNIT - V																																											
9	a)	The following table gives the list of the jobs. <table border="1" style="margin-left: auto; margin-right: auto;"><thead><tr><th>Job</th><th>Immediate predecessor</th><th>Duration (days)</th></tr></thead><tbody><tr><td>A</td><td></td><td>5</td></tr><tr><td>B</td><td></td><td>10</td></tr><tr><td>C</td><td>A</td><td>6</td></tr><tr><td>D</td><td>B</td><td>8</td></tr><tr><td>E</td><td>C, D</td><td>7</td></tr><tr><td>F</td><td>C</td><td>4</td></tr><tr><td>G</td><td>C</td><td>8</td></tr><tr><td>H</td><td>E, F, B</td><td>7</td></tr><tr><td>I</td><td>A, H, D</td><td>6</td></tr></tbody></table> i) Draw the network ii) List all the paths and identify the critical path	Job	Immediate predecessor	Duration (days)	A		5	B		10	C	A	6	D	B	8	E	C, D	7	F	C	4	G	C	8	H	E, F, B	7	I	A, H, D	6	CO3	PO2	10										
Job	Immediate predecessor	Duration (days)																																											
A		5																																											
B		10																																											
C	A	6																																											
D	B	8																																											
E	C, D	7																																											
F	C	4																																											
G	C	8																																											
H	E, F, B	7																																											
I	A, H, D	6																																											
	b)	The following table gives a list of jobs along with their time estimates. <table border="1" style="margin-left: auto; margin-right: auto;"><thead><tr><th>Job</th><th>Optimistic time</th><th>Most likely time</th><th>Pessimistic time</th></tr></thead><tbody><tr><td>1 - 2</td><td>3</td><td>6</td><td>15</td></tr><tr><td>1 - 6</td><td>2</td><td>5</td><td>14</td></tr><tr><td>2 - 3</td><td>6</td><td>12</td><td>30</td></tr><tr><td>2 - 4</td><td>2</td><td>3</td><td>8</td></tr><tr><td>3 - 5</td><td>5</td><td>11</td><td>17</td></tr><tr><td>4 - 5</td><td>3</td><td>6</td><td>15</td></tr><tr><td>6 - 7</td><td>3</td><td>9</td><td>27</td></tr><tr><td>5 - 8</td><td>1</td><td>4</td><td>8</td></tr><tr><td>7 - 8</td><td>4</td><td>19</td><td>28</td></tr></tbody></table>	Job	Optimistic time	Most likely time	Pessimistic time	1 - 2	3	6	15	1 - 6	2	5	14	2 - 3	6	12	30	2 - 4	2	3	8	3 - 5	5	11	17	4 - 5	3	6	15	6 - 7	3	9	27	5 - 8	1	4	8	7 - 8	4	19	28	CO3	PO2	10
Job	Optimistic time	Most likely time	Pessimistic time																																										
1 - 2	3	6	15																																										
1 - 6	2	5	14																																										
2 - 3	6	12	30																																										
2 - 4	2	3	8																																										
3 - 5	5	11	17																																										
4 - 5	3	6	15																																										
6 - 7	3	9	27																																										
5 - 8	1	4	8																																										
7 - 8	4	19	28																																										

		<p>i) Draw the project network ii) What is the approximate probability that jobs in the critical path will be completed by the due date iii) What is the approximate probability that jobs on the next most critical path will be completed by the due date iv) What is your estimate of probability that the entire project will be completed by the due date v) Which due date has 90% chance of being met ?</p>																																																						
		OR																																																						
10	a)	<p>Explain the following</p> <p>i) Optimistic time ii) Pessimistic time iii) Most likely time</p>	CO3	PO2 06																																																				
	b)	<p>The time estimation of the activities of a project is given in the following table</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th>Activity</th> <th>Optimistic time</th> <th>Most likely time</th> <th>Pessimistic time</th> </tr> </thead> <tbody> <tr><td>1 - 2</td><td>1</td><td>2</td><td>3</td></tr> <tr><td>2 - 3</td><td>1</td><td>2</td><td>3</td></tr> <tr><td>2 - 4</td><td>1</td><td>3</td><td>5</td></tr> <tr><td>3 - 5</td><td>3</td><td>4</td><td>5</td></tr> <tr><td>4 - 5</td><td>2</td><td>3</td><td>4</td></tr> <tr><td>4 - 6</td><td>3</td><td>5</td><td>7</td></tr> <tr><td>5 - 7</td><td>6</td><td>7</td><td>8</td></tr> <tr><td>6 - 7</td><td>2</td><td>4</td><td>6</td></tr> <tr><td>7 - 8</td><td>4</td><td>6</td><td>8</td></tr> <tr><td>7 - 9</td><td>1</td><td>2</td><td>3</td></tr> <tr><td>8 - 10</td><td>3</td><td>5</td><td>7</td></tr> <tr><td>9 - 10</td><td></td><td></td><td></td></tr> </tbody> </table> <p>i) Construct a network ii) Identify critical path and all critical activities iii) What is the estimated time of the project ? iv) What is the probability of completing the project in 30 days ? v) What is the probability that the project will not be completed in 29 days ? vi) What is the probability that the project will be completed in 3 days later than expected ? vii) What is the probability that the project will be completed in 2 days earlier than expected ? viii) What due date has 90% chance of being met ?</p>	Activity	Optimistic time	Most likely time	Pessimistic time	1 - 2	1	2	3	2 - 3	1	2	3	2 - 4	1	3	5	3 - 5	3	4	5	4 - 5	2	3	4	4 - 6	3	5	7	5 - 7	6	7	8	6 - 7	2	4	6	7 - 8	4	6	8	7 - 9	1	2	3	8 - 10	3	5	7	9 - 10				CO3	PO2 14
Activity	Optimistic time	Most likely time	Pessimistic time																																																					
1 - 2	1	2	3																																																					
2 - 3	1	2	3																																																					
2 - 4	1	3	5																																																					
3 - 5	3	4	5																																																					
4 - 5	2	3	4																																																					
4 - 6	3	5	7																																																					
5 - 7	6	7	8																																																					
6 - 7	2	4	6																																																					
7 - 8	4	6	8																																																					
7 - 9	1	2	3																																																					
8 - 10	3	5	7																																																					
9 - 10																																																								
