

MATHS ASSIGNMENT

1] Rank of a matrix-

$$>> A = \begin{bmatrix} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \end{bmatrix}$$

$$A = \begin{bmatrix} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \end{bmatrix}$$

$$\text{rank}(A) = 2$$

2] LU - Decomposition method-

$$>> A = \begin{bmatrix} 5 & 4 & 8 \\ 1 & 6 & 8 \\ 2 & 4 & 9 \end{bmatrix}$$

$$>> [L_1, U] = \text{lu}(A)$$

$$L_1 = \begin{bmatrix} 1.0000 & 0 & 0 \\ 0.2000 & 1.0000 & 0 \\ 0.4000 & 0.4615 & 1.000 \end{bmatrix}$$

$$U = \begin{bmatrix} 5.0000 & 4.0000 & 8.0000 \\ 0 & 5.2000 & 6.4000 \\ 0 & 0 & 2.8462 \end{bmatrix}$$

$$>> [L_2, U, P] = \text{lu}(A)$$

$$L_2 = \begin{bmatrix} 1.0000 & 0 & 0 \\ 0.2000 & 1.0000 & 0 \\ 0.4000 & 0.4615 & 1.0000 \end{bmatrix}$$

$$U = \begin{bmatrix} 5.0000 & 4.0000 & 8.0000 \\ 0 & 5.2000 & 6.4000 \\ 0 & 0 & 2.8462 \end{bmatrix}$$

$$P = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$>> x = U \setminus (L \setminus B)$$

$$x = \begin{bmatrix} 2 \\ -1 \\ 3 \end{bmatrix}$$

3. Gauss - Seidel method.

GaussSeidel.m

function Y = GaussSeidel(a, b, x, NoOfIterations)

D = diag(a);

a = a - diag(D);

D = 1./D;

n = length(x);

x = x(:);

Y = Zeros(n, NoOfIterations);

for j = 1: NoOfIterations

for k = 1: n

x(k) = (b(k) - a(k,:) * x) * D(k);

end

Y(:, j) = x;

end.

$$>> A = \begin{bmatrix} 27 & 6 & -1 \\ 6 & 15 & 2 \\ 1 & 1 & 54 \end{bmatrix}$$

$$A = \begin{bmatrix} 27 & 6 & -1 \\ 6 & 15 & 2 \\ 1 & 1 & 54 \end{bmatrix}$$

$$>> B = \begin{bmatrix} 110 \\ 85 \\ 72 \end{bmatrix}$$

$$B = \begin{bmatrix} 110 \\ 85 \\ 72 \end{bmatrix}$$

$$x_0 = [0; 0; 0]$$

$x_0 =$

0

0

0

>> GaussSeidel(A, B, x0, 4)

ans = 3.1481 2.4321 2.4257 2.4255
 3.5407 3.5721 3.5729 3.5730
 1.9132 1.9259 1.9259 1.9259

Gauss - elimination method -

function x = gauss ele(A, b);

[m, n] = size(A);

if, m $\neq$ n.

end

nb = n + 1;

Avq = [A, b];

% forward elimination

for k = 1 : n - 1

for i = k + 1 : n

factor = Avq(i, k) / Avq(k, k);

(i, k : n, b) = Avq(i, k : n, b) - factor * Avq(k, k : nb);

end

end

% backward substitution

x = zeros(n, 1);

x(n) = Avq(n, nb) / Avq(n, n);

for i = n - 1 : 1

x(i) = (Avq(i, nb) - Avq(i, i + 1 : n) * x(i + 1 : n)) / Avq(i, i);

end

x(i);

end

output:

```
>> A = [5 1 1 1; 1 7 1 1; 1 1 6 1; 1 1 1 4]
```

```
A = 5 1 1 1
     1 7 1 1
     1 1 6 1
     1 1 1 4
```

```
>> B = [4; 12; -5; -6]
```

```
B = 4
     12
     -5
     -6
```

```
>> Gauss_e(A, B)
```

```
= 1
   2
  -1
  -2
```

Eigen values and Eigen Vectors.

```
>> A = [-2 2 -3; 2 1 -6; -1 -2 0]
```

```
A = -2 2 -3
     2 1 -6
    -1 -2 0
```

```
>> [v, w] = eig(A)
```

```
v =
-0.9526    0.4082   -0.0230
 0.2722    0.8165    0.8353
-0.1361   -0.4082    0.5492
```

-3.0000

0

0

0

5.0000

0

0

0

-3.0000

Rayleigh Power method

$$A = \begin{bmatrix} 6 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{bmatrix};$$

$i = 0;$

$$x = [1; 1; 1];$$

while ($i < 5$)

$$X = (A * x) / \max((A * x));$$

disp(x);

$i = i + 1;$

end

disp(x);

$$t = X.' * x;$$

display(t);

$$u = ((A * x) * t)' * x;$$

$$evalue = u / t;$$

disp(evalue);

Ans:

1

1

1

1

1

1

1

1

1

1

1

t =

1.6667

6.0000

Newton Raphson -

Syms x;

fun = input("enter the function as a variable of x");

f = inline(fun);

Z = diff(f(x));

f₁ = inline(Z);

x₀ = input('Enter the initial value of interval');

x = x₀;

for i=0; inf

y = x;

x = y - (f(x)/f₁(x));

if x == y

break

end

end

f printf('The total number of iterations are:');

;

x

Answer -

Enter the function as a variable of x $\exp(x) + x - 2$

enter the initial value of interval 0.5

ans =

The total number of iterations are

i = 4

Newton Raphson forward interpolation -

$x = [8 \ 6 \ 8 \ 5 \ 15 \ 18];$

$f_x = [20 \ 20 \ 12 \ 7 \ 6 \ 6];$

$dt = \text{zeros}(6, 10);$

for $i = 1:6$ $dt(i, 1) = x(i);$

$dt(i, 2) = f_x(i);$ % calling function

end

$n = 5;$

for $j = 3:10$

for $i = 1:n$

$dt(i, j) = dt(i+1, j-1) - dt(i, j-1)$

end

$n = n-1;$

end

$h = x(2) - x(1)$

$x_p = 1.5;$

for $i = 1:5$

$q = (x_p - x(i)) / h;$

if $(q > 0 \ \&\& \ q < 1)$

$p = q$

end

end

p

$i = x_p - (p * h)$

for $i = 1:5$

if $(i == x(i))$

$y = i;$

end % calculating different value of y

$$f_0 = f_x(r);$$

$$f_{0_1} = dt(r, 3);$$

$$f_{0_2} = dt(r, (3+1));$$

$$f_{0_3} = dt(r, (3+2));$$

$$f_{0_4} = dt(r, (3+3));$$

$$f_p = (f_0 + ((p * f_{0_1}) + (p * (p-1) * f_{0_2}) / (2)) + ((p * (p-1) * (p-2) * f_{0_3}) / (6)) + ((p * (p-1) * (p-2) * (p-3) * f_{0_4}) / (24)) + ((p * (p-1) * (p-2) * (p-3) * (p-4) * f_{0_5}) / (120))) / (p!)$$

Answer

dt =

8	20	0	-8	11	-10	6	0	0	0
6	20	-8	3	1	-4	0	0	0	0
8	12	-5	4	-3	0	0	0	0	0
5	7	-1	1	0	0	0	0	0	0
15	6	0	0	0	0	0	0	0	0
18	6	0	0	0	0	0	0	0	0

Newton Raphson Backward interpolation -

$$x = [8 \ 8 \ 25 \ 16 \ 39 \ 49];$$

$$f_x = [14.621 \ 11.843 \ 9.870 \ 8.418 \ 7.305 \ 6.413];$$

$$dt = \text{zeros}(6, 7);$$

$$\text{for } i = 1:6$$

$$dt(i, 1) = x(i);$$

$$dt(i, 2) = f_x(i);$$

end

$$n = 5$$

$$\text{for } j = 3:7$$

$$\text{for } i = 1:n$$

$x(i, j) = dt(i+1, j-1) - dt(i, j-1)$
end

$n = n - 1;$

end

$h = x(2) - x(1)$

$x_p = 27;$

for $i = 1:6$

$q = (x_p - x(i)) / h;$

if $(q > 0 \ \&\& \ q < 1)$

$P = q;$

end

end

P

$i = x_p - (P * h)$

for $i = 1:6$

if $(1 == x(i))$

$r = i$

end

end

$f_0 = f_x(r);$

$f_{01} = dt((r-1), 3);$

$f_{02} = dt((r-2), (3+1));$

$f_{03} = dt((r-3), (3+2));$

$f_{04} = dt((r-4), (3+3));$

$f_p = (f(0) + ((P * f_{01}) + (P * (P+1) * f_{02}) / (2)) + ((P * (P+1) * (P+2) * f_{03}) / (6))$

Answer

dt =	8.0000	14.6210	-2.7780	0.8050	-0.2840
	0.1020	-0.0380			
	8.0000	11.8430	-1.9730	0.5210	-0.1820
	0.0640	0			
	25.0000	9.8700	-1.4520	0.3390	-0.1180
	0	0			
	16.0000	8.4180	-1.1130	0.2210	0
	0	0			
	39.0000	7.3050	-0.8920	0	0
	0	0			
	49.0000	6.4130	0	0	0
	0	0			