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# B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

## September / October 2023 Supplementary Examinations

**Programme: B.E.**

**Branch: Institutional Electives**

**Course Code: 19MD8OE3OR**

**Course: Operations Research**

**Semester: VIII**

**Duration: 3 hrs.**

**Max Marks: 100**

**Instructions:** 1. Answer any FIVE full questions, choosing one full question from each unit.  
2. Missing data, if any, may be suitably assumed.

		UNIT - I			CO	PO	Marks																						
1	a)	Define: i) Feasible solution ii) Slack variable iii) Unbounded solution			CO1	PO1	<b>06</b>																						
	b)	A company manufactures two types of printed circuits. The requirements of transistors, resistors and capacitors for each type of printed circuits along with other data are given in the below table:			CO1	PO2	<b>06</b>																						
		<table border="1"> <thead> <tr> <th rowspan="2"></th> <th colspan="3">Circuit</th> </tr> <tr> <th>A</th> <th>B</th> <th>Stock Available</th> </tr> </thead> <tbody> <tr> <td>Transistor</td> <td>15</td> <td>10</td> <td>180</td> </tr> <tr> <td>Resistors</td> <td>10</td> <td>20</td> <td>200</td> </tr> <tr> <td>Capacitor</td> <td>15</td> <td>20</td> <td>210</td> </tr> <tr> <td>Profit</td> <td>Rs.5</td> <td>Rs.8</td> <td></td> </tr> </tbody> </table>		Circuit			A	B	Stock Available	Transistor	15	10	180	Resistors	10	20	200	Capacitor	15	20	210	Profit	Rs.5	Rs.8					
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		How many circuits of each type should the company produce from the stock to earn maximum profit.																											
	c)	Use simplex method to solve the LPP: Minimize : $Z = x_1 - 3x_2 + 2x_3$ subject to $3x_1 - x_2 + 2x_3 \leq 7$ $-2x_1 + 4x_2 \leq 12$ $-4x_1 + 3x_2 + 8x_3 \leq 10$ $x_1, x_2, x_3 \geq 0$			CO1	PO2	<b>08</b>																						
		<b>OR</b>																											

**Important Note:** Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.

	2	a)	Using Big M method solve the given LPP : Minimize: $z = 4x_1 + x_2$ subject to $3x_1 + x_2 = 3$ $4x_1 + 3x_2 \geq 6$ $x_1 + 2x_2 \leq 4$ $x_1, x_2 \geq 0$	CO1	PO2	10																																											
		b)	Use simplex method to solve the LPP: Maximize: $Z = x_1 + 2x_2 + x_3$ subject to $2x_1 + x_2 - x_3 \leq 2$ $x_1 - x_2 + 5x_3 \leq 6$ $4x_1 + x_2 + x_3 \leq 6$ $x_1, x_2, x_3 \geq 0$	CO1	PO2	10																																											
<b>UNIT - II</b>																																																	
3	a)		Find the optimal solution for the given transportation problem. (Use Vogel's approximation method to obtain the initial basic feasible solution)	CO2	PO2	10																																											
<table border="1" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th colspan="2" rowspan="2"></th> <th colspan="5">TO</th> <th rowspan="2">SUPPLY</th> </tr> <tr> <th>A</th> <th>B</th> <th>C</th> <th>D</th> <th>E</th> </tr> </thead> <tbody> <tr> <th rowspan="3">FROM</th> <th>1</th> <td>4</td> <td>2</td> <td>3</td> <td>2</td> <td>6</td> <td>8</td> </tr> <tr> <th>2</th> <td>5</td> <td>4</td> <td>5</td> <td>2</td> <td>1</td> <td>12</td> </tr> <tr> <th>3</th> <td>6</td> <td>5</td> <td>4</td> <td>7</td> <td>3</td> <td>14</td> </tr> <tr> <th>DEMAND</th> <td></td> <td>4</td> <td>4</td> <td>6</td> <td>8</td> <td>8</td> <td></td> </tr> </tbody> </table>									TO					SUPPLY	A	B	C	D	E	FROM	1	4	2	3	2	6	8	2	5	4	5	2	1	12	3	6	5	4	7	3	14	DEMAND		4	4	6	8	8	
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	b)		Solve the transportation problem to maximize the optimum profit	CO2	PO2	10																																											
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		UNIT - III																																													
4	a)	A company has 5 jobs to be done. The following matrix shows the return in rupees on assigning ith ( $i = 1, 2, 3, 4, 5$ ) machine to the jth job ( $j = A, B, C, D, E$ ). Assign the five jobs to the five machines so as to maximize the total expected profit.						CO3	PO2	<b>10</b>																																					
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	b)	Solve the following travelling salesman problem						CO3	PO2	<b>10</b>																																					
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5	a)	A project has the following time schedule.						CO4	PO2	<b>10</b>																																					
		<table border="1"> <thead> <tr> <th>Activity</th><th>Time in Weeks</th><th>Activity</th><th>Time in Weeks</th></tr> </thead> <tbody> <tr> <td>(1-2)</td><td>2</td><td>4-6</td><td>3</td></tr> <tr> <td>(1-3)</td><td>2</td><td>5-8</td><td>1</td></tr> <tr> <td>(1-4)</td><td>1</td><td>6-9</td><td>5</td></tr> <tr> <td>(2-5)</td><td>4</td><td>7-8</td><td>4</td></tr> <tr> <td>(3-6)</td><td>8</td><td>8-9</td><td>3</td></tr> <tr> <td>(3-7)</td><td>5</td><td></td><td></td></tr> </tbody> </table>						Activity	Time in Weeks	Activity	Time in Weeks	(1-2)	2	4-6	3	(1-3)	2	5-8	1	(1-4)	1	6-9	5	(2-5)	4	7-8	4	(3-6)	8	8-9	3	(3-7)	5														
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(3-7)	5																																														
		Construct CPM network and compute i) Total float for each activity ii) Critical path and its duration.																																													
	b)	Consider the project network below with activity times given in days						CO4	PO2	<b>10</b>																																					

		<p>The normal and crash data for this project are as follows</p> <table border="1"> <thead> <tr> <th>Activity</th><th>Normal time (Days)</th><th>Crash time (Days)</th><th>Normal cost (\$)</th><th>Crash cost (\$)</th></tr> </thead> <tbody> <tr> <td>A</td><td>4</td><td>3</td><td>80</td><td>105</td></tr> <tr> <td>B</td><td>6</td><td>4</td><td>180</td><td>250</td></tr> <tr> <td>C</td><td>8</td><td>5</td><td>200</td><td>320</td></tr> <tr> <td>D</td><td>10</td><td>6</td><td>350</td><td>530</td></tr> </tbody> </table> <p>         i) Find the Critical path          ii) Find the project completion time and the corresponding cost.          iii) If we want to complete the project in 19 days, then find the best crash time and cost.       </p>	Activity	Normal time (Days)	Crash time (Days)	Normal cost (\$)	Crash cost (\$)	A	4	3	80	105	B	6	4	180	250	C	8	5	200	320	D	10	6	350	530																					
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		<b>OR</b>																																														
6	a)	<p>Fusion Engineering Inc. is designing a new product for welding two different alloys. The company has limited time and resources to complete the project. The following activity information is available.</p> <table border="1"> <thead> <tr> <th>Activity</th><th>Immediate Predecessors</th><th>Normal Time (Days)</th><th>Normal Cost(\$)</th><th>Crash Cost/ Day(\$)</th><th>Crash Time (Days)</th></tr> </thead> <tbody> <tr> <td>A</td><td>-</td><td>4</td><td>400</td><td>125</td><td>3</td></tr> <tr> <td>B</td><td>A</td><td>5</td><td>800</td><td>200</td><td>4</td></tr> <tr> <td>C</td><td>A</td><td>4</td><td>520</td><td>150</td><td>2</td></tr> <tr> <td>D</td><td>B</td><td>3</td><td>600</td><td>225</td><td>2</td></tr> <tr> <td>E</td><td>C</td><td>3</td><td>255</td><td>100</td><td>2</td></tr> <tr> <td>F</td><td>B,E</td><td>4</td><td>600</td><td>175</td><td>2</td></tr> </tbody> </table> <p>         (i)Draw the project network and find the critical path.          (ii)Find the project completing time and corresponding cost.          (iii)What is the total cost, if the project deadline is 12 days.       </p>	Activity	Immediate Predecessors	Normal Time (Days)	Normal Cost(\$)	Crash Cost/ Day(\$)	Crash Time (Days)	A	-	4	400	125	3	B	A	5	800	200	4	C	A	4	520	150	2	D	B	3	600	225	2	E	C	3	255	100	2	F	B,E	4	600	175	2	CO4	PO2	10	
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	b)	<p>The following table lists the data for a PERT network with their time estimates</p> <table border="1"> <thead> <tr> <th rowspan="2">Activity [i-j]</th><th colspan="3">Duration (Weeks)</th></tr> <tr> <th>Optimistic</th><th>Most likely</th><th>Pessimistic</th></tr> </thead> <tbody> <tr> <td>1-2</td><td>5</td><td>8</td><td>10</td></tr> <tr> <td>1-3</td><td>18</td><td>20</td><td>22</td></tr> <tr> <td>1-4</td><td>26</td><td>33</td><td>40</td></tr> <tr> <td>2-5</td><td>16</td><td>18</td><td>20</td></tr> <tr> <td>2-6</td><td>15</td><td>20</td><td>25</td></tr> <tr> <td>3-6</td><td>6</td><td>9</td><td>12</td></tr> <tr> <td>4-7</td><td>7</td><td>10</td><td>12</td></tr> <tr> <td>5-7</td><td>7</td><td>8</td><td>9</td></tr> <tr> <td>6-7</td><td>3</td><td>4</td><td>5</td></tr> </tbody> </table> <p>         i) Draw the project network.          ii) Calculate the mean and variance of the critical path.          iii) What is the probability that the project will be completed in 41.5 weeks? [Given : <math>P(0 &lt; z &lt; 0.52) = 0.30</math>]       </p>	Activity [i-j]	Duration (Weeks)			Optimistic	Most likely	Pessimistic	1-2	5	8	10	1-3	18	20	22	1-4	26	33	40	2-5	16	18	20	2-6	15	20	25	3-6	6	9	12	4-7	7	10	12	5-7	7	8	9	6-7	3	4	5	CO4	PO2	10
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		<b>UNIT - V</b>																																														
7	a)	Define: 1) saddle point 2) Pay off matrix 3) Zero sum Two person game	CO5	PO1	06																																											

		b)	<p>Solve the following <math>3 \times 5</math> game using dominance rule</p> <table border="1"> <thead> <tr> <th colspan="2" rowspan="2"></th><th colspan="5">COMPANY B</th></tr> <tr> <th><b>B<sub>1</sub></b></th><th><b>B<sub>2</sub></b></th><th><b>B<sub>3</sub></b></th><th><b>B<sub>4</sub></b></th><th><b>B<sub>5</sub></b></th></tr> </thead> <tbody> <tr> <th rowspan="3">COMPANY A</th><th><b>A<sub>1</sub></b></th><td>2</td><td>5</td><td>10</td><td>7</td><td>2</td></tr> <tr> <th><b>A<sub>2</sub></b></th><td>3</td><td>3</td><td>6</td><td>6</td><td>4</td></tr> <tr> <th><b>A<sub>3</sub></b></th><td>4</td><td>4</td><td>8</td><td>12</td><td>1</td></tr> </tbody> </table> <p>Use dominance principle to find the optimal strategies.</p>			COMPANY B					<b>B<sub>1</sub></b>	<b>B<sub>2</sub></b>	<b>B<sub>3</sub></b>	<b>B<sub>4</sub></b>	<b>B<sub>5</sub></b>	COMPANY A	<b>A<sub>1</sub></b>	2	5	10	7	2	<b>A<sub>2</sub></b>	3	3	6	6	4	<b>A<sub>3</sub></b>	4	4	8	12	1	<i>CO5</i>	<i>PO2</i>	<b>07</b>
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		c)	<p>Solve the game graphically whose payoff matrix for the players A is given in as follows:</p> <table> <thead> <tr> <th colspan="2"></th> <th colspan="4">Player B</th> </tr> <tr> <th colspan="2"></th> <th><i>B<sub>1</sub></i></th> <th><i>B<sub>2</sub></i></th> <th><i>B<sub>3</sub></i></th> <th><i>B<sub>4</sub></i></th> </tr> <tr> <th rowspan="2">Player A</th> <th><i>A<sub>1</sub></i></th> <td>2</td> <td>1</td> <td>0</td> <td>-2</td> </tr> </thead> <tbody> <tr> <th><i>A<sub>2</sub></i></th> <td>1</td> <td>0</td> <td>3</td> <td>2</td> </tr> </tbody> </table>			Player B						<i>B<sub>1</sub></i>	<i>B<sub>2</sub></i>	<i>B<sub>3</sub></i>	<i>B<sub>4</sub></i>	Player A	<i>A<sub>1</sub></i>	2	1	0	-2	<i>A<sub>2</sub></i>	1	0	3	2	<i>CO5</i>	<i>PO2</i>	<b>07</b>								
		Player B																																			
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Player A	<i>A<sub>1</sub></i>	2	1	0	-2																																
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