

B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

September / October 2023 Supplementary Examinations

Programme: B.E

Branch: Information Science and Engineering

Course Code: 19IS4PCTFC

Course: Theoretical Foundations of Computations

Semester: IV

Duration: 3 hrs.

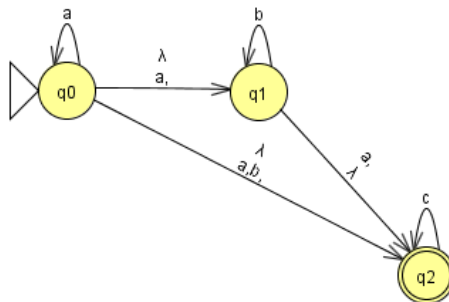
Max Marks: 100

Date: 21.09.2023

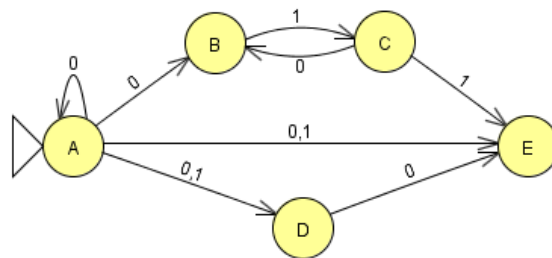
Instructions: 1. Answer any FIVE full questions, choosing one full question from each unit.
2. Missing data, if any, may be suitably assumed.

UNIT - I

- 1 a) Construct Deterministic Finite Automata to 09
- Accept strings of a's and b's having exactly one 'a'.
 - Accept strings of 0's and 1's having 3 consecutive 0's
 - Accept strings which belong to the language $L = \{w \mid |w| \bmod 3 = 0 \text{ and } \Sigma = \{0,1\}\}$
- b) Define ϵ -Closure. Give the ϵ -Closure of all the states in the given automaton. 03



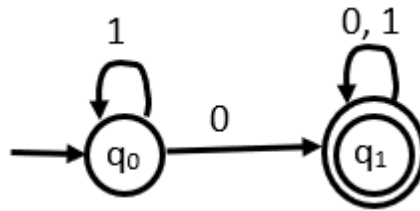
- c) Convert the following NFA to DFA 08



UNIT - II

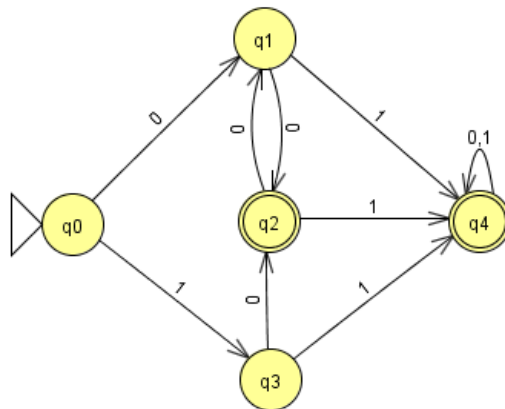
- 2 a) Develop the Regular Expression for the following: 10
- To accept strings of the language $L = \{a^n b^m \mid m+n \text{ is even}\}$
 - To accept strings of the language $L = \{a^n b^m \mid n \geq 4 \text{ and } m \leq 3\}$
 - To accept strings of 0's and 1's containing not more than three a's.
 - To accept strings of the language $L = \{w \mid w \text{ contains } 010 \text{ as a substring for } \Sigma = \{0,1\}\}$

- b) Show that the language $L = \{a^n \mid n \geq 0\}$ is not regular. 06
- c) Deduce regular expression for the finite automata using Kleene's theorem. 04

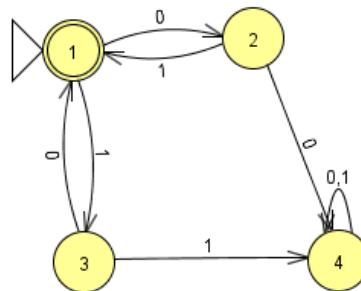


OR

- 3 a) Minimize the following DFA using Table filling algorithm 08



- b) Obtain a Regular Expression for the Finite Automata given below 08



- c) Obtain ϵ -NFA from the regular expression $ab(a+b)^*$ 04

UNIT - III

- 4 a) Define Context Free Grammar (CFG). Design CFG for the following languages and show derivation of the respective string: 10

- i. Language of all palindromes over $\Sigma = \{a, b\}$ and derive the string "abba"
- ii. $L = \{a^n b^n \mid n \geq 0\}$ and derive the string "aabb"
- iii. Language consisting of strings even no. of a's with $\Sigma = \{a\}$ and derive the string "aaaa"

- b) Eliminate the NULL production and Unit production from the grammar given below **10**
- $$S \rightarrow AB \mid ABC$$
- $$A \rightarrow BA \mid BC \mid \epsilon \mid a$$
- $$B \rightarrow AC \mid CB \mid \epsilon \mid b$$
- $$C \rightarrow BC \mid AB \mid A \mid c$$

OR

- 5 a) Define ambiguous grammar. Identify if the below given grammar is ambiguous for the string "id+id*id": **05**
- $$E \rightarrow E+E$$
- $$E \rightarrow E-E$$
- $$E \rightarrow E * E$$
- $$E \rightarrow E/E$$
- $$E \rightarrow id$$
- b) Convert the below given grammar to CNF: **10**
- $$S \rightarrow aA \mid a \mid B \mid C$$
- $$A \rightarrow aB \mid \epsilon$$
- $$B \rightarrow aA$$
- $$C \rightarrow cCD$$
- $$D \rightarrow abd$$
- c) Convert the following grammar to GNF: **05**
- $$S \rightarrow AA \mid 0$$
- $$A \rightarrow SS \mid 1$$

UNIT - IV

- 6 a) Design Push Down Automata to accept by final state for the language $L = \{w \in (a,b)^* \mid n_a(w) = n_b(w)\}$. Check whether the PDA is deterministic or not. Give instantaneous description for the string "aabbab" **10**
- b) Describe the algorithm to convert CFG to PDA. Using the same, convert the below grammar to PDA. Test whether "aabbabb" is acceptable by this PDA. **10**
- $$S \rightarrow aABB \mid aAA$$
- $$A \rightarrow aBB \mid a$$
- $$B \rightarrow bBB \mid b$$
- $$C \rightarrow a$$

UNIT - V

- 7 a) Design Turing Machine to accept the language $L = \{ww^R \mid w \in (a,b)^*\}$. Provide instantaneous description for acceptance of the string "abba". **12**
- b) Describe the following with an example: **08**
- Post Correspondence problem
 - Decidable and Un-decidable language
