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# B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

## August 2024 Semester End Main Examinations

**Programme: B.E.**

**Branch: Information Science and Engineering**

**Course Code: 22IS4PCTFC**

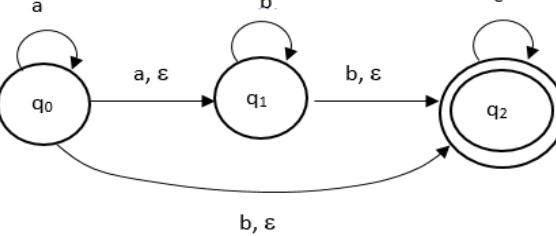
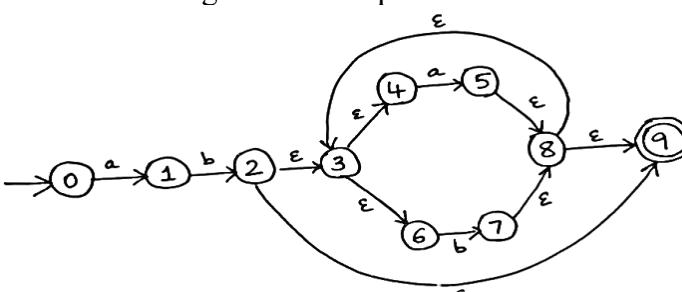
**Course: Theoretical Foundation of Computation**

**Semester: IV**

**Duration: 3 hrs.**

**Max Marks: 100**

**Instructions:** 1. Answer any FIVE full questions, choosing one full question from each unit.  
2. Missing data, if any, may be suitably assumed.

		UNIT - I	CO	PO	Marks												
1	a)	<p>Obtain DFA for the following languages with <math>\Sigma = \{a,b\}</math></p> <p>(i) All strings with even number of a's and even number of b's.</p> <p>(ii) All strings that do not contain substring 'aa'.</p> <p>(iii) All strings that begin and end with different letters, 'a' and 'b'.</p>	CO3	PO3	<b>06</b>												
	b)	<p>Convert the following NFA to equivalent DFA.</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td><math>\delta</math></td> <td>0</td> <td>1</td> </tr> <tr> <td><math>\rightarrow p</math></td> <td><math>\{p,q\}</math></td> <td><math>\{p\}</math></td> </tr> <tr> <td>q</td> <td><math>\emptyset</math></td> <td><math>\{r\}</math></td> </tr> <tr> <td><math>*r</math></td> <td><math>\{p,r\}</math></td> <td><math>\{q\}</math></td> </tr> </table>	$\delta$	0	1	$\rightarrow p$	$\{p,q\}$	$\{p\}$	q	$\emptyset$	$\{r\}$	$*r$	$\{p,r\}$	$\{q\}$	CO1	PO1	<b>08</b>
$\delta$	0	1															
$\rightarrow p$	$\{p,q\}$	$\{p\}$															
q	$\emptyset$	$\{r\}$															
$*r$	$\{p,r\}$	$\{q\}$															
	c)	<p>Provide definitions for <math>\epsilon</math>-NFA and <math>\epsilon</math>-CLOSURE. Write <math>\epsilon</math>-CLOSURE(<math>q</math>) considering each <math>q \in Q</math> for the given automaton.</p> 	CO1	PO1	<b>06</b>												
		<b>OR</b>															
2	a)	Convert the following $\epsilon$ -NFA to equivalent DFA.	CO1	PO1	<b>10</b>												
																	

**Important Note:** Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.

	b)	<p>Minimize the following finite automaton.</p> <table border="1"> <tr> <th><math>\delta</math></th><th>a</th><th>b</th></tr> <tr> <td>→ A</td><td>B</td><td>F</td></tr> <tr> <td>B</td><td>G</td><td>C</td></tr> <tr> <td>*C</td><td>A</td><td>C</td></tr> <tr> <td>D</td><td>C</td><td>G</td></tr> <tr> <td>E</td><td>H</td><td>F</td></tr> <tr> <td>F</td><td>C</td><td>G</td></tr> <tr> <td>G</td><td>G</td><td>E</td></tr> <tr> <td>H</td><td>G</td><td>C</td></tr> </table>	$\delta$	a	b	→ A	B	F	B	G	C	*C	A	C	D	C	G	E	H	F	F	C	G	G	G	E	H	G	C	CO1	PO1	<b>10</b>
$\delta$	a	b																														
→ A	B	F																														
B	G	C																														
*C	A	C																														
D	C	G																														
E	H	F																														
F	C	G																														
G	G	E																														
H	G	C																														
		<b>UNIT - II</b>																														
3	a)	<p>Obtain <math>\epsilon</math>-NFA for the regular expression</p> <p>(i) <math>(a+b)^* aba (a+b)^*</math>  (ii) <math>a^*b + (ab)^*</math></p>	CO1	PO1	<b>06</b>																											
	b)	Show that $L=\{w \mid w \in \{a,b\}^* \text{ and } n_a(w) < n_b(w)\}$ is not regular using Pumping Lemma, where $n_a(w)$ denotes number of a's and $n_b(w)$ denotes number of b's.	CO2	PO2	<b>08</b>																											
	c)	<p>Write regular expressions for the following languages:</p> <p>(i) Set of strings of a's and b's ending with either 'a' or 'bb'.</p> <p>(ii) Set of strings of a's and b's having substring 'ab'</p> <p>(iii) Set of strings consisting of even number of a's followed by odd number of b's.</p>	CO2	PO2	<b>06</b>																											
		<b>OR</b>																														
4	a)	<p>Obtain regular expression for the following finite automata by State elimination method.</p>	CO1	PO1	<b>10</b>																											
	b)	<p>State and prove Pumping Lemma for regular languages. Using the same, show that the language of palindromes is not regular.</p>	CO2	PO2	<b>10</b>																											
		<b>UNIT - III</b>																														
5	a)	<p>Obtain grammar to generate the following languages:</p> <p>(i) <math>L= \{ 0^m 1^m 2^n \mid m \geq 1 \text{ and } n \geq 0 \}</math>  (ii) <math>L= \{ w c w^R \mid w \in \{a,b\}^*, \Sigma=\{a,b,c\} \}</math></p>	CO3	PO3	<b>06</b>																											
	b)	<p>Show that the following grammar is ambiguous for the string aabbab.</p> <p><math>S \rightarrow aB \mid bA</math>  <math>A \rightarrow aS \mid bAA \mid a</math>  <math>B \rightarrow bS \mid aBB \mid b</math></p>	CO2	PO2	<b>05</b>																											

		c)	<p>Begin with the grammar</p> $S \rightarrow ABC \mid BaB$ $A \rightarrow aA \mid BaC \mid aaa$ $B \rightarrow bBb \mid a \mid D$ $C \rightarrow CA \mid AC$ $D \rightarrow \epsilon$ <p>(i) Eliminate <math>\epsilon</math>-productions.  (ii) Eliminate any unit productions in the resulting grammar.  (iii) Eliminate any useless symbols in the resulting grammar.  (iv) Put the resulting grammar into Chomsky Normal Form.</p>	CO1	PO1	<b>09</b>
			<b>UNIT - IV</b>			
6	a)		<p>Design Pushdown Automata for the language to accept string of balanced parenthesis by final state. The parenthesis to be considered are: (, ), [ , ]. Show instantaneous description for the string [( )]. Find out whether the PDA is deterministic or not.</p>	CO3	PO3	<b>12</b>
	b)		<p>Obtain Pushdown Automata for the grammar:</p> $S \rightarrow aABC$ $A \rightarrow aB \mid a$ $B \rightarrow bA \mid b$ $C \rightarrow a$	CO1	PO1	<b>08</b>
			<b>UNIT - V</b>			
7	a)		<p>Design Turing Machine to accept the language <math>L(M) = \{0^n 1^n 2^n \mid n \geq 1\}</math>. Show instantaneous description for 001122.</p>	CO3	PO3	<b>12</b>
	b)		<p>Let x and y be two positive integers considered as unary numbers over <math>\{1\}^+</math>. Obtain Turing Machine to perform <math>x+y</math>.</p>	CO2	PO2	<b>08</b>

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