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B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

September / October 2023 Supplementary Examinations

Programme: B.E

Semester: IV

Branch: Information Science and Engineering

Duration: 3 hrs.

Course Code: 19IS4PCTFC

Max Marks: 100

Course: Theoretical Foundations of Computations

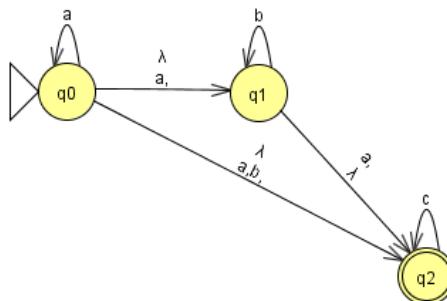
Date: 21.09.2023

Instructions: 1. Answer any FIVE full questions, choosing one full question from each unit.
2. Missing data, if any, may be suitably assumed.

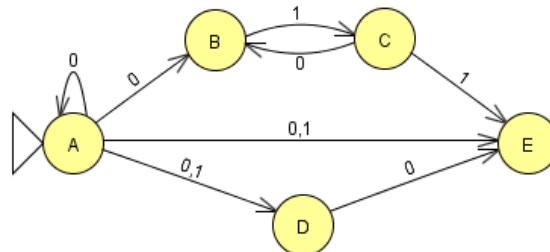
UNIT - I

1 a) Construct Deterministic Finite Automata to **09**
 i. Accept strings of a's and b's having exactly one 'a'.
 ii. Accept strings of 0's and 1's having 3 consecutive 0's
 iii. Accept strings which belong to the language $L=\{w \mid |w| \bmod 3=0 \text{ and } \Sigma=\{0,1\}\}$

b) Define ϵ -Closure. Give the ϵ -Closure of all the states in the given automaton. **03**



c) Convert the following NFA to DFA **08**



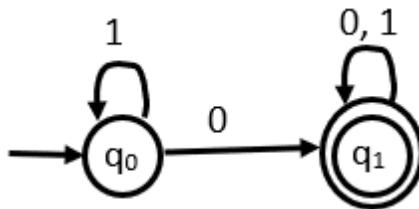
UNIT - II

2 a) Develop the Regular Expression for the following: **10**
 i. To accept strings of the language $L=\{a^n b^m \mid m+n \text{ is even}\}$
 ii. To accept strings of the language $L=\{a^n b^m \mid n \geq 4 \text{ and } m \leq 3\}$
 iii. To accept strings of 0's and 1's containing not more than three a's.
 iv. To accept strings of the language $L=\{w \mid w \text{ contains 010 as a substring for } \Sigma=\{0,1\}\}$

Important Note: Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.

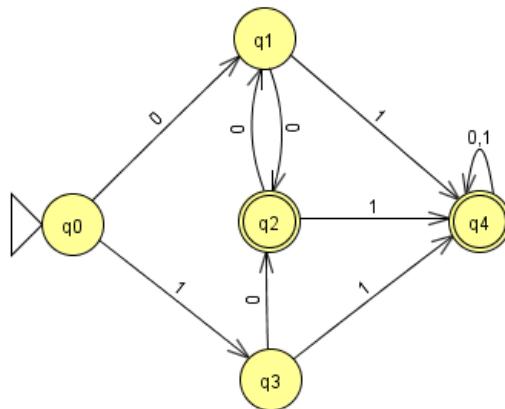
b) Show that the language $L=\{a^{n!} \mid n \geq 0\}$ is not regular. 06

c) Deduce regular expression for the finite automata using Kleene's theorem. 04

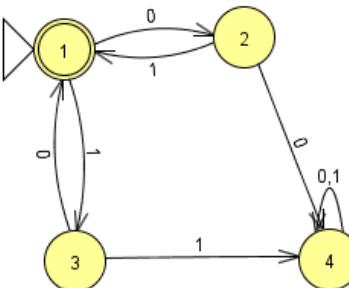


OR

3 a) Minimize the following DFA using Table filling algorithm 08



b) Obtain a Regular Expression for the Finite Automata given below 08



c) Obtain ϵ -NFA from the regular expression $ab(a+b)^*$ 04

UNIT - III

4 a) Define Context Free Grammar (CFG). Design CFG for the following languages and show derivation of the respective string: 10

- i. Language of all palindromes over $\Sigma=\{a,b\}$ and derive the string "abba"
- ii. $L=\{a^n b^n \mid n \geq 0\}$ and derive the string "aabb"
- iii. Language consisting of strings even no. of a's with $\Sigma=\{a\}$ and derive the string "aaaa"

b) Eliminate the NULL production and Unit production from the grammar given below **10**

$S \rightarrow AB \mid ABC$
 $A \rightarrow BA \mid BC \mid \epsilon \mid a$
 $B \rightarrow AC \mid CB \mid \epsilon \mid b$
 $C \rightarrow BC \mid AB \mid A \mid c$

OR

5 a) Define ambiguous grammar. Identify if the below given grammar is ambiguous for the string “id+id*id”: **05**

$E \rightarrow E+E$
 $E \rightarrow E-E$
 $E \rightarrow E^*E$
 $E \rightarrow E/E$
 $E \rightarrow id$

b) Convert the below given grammar to CNF: **10**

$S \rightarrow aA \mid a \mid B \mid C$
 $A \rightarrow aB \mid \epsilon$
 $B \rightarrow aA$
 $C \rightarrow cCD$
 $D \rightarrow abd$

c) Convert the following grammar to GNF: **05**

$S \rightarrow AA \mid 0$
 $A \rightarrow SS \mid 1$

UNIT - IV

6 a) Design Push Down Automata to accept by final state for the language **10**
 $L = \{w \in (a,b)^* \mid n_a(w) = n_b(w)\}$. Check whether the PDA is deterministic or not. Give instantaneous description for the string “aabbab”

b) Describe the algorithm to convert CFG to PDA. Using the same, convert the below grammar to PDA. Test whether “aabbabb” is acceptable by this PDA. **10**

$S \rightarrow aABB \mid aAA$
 $A \rightarrow aBB \mid a$
 $B \rightarrow bBB \mid b$
 $C \rightarrow a$

UNIT - V

7 a) Design Turing Machine to accept the language $L = \{ww^R \mid w \in (a,b)^*\}$. **12**
Provide instantaneous description for acceptance of the string “abba”.

b) Describe the following with an example: **08**

- Post Correspondence problem
- Decidable and Un-decidable language
