

U.S.N.

B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

June 2025 Semester End Main Examinations

Programme: B.E.

Semester: VI

Branch: Institutional Elective

Duration: 3 hrs.

Course Code: 23IM6OEOPR / 22IM6OEOPR

Max Marks: 100

Course: Operations Research

Instructions: 1. Answer any FIVE full questions, choosing one full question from each unit.
2. Missing data, if any, may be suitably assumed.

Important Note: Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.			UNIT - I	<i>CO</i>	<i>PO</i>	Marks
	1	a)	Define the following terms related to LP: (i) Infeasible solution (ii) Degenerated solution (iii) Multiple solution	<i>CO1</i>	<i>PO1</i>	06
		b)	Solve the LPP using Simplex algorithm MIN $Z = 5x_1 + 3x_2$ subject to $2x_1 + 4x_2 \leq 12$, $2x_1 + 2x_2 = 10$ $5x_1 + 2x_2 \geq 10$ and $x_1, x_2 \geq 0$	<i>CO2</i>	<i>PO2</i>	14
			OR			
	2	a)	Any one standard definition of Operations Research and brief explanation on OR's Scope	<i>CO1</i>	<i>PO1</i>	05
		b)	Explain Phases of OR	<i>CO1</i>	<i>PO1</i>	05
		c)	The standard weight of a special purpose brick is 5 kg and it must contain two basic ingredients B1 and B2. B1 costs Rs 5 per kg and B2 costs Rs 8 per kg. Strength considerations dictate that the brick should contain not more than 4 kg of B1 and minimum 2 kg of B2. Since the demand for the product is likely to be related to the price of the brick, find the minimum cost of brick satisfying the above conditions. Formulate this situation as an LPP and solve it graphically.	<i>CO2</i>	<i>PO2</i>	10
			UNIT - II			
	3	a)	List the assumptions considered in the Transportation model	<i>CO1</i>	<i>PO1</i>	05

	b)	<p>A company has four factories P, Q, R and S which supply to three warehouses A, B, and C. the monthly Demand in tons at A, B and C is 120, 80 and 200 respectively, the monthly Production capacities in tons at factories P, Q, R and S is 60, 50, 140 and 50 respectively. The transportation cost in Rupees per ton is given in the matrix below. Using VAM, determine the transportation schedule that minimizes the total transportation cost.</p> <table><tr><td></td><td>A</td><td>B</td><td>C</td></tr><tr><td>P</td><td>4</td><td>3</td><td>7</td></tr><tr><td>Q</td><td>5</td><td>8</td><td>4</td></tr><tr><td>R</td><td>2</td><td>4</td><td>7</td></tr><tr><td>S</td><td>5</td><td>8</td><td>4</td></tr></table>		A	B	C	P	4	3	7	Q	5	8	4	R	2	4	7	S	5	8	4	CO2	PO2	15																
	A	B	C																																						
P	4	3	7																																						
Q	5	8	4																																						
R	2	4	7																																						
S	5	8	4																																						
		OR																																							
4	a)	<p>Analyze the transportation cost using Least Cost Method and check the optimality using MODI method for the following problem</p> <table><tr><td></td><td>A</td><td>B</td><td>C</td><td>D</td><td>E</td><td>Supply</td></tr><tr><td>X</td><td>8</td><td>8</td><td>9</td><td>4</td><td>3</td><td>800</td></tr><tr><td>Y</td><td>5</td><td>8</td><td>5</td><td>11</td><td>6</td><td>500</td></tr><tr><td>Z</td><td>8</td><td>9</td><td>7</td><td>3</td><td>3</td><td>900</td></tr><tr><td>Demand</td><td>400</td><td>350</td><td>300</td><td>250</td><td>900</td><td></td></tr></table>		A	B	C	D	E	Supply	X	8	8	9	4	3	800	Y	5	8	5	11	6	500	Z	8	9	7	3	3	900	Demand	400	350	300	250	900		CO2	PO2	10	
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Y	5	8	5	11	6	500																																			
Z	8	9	7	3	3	900																																			
Demand	400	350	300	250	900																																				
	b)	<p>Analyze the transportation cost using VAM and check the optimality using MODI method for the following problem</p> <table><tr><td></td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>Supply</td></tr><tr><td>A</td><td>1</td><td>9</td><td>13</td><td>36</td><td>51</td><td>50</td></tr><tr><td>B</td><td>24</td><td>12</td><td>16</td><td>20</td><td>1</td><td>100</td></tr><tr><td>C</td><td>14</td><td>33</td><td>1</td><td>23</td><td>26</td><td>150</td></tr><tr><td>Demand</td><td>100</td><td>70</td><td>50</td><td>40</td><td>40</td><td></td></tr></table>		1	2	3	4	5	Supply	A	1	9	13	36	51	50	B	24	12	16	20	1	100	C	14	33	1	23	26	150	Demand	100	70	50	40	40		CO2	PO2	10	
	1	2	3	4	5	Supply																																			
A	1	9	13	36	51	50																																			
B	24	12	16	20	1	100																																			
C	14	33	1	23	26	150																																			
Demand	100	70	50	40	40																																				
		UNIT - III																																							
5	a)	Differentiate between Assignment problem and Travelling salesmen problem	CO1	PO1	04																																				
	b)	<p>Find Solution of Travelling salesman problem</p> <table><tr><td>Work\Job</td><td>A</td><td>B</td><td>C</td><td>D</td><td>E</td></tr><tr><td>A</td><td>∞</td><td>5</td><td>8</td><td>1</td><td>5</td></tr><tr><td>B</td><td>5</td><td>∞</td><td>7</td><td>1</td><td>5</td></tr><tr><td>C</td><td>8</td><td>7</td><td>∞</td><td>8</td><td>6</td></tr><tr><td>D</td><td>1</td><td>1</td><td>8</td><td>∞</td><td>8</td></tr><tr><td>E</td><td>5</td><td>5</td><td>6</td><td>8</td><td>∞</td></tr></table>	Work\Job	A	B	C	D	E	A	∞	5	8	1	5	B	5	∞	7	1	5	C	8	7	∞	8	6	D	1	1	8	∞	8	E	5	5	6	8	∞	CO2	PO2	08
Work\Job	A	B	C	D	E																																				
A	∞	5	8	1	5																																				
B	5	∞	7	1	5																																				
C	8	7	∞	8	6																																				
D	1	1	8	∞	8																																				
E	5	5	6	8	∞																																				

	c)	Find the optimal Assignment that will result in minimum cost	CO2	PO2	08																																												
		<table><tr><td>Firm\Job</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td></tr><tr><td>A</td><td>44</td><td>67</td><td>41</td><td>53</td><td>48</td><td>64</td></tr><tr><td>B</td><td>46</td><td>69</td><td>40</td><td>45</td><td>45</td><td>68</td></tr><tr><td>C</td><td>43</td><td>73</td><td>37</td><td>51</td><td>44</td><td>62</td></tr><tr><td>D</td><td>50</td><td>65</td><td>35</td><td>50</td><td>46</td><td>65</td></tr></table>	Firm\Job	1	2	3	4	5	6	A	44	67	41	53	48	64	B	46	69	40	45	45	68	C	43	73	37	51	44	62	D	50	65	35	50	46	65												
Firm\Job	1	2	3	4	5	6																																											
A	44	67	41	53	48	64																																											
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C	43	73	37	51	44	62																																											
D	50	65	35	50	46	65																																											
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6	a)	Find the optimal assignment and optimum cost for the following problem shown below	CO2	PO2	10																																												
		<table><tr><td></td><td colspan="6">Jobs</td></tr><tr><td rowspan="6">M/c</td><td></td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td></tr><tr><td>A</td><td>12</td><td>13</td><td>8</td><td>11</td><td>10</td></tr><tr><td>B</td><td>10</td><td>11</td><td>12</td><td>9</td><td>13</td></tr><tr><td>C</td><td>13</td><td>10</td><td>15</td><td>12</td><td>11</td></tr><tr><td>D</td><td>15</td><td>14</td><td>13</td><td>10</td><td>12</td></tr><tr><td>E</td><td>11</td><td>12</td><td>14</td><td>13</td><td>15</td></tr></table>		Jobs						M/c		1	2	3	4	5	A	12	13	8	11	10	B	10	11	12	9	13	C	13	10	15	12	11	D	15	14	13	10	12	E	11	12	14	13	15			
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	D	15	14	13	10	12																																											
	E	11	12	14	13	15																																											
	b)	A person has to visit 5 cities and cost of going from one city to another is shown below. Find the optimum route and optimum cost using Hungarian method	CO2	PO2	10																																												
		<table><tr><td></td><td colspan="6">To</td></tr><tr><td rowspan="6">From</td><td></td><td>A</td><td>B</td><td>C</td><td>D</td><td>E</td></tr><tr><td>A</td><td>-</td><td>20</td><td>18</td><td>17</td><td>21</td></tr><tr><td>B</td><td>19</td><td>-</td><td>17</td><td>16</td><td>15</td></tr><tr><td>C</td><td>18</td><td>16</td><td>-</td><td>20</td><td>14</td></tr><tr><td>D</td><td>16</td><td>17</td><td>19</td><td>-</td><td>18</td></tr><tr><td>E</td><td>17</td><td>18</td><td>20</td><td>19</td><td>-</td></tr></table>		To						From		A	B	C	D	E	A	-	20	18	17	21	B	19	-	17	16	15	C	18	16	-	20	14	D	16	17	19	-	18	E	17	18	20	19	-			
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	D	16	17	19	-	18																																											
	E	17	18	20	19	-																																											
		UNIT - IV																																															
7	a)	Define the following w.r.t network analysis: i) Path ii) Activity iii) Looping iv) Network	CO1	PO1	04																																												

	b)	<p>A small project consists activities for which the relevant data is given below:</p> <table><tr><td>Activity</td><td>A</td><td>B</td><td>C</td><td>D</td><td>E</td><td>F</td><td>G</td></tr><tr><td>Preceding Activity</td><td>-</td><td>-</td><td>-</td><td>A , B</td><td>A, B</td><td>C , D, E</td><td>C , D, E</td></tr><tr><td>Duration (Days)</td><td>4</td><td>7</td><td>6</td><td>5</td><td>7</td><td>6</td><td>5</td></tr></table> <p>i) Draw the network and find the project completion time ii) Calculate earliest and latest times. iii) Calculate the total float, free float and independent floats for each activity.</p>	Activity	A	B	C	D	E	F	G	Preceding Activity	-	-	-	A , B	A, B	C , D, E	C , D, E	Duration (Days)	4	7	6	5	7	6	5	CO3	PO3	16								
Activity	A	B	C	D	E	F	G																														
Preceding Activity	-	-	-	A , B	A, B	C , D, E	C , D, E																														
Duration (Days)	4	7	6	5	7	6	5																														
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8	a)	Differentiate between PERT & CPM	CO1	PO1			04																														
	b)	<p>The time estimates (in weeks) for the activities of a network are given below: ISRO is planning a project to launch manned mission to moon and has listed activities and are as follows:</p> <table><tr><td>Activity</td><td colspan="3">Time estimates in Months</td></tr><tr><td>1 - 2</td><td>7</td><td>1</td><td>1</td></tr><tr><td>1 – 3</td><td>7</td><td>1</td><td>4</td></tr><tr><td>1 – 4</td><td>8</td><td>2</td><td>2</td></tr><tr><td>2 – 5</td><td>1</td><td>1</td><td>1</td></tr><tr><td>3 – 5</td><td>14</td><td>2</td><td>5</td></tr><tr><td>4 – 6</td><td>8</td><td>2</td><td>5</td></tr><tr><td>5 - 6</td><td>15</td><td>3</td><td>6</td></tr></table> <p>(i) Draw the network and determine the critical path and variance (ii) What is the probability that the project will be completed no more than 4 months later than the expected time? (iii) What should be the scheduled completion time for the probability of completion to be 50%</p>	Activity	Time estimates in Months			1 - 2	7	1	1	1 – 3	7	1	4	1 – 4	8	2	2	2 – 5	1	1	1	3 – 5	14	2	5	4 – 6	8	2	5	5 - 6	15	3	6	CO3	PO3	16
Activity	Time estimates in Months																																				
1 - 2	7	1	1																																		
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1 – 4	8	2	2																																		
2 – 5	1	1	1																																		
3 – 5	14	2	5																																		
4 – 6	8	2	5																																		
5 - 6	15	3	6																																		
		UNIT - V																																			
9	a)	<p>Four jobs 1, 2, 3 & 4 are to be processed on each of Five machines A, B, C & D in the order ABCDE. Find the total minimum elapsed time if no passing of jobs is permitted. Also determine idle time for each machine.</p> <table><tr><td>M/C & Jobs</td><td>A</td><td>B</td><td>C</td><td>D</td><td>E</td></tr><tr><td>1</td><td>7</td><td>5</td><td>2</td><td>3</td><td>9</td></tr><tr><td>2</td><td>6</td><td>6</td><td>4</td><td>5</td><td>10</td></tr><tr><td>3</td><td>5</td><td>4</td><td>5</td><td>6</td><td>8</td></tr><tr><td>4</td><td>8</td><td>3</td><td>3</td><td>2</td><td>6</td></tr></table>	M/C & Jobs	A	B	C	D	E	1	7	5	2	3	9	2	6	6	4	5	10	3	5	4	5	6	8	4	8	3	3	2	6	CO4	PO4	10		
M/C & Jobs	A	B	C	D	E																																
1	7	5	2	3	9																																
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