

# B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

## August 2023 Semester End Make-Up Examinations

Programme: B.E.

Semester: I

Branch: Computer Science Stream

Duration: 3 hrs.

Course Code: 22MA1BSMCS

Max Marks: 100

Course: Mathematical Foundation for Computer Science Stream – 1

Date: 10.08.2023

**Instructions:** Answer any FIVE full questions, choosing one full question from each unit.

### UNIT – I

- 1 a) Find the pedal equation for the polar curve  $r^n = a^n (\cos n\theta + \sin n\theta)$ . 6
- b) Find the angle of intersection for the curves  $r = a \log \theta$  and  $r = \frac{a}{\log \theta}$ . 7
- c) Find the radius of curvature for the curve  $x^3 + y^3 = 3axy$  at the point  $\left(\frac{3a}{2}, \frac{3a}{2}\right)$ . 7

### UNIT – II

- 2 a) If  $z(x+y) = x^2 + y^2$ , Show that  $\left(\frac{\partial z}{\partial x} - \frac{\partial z}{\partial y}\right)^2 = 4\left(1 - \frac{\partial z}{\partial x} - \frac{\partial z}{\partial y}\right)$ . 6
- b) If  $u = f(2x - 3y, 3y - 4z, 4z - 2x)$ , prove that  $\frac{1}{2} \frac{\partial u}{\partial x} + \frac{1}{3} \frac{\partial u}{\partial y} + \frac{1}{4} \frac{\partial u}{\partial z} = 0$ . 7
- c) If  $u = \frac{yz}{x}$ ,  $v = \frac{zx}{y}$  and  $w = \frac{xy}{z}$ , show that  $\frac{\partial(u, v, w)}{\partial(x, y, z)} = 4$ . 7

### OR

- 3 a) Expand  $\log_e(1 + e^x)$  by the Maclaurin's series up to the fourth-degree term. 6
- b) If  $u = x^2 \tan^{-1}\left(\frac{y}{x}\right) - y^2 \tan^{-1}\left(\frac{x}{y}\right)$ , show that  $\frac{\partial^2 u}{\partial x \partial y} = \frac{x^2 - y^2}{x^2 + y^2}$ . 7
- c) Find the extreme values of the function  $f(x, y) = x^2 y^2 - 5x^2 - 8xy - 5y^2$ . 7

### UNIT – III

- 4 a) Solve the differential equation  $(5x^4 + 3x^2 y^2 - 2xy^3) dx + (2x^3 y - 3x^2 y^2 - 5y^4) dy = 0$ . 6

**Important Note:** Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.

- b) Solve the differential equation  $\frac{dy}{dx} + x \sin 2y = x^3 \cos^2 y$ . 7
- c) Show that the family of curves  $y^2 = 4a(x + a)$  is self-orthogonal where  $a$  is the parameter. 7

#### UNIT – IV

- 5 a) Find the integer solution of the Diophantine equation  $172x + 20y = 1000$ . 6
- b) Apply Chinese Remainder theorem to solve the system of linear congruences  $x \equiv 2(\text{mod } 3)$ ,  $x \equiv 3(\text{mod } 5)$ ,  $x \equiv 2(\text{mod } 7)$ . 7
- c) Apply Fermat's little theorem to find the remainder when  $72^{1001}$  is divided by 31. 7

#### OR

- 6 a) Solve the linear congruences  $18x \equiv 30(\text{mod } 42)$ . 6
- b) Solve the polynomial congruence  $x^3 + 3x + 5 \equiv 0(\text{mod } 9)$ . 7
- c) Apply RSA algorithm to find the public and private key using  $p = 3$  and  $q = 11$  and hence encrypt a certain message with plain text numeral "31". 7

#### UNIT - V

- 7 a) Investigate the values of  $\lambda$  and  $\mu$  such that the system  $x + y + z = 6$ ;  $x + 2y + 3z = 10$  and  $x + 2y + \lambda z = \mu$  has i) No solution ii) Unique solution and iii) infinite number of solutions. 6
- b) Apply Gauss – Seidel iterative method to solve the system of equations  $27x + 6y - z = 85$ ;  $6x + 15y + 2z = 72$  and  $x + y + 54z = 110$  by taking initial approximation as  $(0, 0, 0)$ . Carry out 3 iterations. 7
- c) Find all the eigenvalues and the corresponding eigenvectors of the matrix 7

$$A = \begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{bmatrix}$$

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