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# B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

## June 2025 Semester End Main Examinations

**Programme: B.E.**

**Semester: VI**

**Branch: Institutional Elective**

**Duration: 3 hrs.**

**Course Code: 23IM6OEOPR / 22IM6OEOPR**

**Max Marks: 100**

**Course: Operations Research**

**Instructions:** 1. Answer any FIVE full questions, choosing one full question from each unit.  
2. Missing data, if any, may be suitably assumed.

			<b>UNIT - I</b>		<i>CO</i>	<i>PO</i>	<b>Marks</b>	
<b>Important Note:</b> Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.	1	a)	Define the following terms related to LP: (i) Infeasible solution (ii) Degenerated solution (iii) Multiple solution		<i>CO1</i>	<i>PO1</i>	<b>06</b>	
		b)	Solve the LPP using Simplex algorithm $\text{MIN } Z = 5x_1 + 3x_2$ subject to $2x_1 + 4x_2 \leq 12$ , $2x_1 + 2x_2 = 10$ $5x_1 + 2x_2 \geq 10$ and $x_1, x_2 \geq 0$		<i>CO2</i>	<i>PO2</i>	<b>14</b>	
			<b>OR</b>					
		2	a)	Any one standard definition of Operations Research and brief explanation on OR's Scope		<i>CO1</i>	<i>PO1</i>	<b>05</b>
			b)	Explain Phases of OR		<i>CO1</i>	<i>PO1</i>	<b>05</b>
		c)	The standard weight of a special purpose brick is 5 kg and it must contain two basic ingredients B1 and B2. B1 costs Rs 5 per kg and B2 costs Rs 8 per kg. Strength considerations dictate that the brick should contain not more than 4 kg of B1 and minimum 2 kg of B2. Since the demand for the product is likely to be related to the price of the brick, find the minimum cost of brick satisfying the above conditions. Formulate this situation as an LPP and solve it graphically.		<i>CO2</i>	<i>PO2</i>	<b>10</b>	
			<b>UNIT - II</b>					
	3	a)	List the assumptions considered in the Transportation model		<i>CO1</i>	<i>PO1</i>	<b>05</b>	

	b)	<p>A company has four factories P, Q, R and S which supply to three warehouses A, B, and C. the monthly Demand in tons at A, B and C is 120, 80 and 200 respectively, the monthly Production capacities in tons at factories P, Q, R and S is 60, 50, 140 and 50 respectively. The transportation cost in Rupees per ton is given in the matrix below. Using VAM, determine the transportation schedule that minimizes the total transportation cost.</p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td></td><td style="text-align: center;">A</td><td style="text-align: center;">B</td><td style="text-align: center;">C</td></tr> <tr> <td style="text-align: center;">Furnaces</td><td style="border: 1px solid black; padding: 2px;">P</td><td style="border: 1px solid black; padding: 2px;">4</td><td style="border: 1px solid black; padding: 2px;">3</td><td style="border: 1px solid black; padding: 2px;">7</td></tr> <tr> <td></td><td style="border: 1px solid black; padding: 2px;">Q</td><td style="border: 1px solid black; padding: 2px;">5</td><td style="border: 1px solid black; padding: 2px;">8</td><td style="border: 1px solid black; padding: 2px;">4</td></tr> <tr> <td></td><td style="border: 1px solid black; padding: 2px;">R</td><td style="border: 1px solid black; padding: 2px;">2</td><td style="border: 1px solid black; padding: 2px;">4</td><td style="border: 1px solid black; padding: 2px;">7</td></tr> <tr> <td></td><td style="border: 1px solid black; padding: 2px;">S</td><td style="border: 1px solid black; padding: 2px;">5</td><td style="border: 1px solid black; padding: 2px;">8</td><td style="border: 1px solid black; padding: 2px;">4</td></tr> </table>		A	B	C	Furnaces	P	4	3	7		Q	5	8	4		R	2	4	7		S	5	8	4	<i>CO2</i>	<i>PO2</i>	<b>15</b>												
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		<b>OR</b>																																							
4	a)	Analyze the transportation cost using Least Cost Method and check the optimality using MODI method for the following problem	<i>CO2</i>	<i>PO2</i>	<b>10</b>																																				
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	b)	Analyze the transportation cost using VAM and check the optimality using MODI method for the following problem	<i>CO2</i>	<i>PO2</i>	<b>10</b>																																				
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		<b>UNIT - III</b>																																							
5	a)	Differentiate between Assignment problem and Travelling salesmen problem	<i>CO1</i>	<i>PO1</i>	<b>04</b>																																				
	b)	Find Solution of Travelling salesman problem	<i>CO2</i>	<i>PO2</i>	<b>08</b>																																				
		<table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td style="text-align: center;">Work\Job</td><td style="text-align: center;">A</td><td style="text-align: center;">B</td><td style="text-align: center;">C</td><td style="text-align: center;">D</td><td style="text-align: center;">E</td></tr> <tr> <td style="text-align: center;">A</td><td style="border: 1px solid black; padding: 2px;">v</td><td style="border: 1px solid black; padding: 2px;">5</td><td style="border: 1px solid black; padding: 2px;">8</td><td style="border: 1px solid black; padding: 2px;">4</td><td style="border: 1px solid black; padding: 2px;">5</td></tr> <tr> <td style="text-align: center;">B</td><td style="border: 1px solid black; padding: 2px;">5</td><td style="border: 1px solid black; padding: 2px;">v</td><td style="border: 1px solid black; padding: 2px;">7</td><td style="border: 1px solid black; padding: 2px;">4</td><td style="border: 1px solid black; padding: 2px;">5</td></tr> <tr> <td style="text-align: center;">C</td><td style="border: 1px solid black; padding: 2px;">8</td><td style="border: 1px solid black; padding: 2px;">7</td><td style="border: 1px solid black; padding: 2px;">v</td><td style="border: 1px solid black; padding: 2px;">8</td><td style="border: 1px solid black; padding: 2px;">6</td></tr> <tr> <td style="text-align: center;">D</td><td style="border: 1px solid black; padding: 2px;">4</td><td style="border: 1px solid black; padding: 2px;">4</td><td style="border: 1px solid black; padding: 2px;">8</td><td style="border: 1px solid black; padding: 2px;">v</td><td style="border: 1px solid black; padding: 2px;">8</td></tr> <tr> <td style="text-align: center;">E</td><td style="border: 1px solid black; padding: 2px;">5</td><td style="border: 1px solid black; padding: 2px;">5</td><td style="border: 1px solid black; padding: 2px;">6</td><td style="border: 1px solid black; padding: 2px;">8</td><td style="border: 1px solid black; padding: 2px;">v</td></tr> </table>	Work\Job	A	B	C	D	E	A	v	5	8	4	5	B	5	v	7	4	5	C	8	7	v	8	6	D	4	4	8	v	8	E	5	5	6	8	v			
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	c)	Find the optimal Assignment that will result in minimum cost	CO2	PO2	08																																										
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6	a)	Find the optimal assignment and optimum cost for the following problem shown below	CO2	PO2	10																																										
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	b)	A person has to visit 5 cities and cost of going from one city to another is shown below. Find the optimum route and optimum cost using Hungarian method	CO2	PO2	10																																										
		<table border="1"> <thead> <tr> <th rowspan="2">From</th><th colspan="5">To</th></tr> <tr> <th></th><th>A</th><th>B</th><th>C</th><th>D</th><th>E</th></tr> </thead> <tbody> <tr> <td>A</td><td>-</td><td>20</td><td>18</td><td>17</td><td>21</td></tr> <tr> <td>B</td><td>19</td><td>-</td><td>17</td><td>16</td><td>15</td></tr> <tr> <td>C</td><td>18</td><td>16</td><td>-</td><td>20</td><td>14</td></tr> <tr> <td>D</td><td>16</td><td>17</td><td>19</td><td>-</td><td>18</td></tr> <tr> <td>E</td><td>17</td><td>18</td><td>20</td><td>19</td><td>-</td></tr> </tbody> </table>	From	To						A	B	C	D	E	A	-	20	18	17	21	B	19	-	17	16	15	C	18	16	-	20	14	D	16	17	19	-	18	E	17	18	20	19	-			
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		<b>UNIT - IV</b>																																													
7	a)	Define the following w.r.t network analysis: i) Path    ii) Activity   iii) Looping   iv) Network	CO1	PO1	04																																										

	b)	<p>A small project consists of activities for which the relevant data is given below:</p> <table border="1"> <thead> <tr> <th>Activity</th><th>A</th><th>B</th><th>C</th><th>D</th><th>E</th><th>F</th><th>G</th></tr> </thead> <tbody> <tr> <td>Preceding Activity</td><td>-</td><td>-</td><td>-</td><td>A, B</td><td>A, B</td><td>C, D, E</td><td>C, D, E</td></tr> <tr> <td>Duration (Days)</td><td>4</td><td>7</td><td>6</td><td>5</td><td>7</td><td>6</td><td>5</td></tr> </tbody> </table> <p>i) Draw the network and find the project completion time  ii) Calculate earliest and latest times.  iii) Calculate the total float, free float and independent floats for each activity.</p>	Activity	A	B	C	D	E	F	G	Preceding Activity	-	-	-	A, B	A, B	C, D, E	C, D, E	Duration (Days)	4	7	6	5	7	6	5	CO3	PO3	<b>16</b>								
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8	a)	Differentiate between PERT & CPM	CO1	PO1	<b>04</b>																																
	b)	<p>The time estimates (in weeks) for the activities of a network are given below:  ISRO is planning a project to launch manned mission to moon and has listed activities and are as follows:</p> <table border="1"> <thead> <tr> <th>Activity</th><th colspan="3">Time estimates in Months</th></tr> </thead> <tbody> <tr> <td>1 - 2</td><td>7</td><td>1</td><td>1</td></tr> <tr> <td>1 – 3</td><td>7</td><td>1</td><td>4</td></tr> <tr> <td>1 – 4</td><td>8</td><td>2</td><td>2</td></tr> <tr> <td>2 – 5</td><td>1</td><td>1</td><td>1</td></tr> <tr> <td>3 – 5</td><td>14</td><td>2</td><td>5</td></tr> <tr> <td>4 – 6</td><td>8</td><td>2</td><td>5</td></tr> <tr> <td>5 - 6</td><td>15</td><td>3</td><td>6</td></tr> </tbody> </table> <p>(i) Draw the network and determine the critical path and variance  (ii) What is the probability that the project will be completed no more than 4 months later than the expected time?  (iii) What should be the scheduled completion time for the probability of completion to be 50%</p>	Activity	Time estimates in Months			1 - 2	7	1	1	1 – 3	7	1	4	1 – 4	8	2	2	2 – 5	1	1	1	3 – 5	14	2	5	4 – 6	8	2	5	5 - 6	15	3	6	CO3	PO3	<b>16</b>
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5 - 6	15	3	6																																		
		<b>UNIT - V</b>																																			
9	a)	<p>Four jobs 1, 2, 3 &amp; 4 are to be processed on each of Five machines A, B, C &amp; D in the order ABCDE. Find the total minimum elapsed time if no passing of jobs is permitted. Also determine idle time for each machine.</p> <table border="1"> <thead> <tr> <th>M/C &amp; Jobs</th><th>A</th><th>B</th><th>C</th><th>D</th><th>E</th></tr> </thead> <tbody> <tr> <td>1</td><td>7</td><td>5</td><td>2</td><td>3</td><td>9</td></tr> <tr> <td>2</td><td>6</td><td>6</td><td>4</td><td>5</td><td>10</td></tr> <tr> <td>3</td><td>5</td><td>4</td><td>5</td><td>6</td><td>8</td></tr> <tr> <td>4</td><td>8</td><td>3</td><td>3</td><td>2</td><td>6</td></tr> </tbody> </table>	M/C & Jobs	A	B	C	D	E	1	7	5	2	3	9	2	6	6	4	5	10	3	5	4	5	6	8	4	8	3	3	2	6	CO4	PO4	<b>10</b>		
M/C & Jobs	A	B	C	D	E																																
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	b)	Use graphical method to minimize the time required to process the following jobs on the machines shown below. For each machine specify the job which should be done first. Also calculate the total elapsed time and idle time to complete both jobs. Plot Gantt chart for both the jobs.	CO4	PO4	<b>10</b>																																								
		<table border="1"> <thead> <tr> <th colspan="7">Machines</th> </tr> <tr> <th></th> <th></th> <th></th> <th></th> <th></th> <th></th> <th></th> </tr> </thead> <tbody> <tr> <td rowspan="2">Job 1</td> <td>Sequence</td> <td>A</td> <td>B</td> <td>C</td> <td>D</td> <td>E</td> </tr> <tr> <td>Time (hrs)</td> <td>6</td> <td>8</td> <td>4</td> <td>12</td> <td>4</td> </tr> <tr> <td rowspan="2">Job 2</td> <td>Sequence</td> <td>B</td> <td>C</td> <td>A</td> <td>D</td> <td>E</td> </tr> <tr> <td>Time (hrs)</td> <td>10</td> <td>8</td> <td>6</td> <td>4</td> <td>12</td> </tr> </tbody> </table>	Machines														Job 1	Sequence	A	B	C	D	E	Time (hrs)	6	8	4	12	4	Job 2	Sequence	B	C	A	D	E	Time (hrs)	10	8	6	4	12			
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	Time (hrs)	10	8	6	4	12																																							
		<b>OR</b>																																											
10	a)	There are seven jobs, each of which has to be processed on machine A and then on Machine B (order of machining is AB). Processing time is given in hours. Find the optimal sequence in which the jobs are to be processed so as to minimize the total time elapsed.	CO4	PO4	<b>08</b>																																								
		<table border="1"> <tr> <td>JOB:</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> <td>7</td> </tr> <tr> <td>MACHINE: A (TIME IN HOURS).</td> <td>3</td> <td>12</td> <td>15</td> <td>6</td> <td>10</td> <td>11</td> <td>9</td> </tr> <tr> <td>MACHINE: B (TIME IN HOURS).</td> <td>8</td> <td>10</td> <td>10</td> <td>6</td> <td>12</td> <td>1</td> <td>3</td> </tr> </table>	JOB:	1	2	3	4	5	6	7	MACHINE: A (TIME IN HOURS).	3	12	15	6	10	11	9	MACHINE: B (TIME IN HOURS).	8	10	10	6	12	1	3																			
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	b)	List any 5 assumptions made in Sequencing problems	CO1	PO1	<b>04</b>																																								
	c)	Find the sequence of job 1 and 2 on four machines for the given technological order.	CO4	PO4	<b>08</b>																																								
		<table border="1"> <tr> <td>Job 1</td> <td>Order of machining:</td> <td>A</td> <td>B</td> <td>C</td> <td>D</td> </tr> <tr> <td></td> <td>Time in hours.</td> <td>2</td> <td>3</td> <td>3</td> <td>4</td> </tr> <tr> <td>Job 2</td> <td>Order of machining:</td> <td>A</td> <td>B</td> <td>C</td> <td>D</td> </tr> <tr> <td></td> <td>Time in hours.</td> <td>2</td> <td>3</td> <td>3</td> <td>4</td> </tr> </table>	Job 1	Order of machining:	A	B	C	D		Time in hours.	2	3	3	4	Job 2	Order of machining:	A	B	C	D		Time in hours.	2	3	3	4																			
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