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B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

May 2024 Semester End Make-Up Examinations

Programme: B.E.

Branch: Mechanical Engineering

Course Code: 16ME8DCORE

Course: Operations Research

Semester: VIII

Duration: 3 hrs.

Max Marks: 100

Instructions: 1. Answer any FIVE full questions, choosing one full question from each unit.
2. Missing data, if any, may be suitably assumed.

UNIT - I			CO	PO	Marks
1	a)	Define OR. Explain the characteristics of OR.	CO1	PO1	08
	b)	A manufacturer of a line of patent medicines is preparing a production plan on medicines A and B. There are sufficient ingredients available to make 20,000 bottles of A and 40,000 bottles of B, but there are only 45,000 bottles into which either of the medicines can be filled. Furthermore, it takes 3 hours to prepare enough material to fill 1000 bottles of A and 1 hour to prepare enough material to fill 1000 bottles of B and there are 66 hours available for this operation. The profit is Rs. 8 per bottle of A and Rs.7 per bottle of B. Formulate this problem as L.P.P to maximize the profit and solve graphically to determine the maximum profit.		PO1	12
OR					
2	a)	What do you mean by degeneracy in simplex problem? How do you resolve it?	CO1	PO1	05
	b)	Show that there is an unbounded solution to the following LPP $\text{Max } Z = 4x_1 + x_2 + 3x_3 + 5x_4$ $\text{Subject to } 4x_1 - 6x_2 - 5x_3 - 4x_4 \geq -20$ $-3x_1 - 2x_2 + 4x_3 + x_4 \leq 10$ $-8x_1 - 3x_2 + 3x_3 + 2x_4 \leq 20$ $x_1, x_2, x_3, x_4 \geq 0$	CO1	PO1	15

Important Note: Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.

		UNIT - II																																									
3	a)	Solve the following TP to determine the optimum transportation schedule.						CO2	PO1																																		
		<table border="1"> <thead> <tr> <th></th><th>D</th><th>E</th><th>F</th><th>G</th><th></th><th>supply</th></tr> </thead> <tbody> <tr> <td>A</td><td>8</td><td>10</td><td>7</td><td>6</td><td></td><td>50</td></tr> <tr> <td>B</td><td>12</td><td>9</td><td>4</td><td>7</td><td></td><td>40</td></tr> <tr> <td>C</td><td>9</td><td>11</td><td>10</td><td>8</td><td></td><td>30</td></tr> <tr> <td>Demand</td><td>25</td><td>32</td><td>40</td><td>23</td><td></td><td></td></tr> </tbody> </table>							D	E	F	G		supply	A	8	10	7	6		50	B	12	9	4	7		40	C	9	11	10	8		30	Demand	25	32	40	23			12
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	b)	Explain Degeneracy in Transportation problem.						2	I																																		
		OR																																									
4	a)	Four workers are available to work on four machines and the respective costs associated with each machine worker assignment is given below:						CO2	PO1																																		
		<table border="1"> <thead> <tr> <th colspan="2"></th><th colspan="4">MACHINE</th></tr> <tr> <th></th><th></th><th>M1</th><th>M2</th><th>M3</th><th>M4</th></tr> </thead> <tbody> <tr> <td rowspan="4">Workers</td><td>W1</td><td>12</td><td>3</td><td>6</td><td>-</td></tr> <tr> <td>W2</td><td>4</td><td>10</td><td>-</td><td>5</td></tr> <tr> <td>W3</td><td>7</td><td>2</td><td>8</td><td>9</td></tr> <tr> <td>W4</td><td>-</td><td>7</td><td>8</td><td>6</td></tr> </tbody> </table>								MACHINE						M1	M2	M3	M4	Workers	W1	12	3	6	-	W2	4	10	-	5	W3	7	2	8	9	W4	-	7	8	6	12		
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		The sign (-) indicates that the particular worker machine assignment is not permitted. (i) Determine the optimum assignment. (ii) A fifth machine is available to replace one of the existing machines and the associated costs are W1 = 4 Rs, W2=3 Rs. W3=3Rs and W4=2 Rs. Determine whether the new machine can be accepted and if so, which machine does it replace?																																									
	b)	Differentiate between Transportation and Assignment problems.						CO2	PO1																																		
		UNIT - III																																									
5	a)	Solve the following game.						CO3	PO1																																		
		<table border="1"> <thead> <tr> <th colspan="2"></th><th colspan="3">Player A strategies</th></tr> <tr> <th>Player B strategies</th><th></th><th>I</th><th>II</th><th>III</th></tr> </thead> <tbody> <tr> <td rowspan="3">Player A strategies</td><td>A</td><td>-4</td><td>6</td><td>3</td></tr> <tr> <td>B</td><td>-3</td><td>-3</td><td>4</td></tr> <tr> <td>C</td><td>2</td><td>-3</td><td>4</td></tr> </tbody> </table>								Player A strategies			Player B strategies		I	II	III	Player A strategies	A	-4	6	3	B	-3	-3	4	C	2	-3	4	10												
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	b)	Players A and B play a game in which each player has three coins 20p, 25p and 50p. Each of them selects a coin without the knowledge of the other player. If the sum of the values of the coins is an even number, A wins B's coin. If the sum is an odd number, B wins A's coin. (i) Develop a payoff matrix with respect to player A. (ii) Find the optimal strategies for the players. What is the value of the game?						CO3	PO1																																		
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		UNIT - IV																																																																																		
6	a)	There are six jobs, each of which is to be processed through three machines A, B and C in the order CBA, processing time in hours are shown in the table below.						CO4	PO4																																																																											
		<table border="1"> <thead> <tr> <th colspan="2">Jobs</th><th colspan="3">Machines</th></tr> <tr> <th colspan="2"> </th><th colspan="2">A</th><th>B</th></tr> </thead> <tbody> <tr> <td colspan="2">1</td><td colspan="2">8</td><td>3</td></tr> <tr> <td colspan="2">2</td><td colspan="2">7</td><td>4</td></tr> <tr> <td colspan="2">3</td><td colspan="2">6</td><td>5</td></tr> <tr> <td colspan="2">4</td><td colspan="2">9</td><td>2</td></tr> <tr> <td colspan="2">5</td><td colspan="2">10</td><td>1</td></tr> <tr> <td colspan="2">6</td><td colspan="2">9</td><td>6</td></tr> <tr> <td colspan="2"></td><td colspan="2"></td><td>C</td></tr> <tr> <td colspan="2"></td><td colspan="2"></td><td>8</td></tr> <tr> <td colspan="2"></td><td colspan="2"></td><td>3</td></tr> <tr> <td colspan="2"></td><td colspan="2"></td><td>7</td></tr> <tr> <td colspan="2"></td><td colspan="2"></td><td>2</td></tr> <tr> <td colspan="2"></td><td colspan="2"></td><td>5</td></tr> <tr> <td colspan="2"></td><td colspan="2"></td><td>1</td></tr> </tbody> </table>		Jobs		Machines					A		B	1		8		3	2		7		4	3		6		5	4		9		2	5		10		1	6		9		6					C					8					3					7					2					5					1	Determine the optimum sequence for the five jobs and the minimum elapsed time.					
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	b)	Use graphical method to solve the following sequencing problem, also calculate the total time required to complete both the jobs.						CO4	PO1																																																																											
		<table border="1"> <thead> <tr> <th colspan="2">Job 1</th><th colspan="2">Sequence</th><th>A</th><th>B</th><th>C</th><th>D</th><th>E</th></tr> <tr> <th colspan="2"></th><th colspan="2">Time(hrs)</th><th>2</th><th>3</th><th>4</th><th>6</th><th>2</th></tr> </thead> <tbody> <tr> <th colspan="2">Job 2</th><th colspan="2">Sequence</th><th>C</th><th>A</th><th>D</th><th>E</th><th>B</th></tr> <tr> <th colspan="2"></th><th colspan="2">Time(hrs)</th><th>4</th><th>5</th><th>3</th><th>2</th><th>6</th></tr> </tbody> </table>								Job 1		Sequence		A	B	C	D	E			Time(hrs)		2	3	4	6	2	Job 2		Sequence		C	A	D	E	B			Time(hrs)		4	5	3	2	6																																							
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7	a)	The cost of a machine is Rs 6100 and its scrap value is only Rs 100. The maintenance costs are found from experience to be as follows:						CO5	PO1																																																																											
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		When should the machine be replaced?																																																																																		
	b)	Find the cost per period of individual replacement policy of an installation of 300 light bulbs, given the following: Cost of replacing an individual bulb is Rs. 2 Conditional probability of failure is given below:						CO5	PO1																																																																											
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