

# B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

## May 2023 Semester End Make-Up Examinations

**Programme: B.E.**

**Branch: Institutional Elective**

**Course Code: 21MD7IEOPR**

**Course: Operations Research**

**Semester: VII**

**Duration: 3 hrs.**

**Max Marks: 100**

**Date: 17.05.2023**

**Instructions:** 1. Answer any FIVE full questions, choosing one full question from each unit.  
2. Missing data, if any, may be suitably assumed.

### UNIT - I

- 1 a) Briefly explain phases of O R 10  
b) Use simplex method to solve: Maximize  $Z = 3X_1 + 4X_2$  subject to  $3X_1 + 2X_2 \leq 6$ ,  $2X_1 + 4X_2 \leq 8$  and  $X_i \geq 0$  10

**OR**

- 2 a) Solve the following problem by simplex method: Maximize  $Z = 2X_1 + 3X_2$  subject to  $5X_1 + 3X_2 = 15$ ,  $4X_1 + 5X_2 = 20$  and  $X_i \geq 0$  10  
b) Use simplex method to solve: Maximize  $Z = 6X_1 + 4X_2$  subject to  $2X_1 + 3X_2 \leq 6$ ,  $6X_1 + 3X_2 \leq 12$  and  $X_i \geq 0$  10

### UNIT - II

- 3 a) Differentiate between transportation problem and assignment problem 06  
b) Obtain the optimal solution for the following transportation problem using North West Corner method. 14

Table 1

|          | A   | B   | C   | D   | Capacity |
|----------|-----|-----|-----|-----|----------|
| R1       | 12  | 14  | 18  | 15  | 250      |
| R2       | 15  | 18  | 16  | 13  | 300      |
| R3       | 18  | 19  | 15  | 14  | 350      |
| Required | 200 | 225 | 275 | 250 |          |

### UNIT - III

- 4 a) A company has five jobs to be done. The following matrix (table 2) shows the returns in Rupees on assigning  $i^{\text{th}}$  machine to  $j^{\text{th}}$  job. Assign the five jobs to the five machines. 10

**Important Note:** Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.

- b) A travelling salesman has to visit 5 cities. He wishes to start from a particular city, visit each city once and then return to his starting point. Cost of going from one city to another is shown in **table 3**. Find the least cost route and the optimal cost. **10**

Table 2

| Persons | Jobs |    |   |    |   |   |
|---------|------|----|---|----|---|---|
|         |      | 1  | 2 | 3  | 4 | 5 |
|         | A    | 11 | 5 | 12 | 4 | 5 |
|         | B    | 4  | 2 | 3  | 5 | 2 |
|         | C    | 12 | 3 | 14 | 6 | 3 |
|         | D    | 14 | 6 | 11 | 7 | 6 |

Table 3

|      | City |   |   |   |   |   |
|------|------|---|---|---|---|---|
| City |      | A | B | C | D | E |
|      | A    | - | 8 | 6 | 7 | 9 |
|      | B    | 6 | - | 7 | 9 | 8 |
|      | C    | 8 | 7 | - | 6 | 5 |
|      | D    | 7 | 5 | 9 | - | 6 |
|      | E    | 5 | 6 | 8 | 9 | - |

#### UNIT - IV

- 5 a) Differentiate between PERT and CPM **06**
- b) A project schedule has the following characteristics as shown in table 4. (i) Construct the project network, (ii) identify the critical path and project duration (iii) compute EST, EFT, LST, LFT, total float and free float for each activity **14**

Table 4

| Activity    | 1-2 | 1-3 | 2-4 | 3-4 | 3-5 | 4-9 | 5-6 | 5-7 | 6-8 | 7-8 | 8-10 | 9-10 |
|-------------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|------|------|
| Time (days) | 4   | 2   | 1   | 4   | 6   | 5   | 4   | 8   | 2   | 3   | 5    | 7    |

#### OR

- 6 a) Define Total Float, Independent Float, Free Float, Optimistic time, Most likely time and Pessimistic time **06**
- b) A project schedule has the following characteristic shown in table 5. (i) Construct the project network (ii) find the expected time and variance of the activities **14**
- (iii) Identify the critical path and expected project duration (iv) what is the probability of completing the project in 30 days schedule time (v) what is the probability of completing 3 days earlier than expected (vi) what is the probability that will not be completed one day later than the expected (vii) what due date 90% of chance of being met

Table 5

| Activity | 1-2 | 2-3 | 2-4 | 3-5 | 4-5 | 4-6 | 5-7 | 6-7 | 7-8 | 7-9 | 8-10 | 9-10 |
|----------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|------|------|
| Tm       | 2   | 2   | 3   | 4   | 3   | 5   | 5   | 7   | 4   | 6   | 2    | 5    |
| To       | 1   | 1   | 1   | 3   | 2   | 3   | 4   | 6   | 2   | 4   | 1    | 3    |
| Tp       | 3   | 3   | 5   | 5   | 4   | 7   | 6   | 8   | 6   | 8   | 3    | 7    |

## UNIT - V

- 7 a) Use the relation of dominance to solve the game whose payoff matrix is given in table 6 10
- b) Consider the payoff matrix of player A as shown in table 7. Solve it optimally using graphical method 10

Table 6

| Player A | Player B |    |    |     |    |    |    |
|----------|----------|----|----|-----|----|----|----|
|          |          | I  | II | III | IV | V  | VI |
|          | I        | 16 | 14 | 11  | 10 | 15 | 16 |
|          | II       | 12 | 18 | 13  | 12 | 14 | 17 |
|          | III      | 10 | 13 | 12  | 10 | 11 | 15 |
|          | IV       | 11 | 15 | 10  | 13 | 12 | 14 |
|          | V        | 12 | 17 | 17  | 15 | 16 | 18 |
|          | VI       | 12 | 10 | 11  | 14 | 12 | 13 |

Table 7

| Player A | Player B |   |   |   |   |   |   |
|----------|----------|---|---|---|---|---|---|
|          |          | 1 | 2 | 3 | 4 | 5 | 6 |
|          | 1        | 4 | 3 | 6 | 1 | 5 | 2 |
|          | 2        | 8 | 5 | 7 | 1 | 6 | 4 |
|          | 3        | 1 | 4 | 2 | 3 | 5 | 1 |
|          | 4        | 9 | 6 | 8 | 7 | 6 | 5 |
|          | 5        | 7 | 5 | 4 | 8 | 9 | 6 |
|          | 6        | 2 | 3 | 4 | 7 | 1 | 5 |

\*\*\*\*\*