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# B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

## February 2025 Semester End Main Examinations

**Programme: B.E.**

**Branch: Mechanical Engineering**

**Course Code: 23ME4ESORE**

**Course: Operations Research**

**Semester: IV**

**Duration: 3 hrs.**

**Max Marks: 100**

**Instructions:** 1. Answer any FIVE full questions, choosing one full question from each unit.  
2. Missing data, if any, may be suitably assumed.

<b>UNIT - I</b>			<b>CO</b>	<b>PO</b>	<b>Marks</b>
1	a)	Explain the scope of Operations Research	<i>CO1</i>	<i>PO1</i> <i>PO2</i> <i>PO3</i>	<b>10</b>
	b)	A man goes to market to purchase buttons. He needs at least 20 large buttons and small 30 buttons. The shopkeeper sells button in two forms (i) boxes and (ii) cards. A box contains 2 large buttons and 5 small buttons and a card 10 large buttons and 5 small buttons. Find the most economical way in which he should purchase the buttons, if a box costs 10 paisa and a card costs 25 paisa only. Formulate the problem and solve using graphical method.	<i>CO1</i>	<i>PO1</i> <i>PO2</i> <i>PO3</i>	<b>10</b>
<b>OR</b>					
2	a)	Explain feasible, basic feasible and optimal solution.	<i>CO1</i>	<i>PO1</i> <i>PO2</i> <i>PO3</i>	<b>06</b>
	b)	Solve the following LPP by the simplex method. $\text{Max } Z = 3x_1 + 2x_2$ Subject to constraints $2x_1 + x_2 \leq 1$ $3x_1 + 4x_2 \geq 4$ $x_1, x_2 \geq 0$	<i>CO1</i>	<i>PO1</i> <i>PO2</i> <i>PO3</i>	<b>14</b>
<b>UNIT - II</b>					
3	a)	Solve the dual simplex method to solve the following linear programming problem $\text{Max } Z = -2x_1 - 3x_2$ Subject to constraints $x_1 + x_2 \geq 2$ $2x_1 + x_2 \leq 10$ $x_1 + x_2 \leq 8$ $x_1, x_2 \geq 0$	<i>CO2</i>	<i>PO1</i> <i>PO2</i> <i>PO3</i>	<b>14</b>

**Important Note:** Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.

	b)	What are the advantages of Revised simplex method over standard simplex method?	CO2	PO1 PO2 PO3	06																																								
		<b>OR</b>																																											
4	a)	Obtain the dual of the following primal LP problem. Maximize $Z = x_1 - 2x_2 + 3x_3$ subject to the constraints (i) $-2x_1 + x_2 + 3x_3 = 2$ , (ii) $2x_1 + 3x_2 + 4x_3 = 1$ and $x_1, x_2, x_3 \geq 0$	CO2	PO1 PO2 PO3	06																																								
	b)	Use the revised simplex method to solve the following LP problem: Maximize $Z = 2x_1 + x_2$ subject to the constraints (i) $3x_1 + 4x_2 \leq 6$ , (ii) $6x_1 + x_2 \leq 3$ and $x_1, x_2 \geq 0$	CO2	PO1 PO2 PO3	14																																								
		<b>UNIT - III</b>																																											
5		A cement company has 3 factories which manufactures cement and sends to 4 distribution centers. The supply position, demand and the associated transportation cost per quintal are shown below:	CO1	PO1 PO2 PO3	20																																								
		<table border="1" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th colspan="2"></th> <th colspan="4">Distribution centre</th> <th>Supply</th> </tr> <tr> <th colspan="2"></th> <th>W</th> <th>X</th> <th>Y</th> <th>Z</th> <th><math>C_i</math></th> </tr> </thead> <tbody> <tr> <td rowspan="3" style="text-align: center;">Factory</td> <td>A</td> <td>10</td> <td>8</td> <td>5</td> <td>4</td> <td>7</td> </tr> <tr> <td>B</td> <td>7</td> <td>9</td> <td>15</td> <td>8</td> <td>8</td> </tr> <tr> <td>C</td> <td>6</td> <td>10</td> <td>14</td> <td>8</td> <td>10</td> </tr> <tr> <td></td> <td>Demand</td> <td>6</td> <td>6</td> <td>8</td> <td>5</td> <td></td> </tr> </tbody> </table> <p> i) Find out the optimal transportation schedule.  ii) If the company wants, at least 5 quintals of cement to be sent from C to Y, will the transportation schedule be any different. If so, what will be the new optimal schedule and cost?  iii) Suppose the company desires to send at most 0.5 quintals from C to Y, what will be the optimal schedule and cost? </p>			Distribution centre				Supply			W	X	Y	Z	$C_i$	Factory	A	10	8	5	4	7	B	7	9	15	8	8	C	6	10	14	8	10		Demand	6	6	8	5				
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		<b>OR</b>																																											
6	a)	A company has 4 territories open and 4 salespersons available for assignment. The territories are not equally rich in their sales potential. It is estimates that a typical salesperson operating in each territory would bring in the following annual sales:	CO1	PO1 PO2 PO3	16																																								
		<table border="1" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th>Territory</th> <th>I</th> <th>II</th> <th>III</th> <th>IV</th> </tr> </thead> <tbody> <tr> <td>Annual sales (Rs)</td> <td>60000</td> <td>50000</td> <td>40000</td> <td>30000</td> </tr> </tbody> </table> <p>Four salesperson are also considered to differ in their ability: it is</p>	Territory	I	II	III	IV	Annual sales (Rs)	60000	50000	40000	30000																																	
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		<p>estimated that working under the same conditions, their yearly sales would be proportional as follows:</p> <table border="1"> <tr> <td>Salesperson</td><td>A</td><td>B</td><td>C</td><td>D</td></tr> <tr> <td>Proportion</td><td>7</td><td>5</td><td>5</td><td>4</td></tr> </table> <p>If the criterion is to maximize expected sales, then the initiative answer is to assign the best salesperson to the richest territory, the next best salesperson to the second richest territory and so on. Verify this answer by the assignment technique.</p>	Salesperson	A	B	C	D	Proportion	7	5	5	4																																		
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	b)	Explain the difference between TP and AP	CO1	PO1 PO2 PO3																																										
<b>UNIT - IV</b>																																														
7	a)	Explain the following terms with reference to game theory i) Saddle point ii) Mixed strategy iii) 2-person zero sum game	CO3	PO1 PO2 PO3																																										
	b)	<p>A chemical manufacturer has to process 7 products through two stages of manufacturing viz., Crushing and Refining. The time taken for each of these items at the different stages is given below in appropriate units.</p> <table border="1"> <tr> <td>Products</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td></tr> <tr> <td>Time</td><td>Crushing</td><td>5</td><td>7</td><td>3</td><td>4</td><td>6</td><td>7</td><td>12</td></tr> <tr> <td></td><td>Refining</td><td>2</td><td>6</td><td>7</td><td>5</td><td>9</td><td>5</td><td>8</td></tr> </table> <p>i) Find an order in which these products are to be produced through these stages so as to minimize the total processing time. Also determine the make span and idle time for each process.</p> <p>ii) Suppose a third stage viz., Finishing, with the following processing time is to be added, find the order in which these products are to be produced through these three stages so as to minimize the total processing time.</p> <table border="1"> <tr> <td>Products</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td></tr> <tr> <td>Finishing</td><td>10</td><td>12</td><td>11</td><td>13</td><td>12</td><td>10</td><td>11</td></tr> </table>	Products	1	2	3	4	5	6	7	Time	Crushing	5	7	3	4	6	7	12		Refining	2	6	7	5	9	5	8	Products	1	2	3	4	5	6	7	Finishing	10	12	11	13	12	10	11	CO4	PO1 PO2 PO3
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8	a)	Players A and B play a game in which each has three coins, a 5p, 10p and a 20p. Each selects a coin without the knowledge of the other's choice. If the sum of the coins is an odd amount, then A wins B's coin. But, if the sum is even, then B wins A's coin. Find the best strategy for each player and the values of the game.	CO4	PO1 PO2 PO3																																										
	b)	Use the graphical method to minimize the time needed to process the following jobs on the machines shown, i.e. for each machine find the job that should be done first. Also, calculate the total elapsed time to complete both jobs.	CO4	PO1 PO2 PO3																																										

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