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B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

July 2023 Semester End Main Examinations

Programme: B.E.

Branch: Institutional Elective

Course Code: 19MD8OE3OR

Course: Operations Research

Semester: VIII

Duration: 3 hrs.

Max Marks: 100

Date: 06.07.2023

Instructions: 1. Answer any FIVE full questions, choosing one full question from each unit.
2. Missing data, if any, may be suitably assumed.

UNIT - I			CO	PO	Marks
Important Note: Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.	1	a)	What are the different phases of OR? Briefly explain them.	<i>CO1</i>	<i>PO1</i> 06
		b)	Use simplex method to solve the LPP: Maximize: $Z = 3x_1 + 4x_2$ <p>Subject to</p> $x_1 - x_2 \leq 1$ $-x_1 + x_2 \leq 2$ $x_1, x_2 \geq 0$	<i>CO1</i>	<i>PO2</i> 07
		c)	Use graphical method to solve the following. Maximize: $Z = 3x_1 + 2x_2$, Subject to $5x_1 + x_2 \geq 10$ $x_1 + x_2 \geq 6$ $x_1 + 4x_2 \geq 12$ $x_1 \geq 0, x_2 \geq 0$	<i>CO1</i>	<i>PO2</i> 07
OR					
	2	a)	Use simplex method to solve the following LPP, Minimize: $Z = x_1 - 3x_2 + 2x_3$ Subject to $3x_1 - x_2 + 2x_3 \leq 7$ $-2x_1 + 4x_2 \leq 12$ $-4x_1 + 3x_2 + 8x_3 \leq 10$ $x_1, x_2, x_3 \geq 0$	<i>CO1</i>	<i>PO2</i> 10
		b)	Solve the following LPP by Big -M method Minimize: $Z = 4x_1 + x_2$, Subject to $3x_1 + x_2 = 3$, $4x_1 + 3x_2 \geq 6$ $x_1 + 2x_2 \leq 4$ $x_1, x_2 \geq 0$	<i>CO1</i>	<i>PO2</i> 10

UNIT - II																																																						
3	a)	Determine an initial basic feasible solution to the following transportation problem by North-West corner rule and least cost method.																																																				
<table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th colspan="2"></th> <th colspan="3" style="text-align: center;">To</th> <th colspan="2"></th> </tr> <tr> <th colspan="2"></th> <th style="text-align: center;">D1</th> <th style="text-align: center;">D2</th> <th style="text-align: center;">D3</th> <th colspan="2"></th> </tr> <tr> <th rowspan="5" style="text-align: center; vertical-align: middle;">From</th> <th style="text-align: center;">O1</th> <td style="text-align: center;">2</td> <td style="text-align: center;">7</td> <td style="text-align: center;">4</td> <td style="text-align: center;">5</td> <td rowspan="5" style="text-align: center; vertical-align: middle;">Supply</td> </tr> </thead> <tbody> <tr> <th style="text-align: center;">O2</th> <td style="text-align: center;">3</td> <td style="text-align: center;">3</td> <td style="text-align: center;">1</td> <td style="text-align: center;">8</td> </tr> <tr> <th style="text-align: center;">O3</th> <td style="text-align: center;">5</td> <td style="text-align: center;">4</td> <td style="text-align: center;">7</td> <td style="text-align: center;">7</td> </tr> <tr> <th style="text-align: center;">O4</th> <td style="text-align: center;">1</td> <td style="text-align: center;">6</td> <td style="text-align: center;">2</td> <td style="text-align: center;">14</td> </tr> <tr> <th colspan="2"></th> <td style="text-align: center;">7</td> <td style="text-align: center;">9</td> <td style="text-align: center;">18</td> <td style="text-align: center;">34</td> </tr> <tr> <th colspan="6" style="text-align: center;">Demand</th><th></th></tr> </tbody> </table>								To							D1	D2	D3			From	O1	2	7	4	5	Supply	O2	3	3	1	8	O3	5	4	7	7	O4	1	6	2	14			7	9	18	34	Demand						
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b) Determine the optimal solution by MODI method to the transportation problem of above example Q No.3, considering initial basic feasible solution obtained by Vogel's approximation method.																																																						
UNIT - III																																																						
4	a)	Determine an optimum assignment schedule to the following problem.																																																				
<table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th rowspan="6" style="text-align: center; vertical-align: middle;">Person</th> <th colspan="5" style="text-align: center;">Job</th> <th rowspan="6"></th> </tr> <tr> <th style="text-align: center;">1</th> <th style="text-align: center;">2</th> <th style="text-align: center;">3</th> <th style="text-align: center;">4</th> <th style="text-align: center;">5</th> </tr> </thead> <tbody> <tr> <th style="text-align: center;">A</th> <td style="text-align: center;">8</td> <td style="text-align: center;">4</td> <td style="text-align: center;">2</td> <td style="text-align: center;">6</td> <td style="text-align: center;">1</td> </tr> <tr> <th style="text-align: center;">B</th> <td style="text-align: center;">0</td> <td style="text-align: center;">9</td> <td style="text-align: center;">5</td> <td style="text-align: center;">5</td> <td style="text-align: center;">4</td> </tr> <tr> <th style="text-align: center;">C</th> <td style="text-align: center;">3</td> <td style="text-align: center;">8</td> <td style="text-align: center;">9</td> <td style="text-align: center;">2</td> <td style="text-align: center;">6</td> </tr> <tr> <th style="text-align: center;">D</th> <td style="text-align: center;">4</td> <td style="text-align: center;">3</td> <td style="text-align: center;">1</td> <td style="text-align: center;">0</td> <td style="text-align: center;">3</td> </tr> <tr> <th style="text-align: center;">E</th> <td style="text-align: center;">9</td> <td style="text-align: center;">5</td> <td style="text-align: center;">8</td> <td style="text-align: center;">9</td> <td style="text-align: center;">5</td> <th></th> </tr> </tbody> </table>						Person	Job						1	2	3	4	5	A	8	4	2	6	1	B	0	9	5	5	4	C	3	8	9	2	6	D	4	3	1	0	3	E	9	5	8	9	5							
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		UNIT - IV																																																									
5	a)	<p>A project consists of 12 activities. Table below shows the duration for each activity in days.</p> <p>a) Draw the network of the project and number the events as per Fulkerson's rule.</p> <p>b) Establish the critical path and determine the project duration.</p>						CO4	PO2	10																																																	
		<table border="1"> <thead> <tr> <th>Activity</th><th>Preceded by</th><th>Duration</th><th>Activity</th><th>Preceded by</th><th>Duration</th></tr> </thead> <tbody> <tr> <td>A</td><td>-</td><td>5</td><td>G</td><td>E</td><td>3</td></tr> <tr> <td>B</td><td>A</td><td>9</td><td>H</td><td>E</td><td>9</td></tr> <tr> <td>C</td><td>A</td><td>7</td><td>J</td><td>A</td><td>7</td></tr> <tr> <td>D</td><td>A</td><td>5</td><td>K</td><td>H</td><td>9</td></tr> <tr> <td>E</td><td>C</td><td>12</td><td>L</td><td>F</td><td>5</td></tr> <tr> <td>F</td><td>C</td><td>9</td><td>M</td><td>G,K</td><td>5</td></tr> </tbody> </table>							Activity	Preceded by	Duration	Activity	Preceded by	Duration	A	-	5	G	E	3	B	A	9	H	E	9	C	A	7	J	A	7	D	A	5	K	H	9	E	C	12	L	F	5	F	C	9	M	G,K	5									
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	b)	<p>Fusion Engineering Inc. is designing a new product for welding two different alloys. The company has limited time and resources to complete the project. The following activity information is available.</p> <table border="1"> <thead> <tr> <th>Activity</th><th>Immediate Predecessors</th><th>Normal Time (Days)</th><th>Normal Cost(\$)</th><th>Crash Cost/ Day(\$)</th><th>Crash Time (Days)</th></tr> </thead> <tbody> <tr> <td>A</td><td>-</td><td>4</td><td>400</td><td>125</td><td>3</td></tr> <tr> <td>B</td><td>A</td><td>5</td><td>800</td><td>200</td><td>4</td></tr> <tr> <td>C</td><td>A</td><td>4</td><td>520</td><td>150</td><td>2</td></tr> <tr> <td>D</td><td>B</td><td>3</td><td>600</td><td>225</td><td>2</td></tr> <tr> <td>E</td><td>C</td><td>3</td><td>255</td><td>100</td><td>2</td></tr> <tr> <td>F</td><td>B,E</td><td>4</td><td>600</td><td>175</td><td>2</td></tr> </tbody> </table> <p>(i)Draw the project network and find the critical path. (ii)Find the project completing time and corresponding cost. (iii)What is the total cost, if the project deadline is 12 days.</p>							Activity	Immediate Predecessors	Normal Time (Days)	Normal Cost(\$)	Crash Cost/ Day(\$)	Crash Time (Days)	A	-	4	400	125	3	B	A	5	800	200	4	C	A	4	520	150	2	D	B	3	600	225	2	E	C	3	255	100	2	F	B,E	4	600	175	2	CO4	PO2	10						
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6	a)	<p>A building project consists of ten activities whose precedence relationships are identified by their node numbers.</p> <table border="1"> <thead> <tr> <th>Activity</th><th>Initial node</th><th>Final node</th><th>Time days</th><th>Activity</th><th>Initial node</th><th>Final node</th><th>Time days</th></tr> </thead> <tbody> <tr> <td>A</td><td>1</td><td>2</td><td>5</td><td>F</td><td>4</td><td>5</td><td>2</td></tr> <tr> <td>B</td><td>2</td><td>3</td><td>2</td><td>G</td><td>4</td><td>7</td><td>3</td></tr> <tr> <td>C</td><td>2</td><td>4</td><td>6</td><td>H</td><td>6</td><td>8</td><td>8</td></tr> <tr> <td>D</td><td>3</td><td>6</td><td>4</td><td>I</td><td>5</td><td>8</td><td>7</td></tr> <tr> <td>E</td><td>3</td><td>5</td><td>4</td><td>J</td><td>7</td><td>8</td><td>2</td></tr> </tbody> </table> <p>Determine i) Activity times ii) Total float iii) Critical path.</p>							Activity	Initial node	Final node	Time days	Activity	Initial node	Final node	Time days	A	1	2	5	F	4	5	2	B	2	3	2	G	4	7	3	C	2	4	6	H	6	8	8	D	3	6	4	I	5	8	7	E	3	5	4	J	7	8	2	CO4	PO2	10
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	b)	<p>Table below shows jobs, normal and crash time and cost of a project.</p> <table border="1"> <thead> <tr> <th>Job</th><th>T_n (days)</th><th>C_n (Rs.)</th><th>T_c (days)</th><th>C_c (Rs.)</th></tr> </thead> <tbody> <tr> <td>1-2</td><td>6</td><td>1400</td><td>4</td><td>1900</td></tr> <tr> <td>1-3</td><td>8</td><td>2000</td><td>5</td><td>2800</td></tr> <tr> <td>2-3</td><td>4</td><td>1100</td><td>2</td><td>1500</td></tr> <tr> <td>2-4</td><td>3</td><td>800</td><td>2</td><td>1400</td></tr> <tr> <td>3-4</td><td>Dummy</td><td>-----</td><td>-----</td><td>-----</td></tr> <tr> <td>2-5</td><td>6</td><td>900</td><td>3</td><td>1600</td></tr> <tr> <td>4-6</td><td>10</td><td>2500</td><td>6</td><td>3500</td></tr> <tr> <td>5-6</td><td>3</td><td>500</td><td>2</td><td>800</td></tr> </tbody> </table> <p>Indirect cost for the project is Rs. 300/- per day.</p> <p>a) Draw the network. b) What is the normal duration and cost of the project. c) Find optimum duration and minimum project cost.</p>	Job	T _n (days)	C _n (Rs.)	T _c (days)	C _c (Rs.)	1-2	6	1400	4	1900	1-3	8	2000	5	2800	2-3	4	1100	2	1500	2-4	3	800	2	1400	3-4	Dummy	-----	-----	-----	2-5	6	900	3	1600	4-6	10	2500	6	3500	5-6	3	500	2	800	CO4	PO2	10
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		UNIT - V																																																
7	a)	Solve the following game.		CO5	PO2	08																																												
		$ \begin{array}{c} & & \text{B} \\ & \text{I} & \text{II} & \text{III} & \text{IV} \\ \text{I} & 1 & 9 & 6 & 0 \\ \text{II} & 2 & 3 & 8 & -1 \\ \text{A} & \text{III} & -5 & -2 & 10 & -3 \\ \text{IV} & 7 & 4 & -2 & -5 \end{array} $																																																
	b)	Use dominance to solve the following game.		CO5	PO2	12																																												
		$ \begin{array}{c} & & \text{B} \\ & \text{A} & & & & & \\ & \text{I} & \text{II} & \text{III} & \text{IV} & \text{V} & \text{VI} \\ \hline \text{I} & 0 & 0 & 0 & 0 & 0 & 0 \\ \text{II} & 4 & 2 & 0 & 2 & 1 & 1 \\ \text{III} & 4 & 3 & 1 & 3 & 2 & 2 \\ \text{IV} & 4 & 3 & 7 & -5 & 1 & 2 \\ \text{V} & 4 & 3 & 4 & -1 & 2 & 2 \\ \text{VI} & 4 & 3 & 3 & -2 & 2 & 2 \end{array} $																																																
