

B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

July 2023 Semester End Main Examinations

Programme: B.E.

Branch: Institutional Elective

Course Code: 19MD80E3OR

Course: Operations Research

Semester: VIII

Duration: 3 hrs.

Max Marks: 100

Date: 06.07.2023

Instructions: 1. Answer any FIVE full questions, choosing one full question from each unit.
2. Missing data, if any, may be suitably assumed.

Important Note: Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.			UNIT - I	CO	PO	Marks
	1	a)	What are the different phases of OR? Briefly explain them.	CO1	PO1	06
		b)	Use simplex method to solve the LPP: Maximize: $Z = 3x_1 + 4x_2$ Subject to $x_1 - x_2 \leq 1$ $-x_1 + x_2 \leq 2$ $x_1, x_2 \geq 0$	CO1	PO2	07
		c)	Use graphical method to solve the following. Maximize: $Z = 3x_1 + 2x_2$, Subject to $5x_1 + x_2 \geq 10$ $x_1 + x_2 \geq 6$, $x_1 + 4x_2 \geq 12$ $x_1 \geq 0, x_2 \geq 0$	CO1	PO2	07
			OR			
	2	a)	Use simplex method to solve the following LPP, Minimize: $Z = x_1 - 3x_2 + 2x_3$ Subject to $3x_1 - x_2 + 2x_3 \leq 7$, $-2x_1 + 4x_2 \leq 12$, $-4x_1 + 3x_2 + 8x_3 \leq 10$ $x_1, x_2, x_3 \geq 0$	CO1	PO2	10
		b)	Solve the following LPP by Big -M method Minimize: $Z = 4x_1 + x_2$, Subject to $3x_1 + x_2 = 3$, $4x_1 + 3x_2 \geq 6$, $x_1 + 2x_2 \leq 4$ $x_1, x_2 \geq 0$	CO1	PO2	10

		UNIT - II																																																
3	a)	Determine an initial basic feasible solution to the following transportation problem by North-West corner rule and least cost method. <div><table><tr><td colspan="2" rowspan="2"></td><td colspan="3">To</td><td rowspan="2"></td></tr><tr><td>D1</td><td>D2</td><td>D3</td></tr><tr><td rowspan="4">From</td><td>O1</td><td>2</td><td>7</td><td>4</td><td>5</td></tr><tr><td>O2</td><td>3</td><td>3</td><td>1</td><td>8</td></tr><tr><td>O3</td><td>5</td><td>4</td><td>7</td><td>7</td></tr><tr><td>O4</td><td>1</td><td>6</td><td>2</td><td>14</td></tr><tr><td colspan="2"></td><td>7</td><td>9</td><td>18</td><td>34</td></tr><tr><td colspan="2"></td><td colspan="3">Demand</td><td></td></tr></table></div>			To				D1	D2	D3	From	O1	2	7	4	5	O2	3	3	1	8	O3	5	4	7	7	O4	1	6	2	14			7	9	18	34			Demand				CO2	PO2	10			
		To																																																
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	O2	3	3	1	8																																													
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	O4	1	6	2	14																																													
		7	9	18	34																																													
		Demand																																																
	b)	Determine the optimal solution by MODI method to the transportation problem of above example Q No.3, considering initial basic feasible solution obtained by Vogel's approximation method.	CO2	PO2	10																																													
		UNIT - III																																																
4	a)	Determine an optimum assignment schedule to the following problem. <div><table><tr><td colspan="2"></td><td colspan="5">Job</td></tr><tr><td colspan="2"></td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td></tr><tr><td rowspan="5">Person</td><td>A</td><td>8</td><td>4</td><td>2</td><td>6</td><td>1</td></tr><tr><td>B</td><td>0</td><td>9</td><td>5</td><td>5</td><td>4</td></tr><tr><td>C</td><td>3</td><td>8</td><td>9</td><td>2</td><td>6</td></tr><tr><td>D</td><td>4</td><td>3</td><td>1</td><td>0</td><td>3</td></tr><tr><td>E</td><td>9</td><td>5</td><td>8</td><td>9</td><td>5</td></tr></table></div>			Job							1	2	3	4	5	Person	A	8	4	2	6	1	B	0	9	5	5	4	C	3	8	9	2	6	D	4	3	1	0	3	E	9	5	8	9	5	CO3	PO2	10
		Job																																																
		1	2	3	4	5																																												
Person	A	8	4	2	6	1																																												
	B	0	9	5	5	4																																												
	C	3	8	9	2	6																																												
	D	4	3	1	0	3																																												
	E	9	5	8	9	5																																												
	b)	Solve the following travelling salesman problem. <div><table><tr><td>To From</td><td>A</td><td>B</td><td>C</td><td>D</td><td>E</td></tr><tr><td>A</td><td>∞</td><td>4</td><td>7</td><td>3</td><td>4</td></tr><tr><td>B</td><td>4</td><td>∞</td><td>6</td><td>3</td><td>4</td></tr><tr><td>C</td><td>7</td><td>6</td><td>∞</td><td>7</td><td>5</td></tr><tr><td>D</td><td>3</td><td>3</td><td>7</td><td>∞</td><td>7</td></tr><tr><td>E</td><td>4</td><td>4</td><td>5</td><td>7</td><td>∞</td></tr></table></div>	To From	A	B	C	D	E	A	∞	4	7	3	4	B	4	∞	6	3	4	C	7	6	∞	7	5	D	3	3	7	∞	7	E	4	4	5	7	∞	CO3	PO2	10									
To From	A	B	C	D	E																																													
A	∞	4	7	3	4																																													
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C	7	6	∞	7	5																																													
D	3	3	7	∞	7																																													
E	4	4	5	7	∞																																													

		UNIT - IV																																																								
5	a)	A project consists of 12 activities. Table below shows the duration for each activity in days. a) Draw the network of the project and number the events as per Fulkerson's rule. b) Establish the critical path and determine the project duration.				CO4	PO2	10																																																		
		<table><tr><td>Activity</td><td>Preceded by</td><td>Duration</td><td>Activity</td><td>Preceded by</td><td>Duration</td></tr><tr><td>A</td><td>-</td><td>5</td><td>G</td><td>E</td><td>3</td></tr><tr><td>B</td><td>A</td><td>9</td><td>H</td><td>E</td><td>9</td></tr><tr><td>C</td><td>A</td><td>7</td><td>J</td><td>A</td><td>7</td></tr><tr><td>D</td><td>A</td><td>5</td><td>K</td><td>H</td><td>9</td></tr><tr><td>E</td><td>C</td><td>12</td><td>L</td><td>F</td><td>5</td></tr><tr><td>F</td><td>C</td><td>9</td><td>M</td><td>G,K</td><td>5</td></tr></table>						Activity	Preceded by	Duration	Activity	Preceded by	Duration	A	-	5	G	E	3	B	A	9	H	E	9	C	A	7	J	A	7	D	A	5	K	H	9	E	C	12	L	F	5	F	C	9	M	G,K	5									
Activity	Preceded by	Duration	Activity	Preceded by	Duration																																																					
A	-	5	G	E	3																																																					
B	A	9	H	E	9																																																					
C	A	7	J	A	7																																																					
D	A	5	K	H	9																																																					
E	C	12	L	F	5																																																					
F	C	9	M	G,K	5																																																					
	b)	Fusion Engineering Inc. is designing a new product for welding two different alloys. The company has limited time and resources to complete the project. The following activity information is available.				CO4	PO2	10																																																		
		<table><tr><td>Activity</td><td>Immediate Predecessors</td><td>Normal Time (Days)</td><td>Normal Cost(\$)</td><td>Crash Cost/Day(\$)</td><td>Crash Time (Days)</td></tr><tr><td>A</td><td>-</td><td>4</td><td>400</td><td>125</td><td>3</td></tr><tr><td>B</td><td>A</td><td>5</td><td>800</td><td>200</td><td>4</td></tr><tr><td>C</td><td>A</td><td>4</td><td>520</td><td>150</td><td>2</td></tr><tr><td>D</td><td>B</td><td>3</td><td>600</td><td>225</td><td>2</td></tr><tr><td>E</td><td>C</td><td>3</td><td>255</td><td>100</td><td>2</td></tr><tr><td>F</td><td>B,E</td><td>4</td><td>600</td><td>175</td><td>2</td></tr></table> <p>(i)Draw the project network and find the critical path. (ii)Find the project completing time and corresponding cost. (iii)What is the total cost, if the project deadline is 12 days.</p>						Activity	Immediate Predecessors	Normal Time (Days)	Normal Cost(\$)	Crash Cost/Day(\$)	Crash Time (Days)	A	-	4	400	125	3	B	A	5	800	200	4	C	A	4	520	150	2	D	B	3	600	225	2	E	C	3	255	100	2	F	B,E	4	600	175	2									
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E	C	3	255	100	2																																																					
F	B,E	4	600	175	2																																																					
		OR																																																								
6	a)	A building project consists of ten activities whose precedence relationships are identified by their node numbers.				CO4	PO2	10																																																		
		<table><tr><td>Activity</td><td>Initial node</td><td>Final node</td><td>Time days</td><td>Activity</td><td>Initial node</td><td>Final node</td><td>Time days</td></tr><tr><td>A</td><td>1</td><td>2</td><td>5</td><td>F</td><td>4</td><td>5</td><td>2</td></tr><tr><td>B</td><td>2</td><td>3</td><td>2</td><td>G</td><td>4</td><td>7</td><td>3</td></tr><tr><td>C</td><td>2</td><td>4</td><td>6</td><td>H</td><td>6</td><td>8</td><td>8</td></tr><tr><td>D</td><td>3</td><td>6</td><td>4</td><td>I</td><td>5</td><td>8</td><td>7</td></tr><tr><td>E</td><td>3</td><td>5</td><td>4</td><td>J</td><td>7</td><td>8</td><td>2</td></tr></table> <p>Determine i) Activity times ii) Total float iii) Critical path.</p>						Activity	Initial node	Final node	Time days	Activity	Initial node	Final node	Time days	A	1	2	5	F	4	5	2	B	2	3	2	G	4	7	3	C	2	4	6	H	6	8	8	D	3	6	4	I	5	8	7	E	3	5	4	J	7	8	2			
Activity	Initial node	Final node	Time days	Activity	Initial node	Final node	Time days																																																			
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E	3	5	4	J	7	8	2																																																			

	b)	<div>Table below shows jobs, normal and crash time and cost of a project.</div> <table><thead><tr><th>Job</th><th>T_n (days)</th><th>C_n (Rs.)</th><th>T_c (days)</th><th>C_c (Rs.)</th></tr></thead><tbody><tr><td>1-2</td><td>6</td><td>1400</td><td>4</td><td>1900</td></tr><tr><td>1-3</td><td>8</td><td>2000</td><td>5</td><td>2800</td></tr><tr><td>2-3</td><td>4</td><td>1100</td><td>2</td><td>1500</td></tr><tr><td>2-4</td><td>3</td><td>800</td><td>2</td><td>1400</td></tr><tr><td>3-4</td><td>Dummy</td><td>-----</td><td>-----</td><td>-----</td></tr><tr><td>2-5</td><td>6</td><td>900</td><td>3</td><td>1600</td></tr><tr><td>4-6</td><td>10</td><td>2500</td><td>6</td><td>3500</td></tr><tr><td>5-6</td><td>3</td><td>500</td><td>2</td><td>800</td></tr></tbody></table> <div>Indirect cost for the project is Rs. 300/- per day.</div> <div>a) Draw the network. b) What is the normal duration and cost of the project. c) Find optimum duration and minimum project cost.</div>	Job	T _n (days)	C _n (Rs.)	T _c (days)	C _c (Rs.)	1-2	6	1400	4	1900	1-3	8	2000	5	2800	2-3	4	1100	2	1500	2-4	3	800	2	1400	3-4	Dummy	-----	-----	-----	2-5	6	900	3	1600	4-6	10	2500	6	3500	5-6	3	500	2	800	CO4	PO2	10														
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		UNIT - V																																																														
7	a)	<div>Solve the following game.</div> <div><table><tr><td></td><td></td><td colspan="4">B</td></tr><tr><td></td><td></td><td>I</td><td>II</td><td>III</td><td>IV</td></tr><tr><td rowspan="4">A</td><td>I</td><td>1</td><td>9</td><td>6</td><td>0</td></tr><tr><td>II</td><td>2</td><td>3</td><td>8</td><td>-1</td></tr><tr><td>III</td><td>-5</td><td>-2</td><td>10</td><td>-3</td></tr><tr><td>IV</td><td>7</td><td>4</td><td>-2</td><td>-5</td></tr></table></div>			B						I	II	III	IV	A	I	1	9	6	0	II	2	3	8	-1	III	-5	-2	10	-3	IV	7	4	-2	-5	CO5	PO2	08																										
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A	I	1	9	6	0																																																											
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	III	-5	-2	10	-3																																																											
	IV	7	4	-2	-5																																																											
	b)	<div>Use dominance to solve the following game.</div> <div><table><tr><td></td><td></td><td colspan="6">B</td></tr><tr><td></td><td></td><td>I</td><td>II</td><td>III</td><td>IV</td><td>V</td><td>VI</td></tr><tr><td rowspan="6">A</td><td>I</td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td></tr><tr><td>II</td><td>4</td><td>2</td><td>0</td><td>2</td><td>1</td><td>1</td></tr><tr><td>III</td><td>4</td><td>3</td><td>1</td><td>3</td><td>2</td><td>2</td></tr><tr><td>IV</td><td>4</td><td>3</td><td>7</td><td>-5</td><td>1</td><td>2</td></tr><tr><td>V</td><td>4</td><td>3</td><td>4</td><td>-1</td><td>2</td><td>2</td></tr><tr><td>VI</td><td>4</td><td>3</td><td>3</td><td>-2</td><td>2</td><td>2</td></tr></table></div>			B								I	II	III	IV	V	VI	A	I	0	0	0	0	0	0	II	4	2	0	2	1	1	III	4	3	1	3	2	2	IV	4	3	7	-5	1	2	V	4	3	4	-1	2	2	VI	4	3	3	-2	2	2	CO5	PO2	12
		B																																																														
		I	II	III	IV	V	VI																																																									
A	I	0	0	0	0	0	0																																																									
	II	4	2	0	2	1	1																																																									
	III	4	3	1	3	2	2																																																									
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	V	4	3	4	-1	2	2																																																									
	VI	4	3	3	-2	2	2																																																									
